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Par

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Development and application of through-bond and through-space correlation NMR experiments between spin-1/2 and quadrupolar nuclei in crystalline and amorphous solids

(Développement et applications d'expériences RMN de corrélation, à travers les liaisons et l'espace, entre noyaux de spin-1/2 et quadripolaires dans les solides cristallins et amorphes)

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Abstract

My PhD thesis focuses on the development of the through-bond and through-space correlation solid state NMR experiments involving half-integer quadrupolar nuclei in order to characterize chemical structure of inorganic material at atomic level. This thesis consists of two part.

First, we introduce two-dimensional (2D) ⁷¹Ga-⁷⁷Se through-bond and through-space heteronuclear correlation (HETCOR) experiments. Such correlations are achieved using (i) the *J*-mediated Refocused Insensitive Nuclei Enhanced by Polarization Transfer (*J*-RINEPT) method with ⁷¹Ga excitation and ⁷⁷Se Carr-Purcell-Meiboon-Gill (CPMG) detection, as well as (ii) the *J*- or dipolar-mediated Heteronuclear Multiple-Quantum Correlation (*J*- or *D*-HMQC) schemes with ⁷¹Ga excitation and quadrupolar CPMG (QCPMG) detection. These methods are applied to the crystalline β -Ga₂Se₃ and the 0.2Ga₂Se₃-0.8GeSe₂ glass. We also report 2D ⁷¹Ga Satellite Transition Magic-Angle Spinning (STMAS) spectrum of β -Ga₂Se₃ using QCPMG detection at high magnetic field, high Magic-Angle Spinning frequency, and high rf-field.

Second, we introduce novel sequences using indirect detection to correlate quadrupolar nuclei and spin-1/2 isotopes, other than ¹H and ¹⁹F. These sequences use γ -encoded symmetry-based RN_n^{ν} schemes that reintroduce the space component |m| = 1 of the heteronuclear dipolar coupling. These schemes can be applied to the indirectly detected spin in Dipolar-mediated Heteronuclear Multiple-Quantum Correlation (*D*-HMQC) sequence or to the detected isotope in a novel sequence, named Dipolar-mediated Heteronuclear Universal-Quantum Correlation (*D*-HUQC). The performance of the sequences have been compared to conventional *D*-HMQC with R³ and SFAM recoupling via SIMPSON simulations and NMR experiments, including ¹³C-{¹⁵N} heteronuclear correlation on glycine and ³¹P-²⁷Al ones on VPI-5 and Na7(AlP₂O₇)₄PO₄.

Chapter 1: General introduction

This thesis focuses on the heteronuclear correlation NMR experiments involving half-integer quadrupolar nuclei. Hence, chapter 1 summarizes the important tool, concept and the state of the art in this field. The section 1.1 introduces the basic principles of solid-state NMR experiments. The section 1.2 describes the property of quadrupolar nuclei. The section 1.3 and 1.4 summarizes sensitivity enhancement and high resolution methodology for quadrupolar nuclei. The section 1.5 describes the heteronuclear dipolar recoupling sequence applied to single channel in HETCOR sequence. The section 1.6 is the review of 2D HETCOR experiments between spin-1/2 and half-integer quadrupolar nuclei.

1.1. Theoretical basis

A brief description of the theoretical basis of solid-state NMR spectroscopy is provided here. More detailed description can be found in the references [1-5]. The dynamics of nuclear spins during NMR experiments is described by the Liouville-von Neuman equation:

$$\frac{d}{dt}\hat{\rho}(t) = -i[\hat{H}(t),\hat{\rho}(t)]$$
(1.1)

where $\hat{\rho}(t)$ and $\hat{H}(t)$ represent the density operator and the Hamiltonian, respectively. The formal solution of the time evolution of the density operator can be recast in Hilbert space as follow

$$\hat{\rho}(t) = \hat{U}(t)\hat{\rho}(0)\hat{U}^{\dagger}(t)$$
(1.2)

with

$$\widehat{U}(t) = \widehat{T}e^{-i\int_0^t \widehat{H}(t)dt}$$
(1.3)

where $\hat{U}(t)$ is called propagator, and \hat{T} is the Dyson time-ordering operator. Signal detection can be performed as

$$S(t) = \langle \hat{Q} \rangle(t) = Tr\{\hat{\rho}(t)\hat{Q}\}$$
(1.4)

The Hamiltonian consists of external and internal terms

$$\widehat{H}(t) = \widehat{H}_{ext} + \widehat{H}_{int}$$
(1.5)

where the first term represents external interactions, including Zeeman and radiofrequency (rf) interaction, while the second one contains internal parts of the nuclear spin Hamiltonian. In the laboratory (LAB) frame, the external Hamiltonian takes the form

$$\widehat{H}_{ext} = \widehat{H}_0 + \widehat{H}_1(t) = \omega_0 \widehat{I}_z + 2\omega_1 \cos(\omega_{\text{ref}}t + \phi)\widehat{I}_z$$
(1.6)

with $\omega_1 = -\gamma B_1$, ω_{ref} and ϕ denoting the rf nutation angular frequency, the angular carrier frequency and phase of the rf-field, respectively, and B_1 the rf field amplitude and γ the gyromagnetic ratio.

The internal components of the Hamiltonian may conveniently be expressed in an irreducible tensor representation

$$\widehat{H}_{int} = \sum_{\lambda} \widehat{H}_{\lambda} ; \qquad \widehat{H}_{\lambda} = C^{\lambda} \sum_{j=0}^{2} \sum_{m=-j}^{J} (-1)^{m} \left[A_{j,-m}^{\lambda} \right]^{L} \widehat{T}_{j,m}^{\lambda}$$
(1.7)

where $A_{j,m}^{\lambda}$ and $\hat{T}_{j,m}^{\lambda}$ represents spatial and spin dependencies, respectively, and C^{λ} is a fundamental interaction dependent constant. *j* describe the rank of the tensor, while the superscript *L* designate that the description applies in LAB frame.

The analytical procedure of NMR experiments is as follows:

(i) Transformation into an appropriate interaction frame,

(ii) The calculation of the effective Hamiltonian,

(iii) The calculation of the response of the initial density operator to the effective Hamiltonian We need to introduce the concept of the rotations, average Hamiltonian (AH) and interaction frame to carry out those analytical calculations.

1.1.1. Rotations

Rotation of spin operators in cyclic 3D subspace

Assume that $\hat{\rho}(0) = \hat{A}$, $H(t) = \omega(t)\hat{B}$, and the operator \hat{A} , \hat{B} , and \hat{C} is cyclic commutative $([[\hat{A}, \hat{B}] = i\hat{C}, [\hat{B}, \hat{C}] = i\hat{A}, [\hat{C}, \hat{A}] = i\hat{B})$, the time-evolution of the density operator is given by $\hat{\rho}(t) = e^{-i\phi\hat{B}}\hat{A}e^{i\omega\phi\hat{B}} = \cos(\phi)\hat{A} - \sin(\phi)i[\hat{B},\hat{A}] = \cos(\phi)\hat{A} - \sin(\phi)\hat{C}$ (1.8) where $\phi = \int_0^t \omega(t)dt$ (e.g., $\phi = \omega_1 t$ for constant amplitude rf irradiation). The important things is to calculate the commutator $[\hat{B}, \hat{A}]$. If the commutator can be calculated easily (for instance, typical sets of non-commuting operators are $\{\hat{I}_x, \hat{I}_y, \hat{I}_z\}$, $\{\hat{I}_x, 2\hat{I}_y\hat{S}_z, 2\hat{I}_z\hat{S}_z\}$, $\{2\hat{I}_x\hat{S}_z, \hat{I}_y, 2\hat{I}_z\hat{S}_z\}$), this representation is preferable.

Rotation of irreducible spherical tensor operators

In irreducible spherical tensor representation, operator T of rank-j transforms as

$$\left[\hat{T}_{j,m}^{\lambda}\right]^{F2} = \sum_{m'^{=-j}}^{J} \left[\hat{T}_{j,m'}^{\lambda}\right]^{F1} D_{m',m}^{(j)}(\Omega)$$
(1.9)

where $D^{(j)}$ is a rank-*j* Wigner rotation matrix and $\Omega = \{\alpha, \beta, \gamma\}$ is the Euler angles separating the two frames F1 and F2. We consider here positive angles referring to counter-clockwise rotations, with the Wigner rotation being: a rotation by α around the original *z*-axis, rotation by β around the new *y*-axis, and finally rotation by γ around resulting *z*-axis. The Wigner matrix may be conveniently expressed in terms of reduced Wigner matrix ($d^{(j)}$) elements

$$D_{m',m}^{(j)}(\Omega) = e^{-im'\alpha} d_{m',m}^{(j)}(\beta) e^{-im\gamma}$$
(1.10)

First and second rank reduced Wigner matrix elements are given in **Table.1.1**.

Table 1.1. Reduced Wigner matrix elements $d_{m',m}^{(j)}(\beta)$ for j = 1, 2

j	$m' \setminus m$	-2	-1	0	1	2
	-1		$\frac{1}{2}(1+c_{\beta})$	$\frac{1}{\sqrt{2}}s_{\beta}$	$\frac{1}{2}(1-c_{\beta})$	
1	0		$-\frac{1}{\sqrt{2}}s_{\beta}$	c_{eta}	$\frac{1}{\sqrt{2}}s_{\beta}$	
	1		$\frac{1}{2}(1-c_{\beta})$	$-\frac{1}{\sqrt{2}}s_{\beta}$	$\frac{1}{2}(1+c_{\beta})$	
	-2	$\frac{1}{4}(1+c_{\beta})^2$	$\frac{1}{2}(1+c_{\beta})s_{\beta}$	$\sqrt{3/8} s_{\beta}^2$	$\frac{1}{2}(1-c_{\beta})s_{\beta}$	$\frac{1}{4}(1-c_{\beta})^2$
	-1	$-\frac{1}{2}(1+c_{\beta})s_{\beta}$	$c_{\beta}^2 - \frac{1}{2}(1 - c_{\beta})$	$\sqrt{3/8} s_{2\beta}$	$\frac{1}{2}(1+c_{\beta})-c_{\beta}^2$	$\frac{1}{2}(1-c_{\beta})s_{\beta}$
2	0	$\sqrt{3/8} s_{\beta}^2$	$-\sqrt{3/8} s_{2\beta}$	$\frac{1}{2} (3c_\beta^2 - 1)$	$\sqrt{3/8}s_{2\beta}$	$\sqrt{3/8} s_{\beta}^2$
	1	$-\frac{1}{2}(1-c_{\beta})s_{\beta}$	$\frac{1}{2}(1+c_{\beta})-c_{\beta}^2$	$-\sqrt{3/8} s_{2\beta}$	$c_{\beta}^2 - \frac{1}{2}(1 - c_{\beta})$	$\frac{1}{2}(1+c_{\beta})s_{\beta}$
	2	$\frac{1}{4}(1-c_{\beta})^2$	$-\frac{1}{2}(1-c_{\beta})s_{\beta}$	$\sqrt{3/8} s_{\beta}^2$	$-\frac{1}{2}(1+c_{\beta})s_{\beta}$	$\frac{1}{4}(1+c_{\beta})^2$

* s_{β} and c_{β} stand for $\sin \beta$ and $\cos \beta$

1.1.2. Effective Hamiltonian

In NMR theory, most Hamiltonian is time dependent. It is effective to obtain time independent Hamiltonian by approximation methods in order to calculate density operator. Typical approximative expression of the Hamiltonian series is as follow.

$$\widehat{H}_{eff}(t) = \overline{\widehat{H}}^{(1)} + \overline{\widehat{H}}^{(2)} + \dots$$
 (1.11)

There are some approximation procedure to drive this effective Hamiltonian. Most popular approximation theory is average Hamiltonian theory (AHT) [3,4] and Floquet theory.[6] AHT treatment is sufficient in this thesis. Advantage of Floquet theory is in the situation of asynchronous condition. In AHT, lowest order terms are defined as

$$\overline{\widehat{H}}^{(1)} = \frac{1}{\tau_c} \int_0^{\tau_c} \widehat{H}(t') dt'$$
(1.12)

$$\overline{\widehat{H}}^{(2)} = \frac{1}{i\tau_c} \int_0^{\tau_c} dt^{"} \int_0^{t^{"}} \left[\widehat{H}(t^{"}), \widehat{H}(t') \right] dt'$$
(1.13)

where τ_c denoting the period over which the averaging is performed. This simple expansion and later variants have proven extremely useful for simplifying the description of NMR experiments, for example, using a first-order approximation of the Hamiltonian in an interaction frame parameterizing out the dependency on rf-fields.

1.1.3. Interaction frame

In the analysis of NMR experiments, it is useful to transform to interaction frame when considering only the effect of the interesting internal parts of the Hamiltonian, which truly affects the spin dynamics. Frequently, Zeeman interaction itself complicates the contribution of internal Hamiltonian to the evolution of the density operator. The transformation to the frame of Zeeman interaction permits to simplify the calculation of the evolution of the density operator. A typical Hamiltonian in NMR consists of large terms, such as Zeeman interaction and small ones, such as chemical shift, dipolar coupling and quadrupolar coupling etc. as follow.

$$\widehat{H}(t) = \widehat{H}_{big}(t) + \widehat{H}_{small}(t)$$
(1.14)

Here, if we only want to discuss the effect of \hat{H}_{small} on the spin system, we decompose the propagator into $\hat{U}(t) = \hat{U}_{big}(t)\tilde{U}(t)$ and then by manipulating the density operator and Hamiltonian with \hat{U}_{big} as follows.

$$\tilde{\hat{\rho}}(t) = \hat{U}^{\dagger}_{big} \hat{\rho}(t) \hat{U}_{big}$$
(1.15)

$$\widetilde{H}(t) = \widehat{U}_{big}^{\dagger} \widehat{H}(t) \widehat{U}_{big} - i \widehat{U}_{big}^{\dagger} \frac{d}{dt} \widehat{U}_{big}(t) = \widetilde{H}_{small}(t)$$
(1.16)

 H_{big} can be removed and converted to interaction frame. Eq.(1.15) and (1.16) fulfill the Liouville-von Neuman equation $\frac{d}{dt}\tilde{\hat{\rho}}(t) = -i[\tilde{\hat{H}}(t),\tilde{\hat{\rho}}(t)]$. In the thesis, the interaction frame symbol "~" is abbreviated from below.

Truncated Hamiltonian in high magnetic field can be derived from combination of AHT and Zeeman interaction frame:

$$\overline{\hat{H}_{\lambda}}^{(1)} = C^{\lambda} \left\{ \left[A_{0,0}^{\lambda} \right]^{L} \widehat{T}_{0,0}^{\lambda} + \left[A_{2,0}^{\lambda} \right]^{L} \widehat{T}_{2,0}^{\lambda} \right\}$$
(1.17)

Thus, all components with $m \neq 0$ vanish in a first-order approximation and only the terms which commute with \hat{l}_z are remained. Truncated Hamiltonians of all internal interaction are given in **Table.1.2** and **1.3**.

λ	C ^λ	$\left[A_{0,0}^{\lambda}\right]^{L}$	$\widehat{T}^{\lambda}_{0,0}$	$\widehat{H}^{iso}_{\lambda}$	$\left[A_{2,0}^{\lambda}\right]^{L}$	$\left[\widehat{T}_{2,0}^{\lambda}\right]^{L}$	$\widehat{H}^{aniso}_{\lambda}$
CS	$-\gamma_I$	$-\sqrt{3}\delta_{iso}$	$-\frac{1}{\sqrt{3}}B_0\hat{I}_z$	$\delta_{iso}\omega_0 \hat{I}_z$	$\left[A_{2,0}^{CS}\right]^L$	$-\sqrt{\frac{2}{3}}B_0\hat{I}_z$	$\sqrt{\frac{2}{3}}\omega_{CSA}\hat{I}_{Z}$
D _{II}	1				$\left[A_{2,0}^{D,II}\right]^L$	$\frac{1}{\sqrt{6}} \left(3\hat{I}_z^j \hat{I}_z^k - \hat{I}^j \\ \cdot \hat{I}^k \right)$	$ \omega_{D,II} \left(3\hat{l}_z^j \hat{l}_z^k - \hat{l}^j \\ \cdot \hat{l}^k \right) $
D _{IS}	1				$\left[A_{2,0}^{D,IS}\right]^L$	$\sqrt{\frac{2}{3}} \hat{I}_z \hat{S}_z$	$\omega_{D,IS} 2\hat{I}_z \hat{S}_z$
J_{II}	1	$-2\pi\sqrt{3}J_{II}^{iso}$	$-rac{1}{\sqrt{3}}\hat{l}^j\cdot\hat{l}^k$	$2\pi J_{II}^{iso}\hat{I}^j\cdot\hat{I}^k$	$\left[A_{2,0}^{J,II}\right]^L$	$\frac{1}{\sqrt{6}} \left(3\hat{l}_z^j \hat{l}_z^k - \hat{l}^j \\ \cdot \hat{l}^k \right)$	
J_{IS}	1	$-2\pi\sqrt{3}J_{IS}^{iso}$	$-\frac{1}{\sqrt{3}}\hat{I}\cdot\hat{S}$	$2\pi J_{IS}^{iso}\hat{I}\cdot\hat{S}$	$\left[A_{2,0}^{J,IS}\right]^L$	$\sqrt{\frac{2}{3}} \hat{I}_z \hat{S}_z$	$\omega_{J,IS}^{aniso} \hat{I}_z \hat{S}_z$
$\begin{array}{c} Q \\ (1^{st}) \end{array}$	$\frac{2\pi C_Q}{2I(2I-1)}$				$\left[A_{2,0}^Q\right]^L$	$\frac{1}{\sqrt{6}} (3\hat{I}_z^2 - I(I + 1))$	$\frac{\omega_Q}{3\sqrt{6}} [A_{2,0}^Q]^L (3\tilde{l}_z^2 - I(I+1))$

 Table.1.2. Construction of Truncated Hamiltonian [5]

Table.1.3. Second rank spatial tensor in the principal axis system [5]

λ	$\left[A_{2,0}^{\lambda}\right]^{P}$	$\left[A_{2,\pm1}^{\lambda} ight]^P$	$\left[A_{2,\pm2}^{\lambda} ight]^{P}$
CS	$\sqrt{\frac{3}{2}}\delta_{aniso}$	0	$-rac{1}{2}\eta\delta_{aniso}$
D_{II}	$\sqrt{6} b_{II}$	0	0
D_{IS}	$\sqrt{6} b_{IS}$	0	0
J_{II}	$2\pi\sqrt{\frac{3}{2}}J_{II}^{aniso}$	0	$-rac{1}{2}\etaJ_{II}^{aniso}$
J_{IS}	$2\pi\sqrt{\frac{3}{2}}J_{IS}^{aniso}$	0	$-rac{1}{2}\etaJ_{IS}^{aniso}$
$Q (1^{st} order)$	$\sqrt{\frac{3}{2}}$	0	$-\frac{1}{2}\eta_Q$

* Second rank spatial tensor in LAB frame, $[A_{2,0}^{\lambda}]^{L}$ is defined as $[A_{2,0}^{\lambda}]^{L} = \sum_{m=-2}^{2} [A_{2,m}^{\lambda}]^{P} D_{m,0}^{(2)}(\Omega_{PL})$ in the case of static condition . $[A_{2,m}^{\lambda}]^{P}$ with $m = 0, \pm 1, \pm 2$ is necessary in order to obtain $[A_{2,0}^{\lambda}]^{L}$. The anisotropies of the spatial tensors (e.g., δ_{aniso} and J_{II}^{aniso}) are defined as $A_{aniso} = [A_{zz}]^{P} - A_{iso}$ with $A_{iso} = 1/3 \left([A_{xx}]^{P} + [A_{yy}]^{P} + [A_{zz}]^{P} \right)$. The asymmetry parameter is defined by $\eta = \left([A_{yy}^{\lambda}]^{P} - [A_{xx}^{\lambda}]^{P} \right) / \left([A_{zz}^{\lambda}]^{P} - A_{iso} \right)$. The dipolar coupling constants are defined by $b_{II} = -\left(\frac{\gamma_{I}^{2}}{r^{3}}\right) \frac{\mu_{0}\hbar}{4\pi}$ and $b_{IS} = -\left(\frac{\gamma_{IYS}}{r^{3}}\right) \frac{\mu_{0}\hbar}{4\pi}$ in rads⁻¹ where $\mu_{0} = 4\pi \cdot 10^{7} \text{ NC}^{-2}\text{s}^{2}$ is the permeability of a vacuum, γ is gyromagnetic ratio, r is the internuclear distance. $C_{Q} = (e^{2}qQ)/h$ (see section. 1.2 in detail) with $h = 6.62608 \cdot 10^{-34}$ Js is Planck's constant. \hbar is Planck's constant divided by 2π .

1.1.4. Magic angle spinning

The sensitivity and resolution of NMR spectra of disordered solids may be improved significantly by rapidly rotating the sample about an axis at the "magic angle", $\beta_{RL} = \tan^{-1}\sqrt{2} \approx 54.74$, with respect to the static magnetic field (**Fig.1.1**). This technique is called magic-angle spinning (MAS). The spatial rotation of the sample causes the orientation-dependent anisotropic spin



interactions to become time-dependent and to be averaged out in the case of rapid sample spinning.

Let us check how heteronuclear dipolar coupling is averaged out by MAS. The coefficient (including spatial part) of dipolar coupling is given by

$$\omega_{D,IS}(t) = \frac{1}{\sqrt{6}} C^{\lambda} \left[A_{2,0}^{D_{IS}} \right]^{L}$$
(1.18)

In the static case of the powder sample, assuming Euler angle $\Omega_{PL} = \{\alpha_{PL}, \beta_{PL}, \gamma_{PL}\}$ between principal axis system (PAS) frame and LAB frame,

$$\omega_{D,IS} = \frac{1}{\sqrt{6}} C^{\lambda} \left[A_{2,0}^{D_{IS}} \right]^{P} d_{0,0}^{(2)}(\beta_{PL}) = \frac{1}{2} b_{IS} (3\cos^{2}(\beta_{PL}) - 1)$$
(1.19)

where the constant and the spatial tensor in PAS frame is shown in **Table.1.2** and **1.3**. In static condition of the powder sample, $\omega_{D,IS}$ only depend on β_{PL} angle. $b_{IS} = -\left(\frac{\gamma_I\gamma_S}{r^3}\right)\frac{\mu_0}{4\pi}$ is the dipolar coupling constant in rads⁻¹.

In the spinning case, LAB frame is associated with PAS frame via rotor-fixed (ROTOR) frame. Euler angle is defined as $\Omega_{PR} = \{\alpha_{PR}, \beta_{PR}, \gamma_{PR}\}, \Omega_{PL} = \{\omega_R, \beta_{RL}, \gamma_{RL}\}, \omega_{D,IS}(t)$ under MAS is

$$\omega_{D,IS}(t) = \sum_{m=-2}^{2} \omega_{D,IS}^{(m)} e^{im\omega_R t}$$
(1.20)

with

$$\omega_{D,IS}^{(m)} = b_{IS} e^{im\gamma_{PR}} d_{0,-m}^{(2)}(\beta_{PR}) d_{-m,0}^{(2)}(\beta_{RL})$$
(1.21)

In MAS case, $\omega_{D,IS}(t)$ depends on not only β_{PR} angle but also γ_{PR} angle unlike static case. Since γ_{RL} angle is related to the rotation around MAS axis, γ_{RL} angle is especially important in rotating solids. In MAS case, $\omega_{D,IS}^{(m)}$ for $m = 0, \pm 1, \pm 2$ are

$$\omega_{D,IS}^{(0)} = \frac{1}{4} b_{IS} (3\cos^2(\beta_{PR}) - 1) (3\cos^2(\beta_{RL}) - 1) = 0$$
(1.22)

$$\omega_{D,IS}^{(\pm 1)} = -\frac{1}{2\sqrt{2}} b_{IS} \sin(2\beta_{PR}) e^{\pm i\gamma_{PR}}$$
(1.23)

$$\omega_{D,IS}^{(\pm 2)} = \frac{1}{4} b_{IS} \sin^2(\beta_{PR}) e^{\pm i2\gamma_{PR}}$$
(1.24)

Assuming sampling at rotor echo and magic angle $\beta_{RL} = \tan^{-1} \sqrt{2}$

$$\phi = \sum_{m=-2}^{2} \int_{0}^{n\tau_{R}} \omega_{D,IS}^{(m)} e^{im\omega_{R}t} dt = \omega_{D,IS}^{(0)} = 0$$
(1.25)

Dipolar coupling is averaged out. As mentioned later, rotor synchronized t_1 acquisition in 2D experiments is necessary for averaging dipolar coupling, CSA and quadrupolar interaction (especially, first-order terms).

In infinite spinning case, by AHT treatment

$$\overline{\hat{H}_{D,IS}}^{(1)} = \frac{\omega_R}{2\pi} \int_0^{\frac{2\pi}{\omega_R}} \widehat{H}_{D,IS} \, dt = \omega_{D,IS}^{(0)} 2\hat{I}_z \hat{S}_z = 0 \tag{1.26}$$

implying that the dipolar coupling does not affect the spin evolution. The above derivation is only valid for commuting dipolar interactions. However, in the case of non-commuting homonuclear dipolar interactions (homogeneous case), it is difficult to remove the dipolar coupling only by MAS. High resolution spectrum can be obtained by combination of MAS and decoupling sequence (which manipulate spin part in Hamiltonian).

1.1.5. Cross polarization

Cross polarization (CP) enhances the NMR signal of low- γ nuclei coupled through dipolar interaction with high- γ nuclei. The pulse sequence is shown in **Fig.1.2**. The cross polarization consists in



Fig.1.2 schematic diagram of the basic $I \rightarrow S$ cross polarization experiment.

(i) Generating transverse magnetization on the I channel by $\pi/2$ pulse and applying a rf-field $\omega_{1,I}$, sufficient to lock it.

- (ii) Satisfying the Hartmann-Hahn (HH) matching condition with a suitable rf-field $\omega_{1,S}$.
- (iii) Adjusting the contact time for which two rf-fields are applied. The optimal contact time depends on b_{IS} .

Under MAS, it is complicated task to understand HH matching condition at quantum mechanics level.^[7] Heteronuclear dipolar recoupled AH under MAS is

0Q condition: $\omega_{1,I} - \omega_{1,S} = n\omega_R$

$$\overline{\hat{H}_{D,IS}}^{(1)} = \frac{1}{4} \omega_{D,IS}^{|n|} \{ \cos(\gamma_{PR}) (\hat{I}_{+} \hat{S}_{-} + \hat{I}_{-} \hat{S}_{+}) \pm \sin(\gamma_{PR}) (\hat{I}_{+} \hat{S}_{-} - \hat{I}_{-} \hat{S}_{+}) \}$$
(1.27)

2Q condition: $\omega_{1,I} + \omega_{1,S} = n\omega_R$

$$\overline{\hat{H}_{D,IS}}^{(1)} = \frac{1}{4} \omega_{D,IS}^{|n|} \{ \cos(|n|\gamma_{PR}) (\hat{I}_{+} \hat{S}_{+} + \hat{I}_{-} \hat{S}_{-}) \pm \sin(|n|\gamma_{PR}) (\hat{I}_{+} \hat{S}_{+} - \hat{I}_{-} \hat{S}_{-}) \}$$
(1.28)

with $n = \pm 1, \pm 2$ and

$$\omega_{D,IS}^{|n|=1} = -\frac{1}{2\sqrt{2}} b_{IS} \sin(2\beta_{PR})$$
(1.29)

$$\omega_{D,IS}^{|n|=2} = \frac{1}{4} b_{IS} \sin^2(\beta_{PR})$$
(1.30)

 $\omega_{1,I} - \omega_{1,S} = n\omega_R$ condition is called zero quantum (0Q) matching because of flip-flop transition. $\omega_{1,I} + \omega_{1,S} = n\omega_R$ condition is called double quantum (2Q) matching because of flip-flip (or flop-flop) transition.

Hence, HH matching condition under MAS is summarized as follow.

$$\omega_{1,S} = \varepsilon \omega_{1,I} + n \omega_R \quad (\varepsilon = \pm 1; n = \pm 1, \pm 2) \tag{1.31}$$

From this results, in case of moderate spinning speed region ($v_R = 10 \sim 20$ kHz) or large rf-amplitude, 0Q condition ($\varepsilon = +1$) can be chosen. On the other hand, in case of very high spinning speed or low rf-amplitude, 2Q condition ($\varepsilon = -1$) can be better than 0Q condition.

1.2. NMR of quadrupolar nuclei

1.2.1. Quadrupolar interaction

Around 75% of NMR-active nuclei are quadrupolar (i.e. have a spin quantum number I > 1/2).[8-12] A quadrupolar nucleus possesses an electric quadrupolar moment, eQ, which interacts with the electric field gradient (EFG) created by the charges (electrons, other nuclei). The EFG is defined by three components, V_{xx} , V_{yy} and V_{zz} , where $V_{zz} = eq$, in its principal axis system. This interaction between eQ and the EFG is generally described in terms of the quadrupolar coupling constant, $C_Q = e^2 qQ/h$ and the asymmetry parameter, $\eta_Q = (V_{xx} - V_{yy})/V_{zz}$. The quadrupolar Hamiltonian in the LAB frame can be written as

$$\widehat{H}_{Q} = \frac{\omega_{Q}}{3} \sum_{m=-2}^{2} (-1)^{m} \left[A_{2,-m}^{Q} \right]^{L} \widehat{T}_{2,m}$$
(1.32)

with

$$\omega_Q = 2\pi \frac{3C_Q}{2I(2I-1)} \tag{1.33}$$

The quadrupolar Hamiltonian can then be approximated in the high field case using AHT and expressed with Clebsch-Gordan coefficients for second-order term. First- and second-order quadrupolar Hamiltonian under fast MAS speed are

$$\overline{\hat{H}_Q}^I = \frac{\omega_Q}{3\sqrt{6}} \left[A_{2,0}^Q \right]^R d_{0,0}^{(2)}(\beta_{RL}) \left(3\hat{I}_z^2 - I(I+1) \right)$$
(1.34)

$$\overline{\hat{H}_Q}^{II} = \frac{\omega_Q^2}{9\omega_0} \left(\left[B_{0,0}^Q \right]^R \widehat{K}_0 + \left[B_{2,0}^Q \right]^R d_{0,0}^{(2)}(\beta_{RL}) \widehat{K}_2 + \left[B_{4,0}^Q \right]^R d_{0,0}^{(2)}(\beta_{RL}) \widehat{K}_4 \right)$$
(1.35)

Where

$$\widehat{K}_{0} = \frac{1}{\sqrt{5}} \widehat{I}_{z} \left(3\widehat{I}_{z}^{2} - I(I+1) \right), \qquad \widehat{K}_{2} = -\frac{1}{2\sqrt{14}} \widehat{I}_{z} \left(12\widehat{I}_{z}^{2} - 8I(I+1) + 3 \right),$$

$$\widehat{K}_{4} = -\frac{1}{2\sqrt{70}} \widehat{I}_{z} \left(34\widehat{I}_{z}^{2} - 18I(I+1) + 5 \right)$$
(1.36)

$$\left[B_{l,0}^{Q}\right]^{R} = \sum_{n=-m}^{m} \left[B_{l,n}^{Q}\right]^{p} D_{n,0}^{(2)}(\Omega_{PR})$$
(1.37)

$$\begin{bmatrix} B_{0,0}^{Q} \end{bmatrix}^{p} = \frac{3+\eta_{Q}^{2}}{2\sqrt{5}}, \quad \begin{bmatrix} B_{2,0}^{Q} \end{bmatrix}^{p} = \frac{-3+\eta_{Q}^{2}}{\sqrt{14}}, \quad \begin{bmatrix} B_{2,\pm 2}^{Q} \end{bmatrix}^{p} = \sqrt{\frac{3}{7}}\eta_{Q},$$

$$\begin{bmatrix} B_{4,0}^{Q} \end{bmatrix}^{p} = \frac{18+\eta_{Q}^{2}}{2\sqrt{70}}, \quad \begin{bmatrix} B_{4,\pm 2}^{Q} \end{bmatrix}^{p} = \frac{3\eta_{Q}}{2\sqrt{7}}, \quad \begin{bmatrix} B_{4,\pm 4}^{Q} \end{bmatrix}^{p} = \frac{\eta_{Q}^{2}}{4},$$

$$(1.38)$$

Transition frequency between eigenstates $|s\rangle$ and $|r\rangle$ can be derived from

$$\omega_{p,q} = \omega_{s \to r} = \left\langle r \left| \overline{\hat{H}_Q} \right| r \right\rangle - \left\langle s \left| \overline{\hat{H}_Q} \right| s \right\rangle$$
(1.39)

It is convenient to express transition frequency in terms of p = r - s (coherence order) and $q = r^2 - s^2$ (satellite order).[2]

For the first-order quadrupolar interaction, transition frequency is given by

$$\omega_{p,q}^{I} = q \frac{\omega_{Q}}{\sqrt{6}} \left[A_{2,0}^{Q} \right]^{R} d_{0,0}^{(2)}(\beta_{RL})$$
(1.40)

For half-integer spins, 1Q Central Transition (CT: $-1/2 \leftrightarrow 1/2$) and symmetric Multiple Quantum (MQ: $-p/2 \leftrightarrow p/2$) coherence (q = 0) are not affected by the first-order term. On the other hand, the Satellite transitions (STs: $m-1 \leftrightarrow m$) ($q \neq 0$) are not strongly affected by the first-order quadrupolar interaction.

For the second-order quadrupolar interaction, transition frequency is given by

$$\omega_{p,q}^{II} = \omega_{p,q}^{(0)} + \omega_{p,q}^{(2)} + \omega_{p,q}^{(4)}$$
(1.41)

where

$$\omega_{p,q}^{(0)} = -p \frac{\left(1 + \eta_Q^2/3\right)}{30} \frac{\left(\omega_Q\right)^2}{\omega_0} \left(I(I+1) - \frac{3}{4}\left(p^2 + 3\frac{q^2}{p^2}\right)\right)$$
(1.42)

$$\omega_{p,q}^{(2)} = C_2(\Omega_{PR}) \left(3\left(p^2 + \frac{3q^2}{p^2}\right) - p(8I(I+1) - 3) \right) d_{0,0}^{(2)}(\beta_{RL})$$
(1.43)

$$\omega_{p,q}^{(4)} = C_4(\Omega_{PR}) \left(\frac{17}{2} \left(p^2 + \frac{3q^2}{p^2} \right) - p(18I(I+1)-5) \right) d_{0,0}^{(4)}(\beta_{RL})$$
(1.44)

with

$$C_2(\Omega_{PR}) = -\frac{1}{9} \frac{\omega_Q^2}{\omega_0} \frac{\left[B_{2,0}^Q\right]^R}{2\sqrt{14}}$$
(1.45)

$$C_4(\Omega_{PR}) = -\frac{1}{9} \frac{\omega_Q^2}{\omega_0} \frac{\left[B_{4,0}^Q\right]^R}{2\sqrt{70}}$$
(1.46)

$$d_{0,0}^{(4)}(\beta_{RL}) = \frac{1}{8} [35\cos^4(\beta_{RL}) - 30\cos^2(\beta_{RL}) + 3]$$
(1.47)

 $\omega_{p,q}^{(0)}$ term is an isotropic quadrupolar-induced frequency which do not broaden the spectrum. $\omega_{p,q}^{(2)}$ and $\omega_{p,q}^{(4)}$ terms are anisotropic and broaden the CT spectrum of powder samples. Especially, $\omega_{p,q}^{(4)}$ term cannot be removed completely by MAS owing to $d_{0,0}^{(4)}(\beta_{RL})$. Secondorder quadrupolar broadening is proportional to $1/\omega_0$. Hence, the use of high magnetic fields improves the spectral resolution. The energy level diagram of I = 3/2 is shown in **Fig.1.3**.



Fig.1.3 schematic energy level diagram of a nucleus with I = 3/2.

1.2.2. CT selective pulse

Another difficulty for quadrupolar nuclei is the manipulation of the magnetization using a rf-field since such field ranging from tens to hundreds kilohertz is typically weaker than the strength of the first-order quadrupolar interaction. In the limit case, where the rf-field is much smaller than the quadrupolar interaction, the CT is selectively excited and the general formula for rf nutation frequency is

$$\omega_{nut} = \left(I + \frac{1}{2}\right)\omega_1 \tag{1.48}$$

An additional result of selective excitation is that it reduces the intensity of the resulting central transition signal. If the signal following a non-selective pulse of length can be described by

$$S(\tau_p) = S_0 \sin(\omega_1 \tau_p) \tag{1.49}$$

then the signal following a CT selective pulse is

$$S(\tau_p) = \frac{S_0}{I + 1/2} \sin\left((I + 1/2)\omega_1 \tau_p\right)$$
(1.50)

The $\pi/2$ and π CT-selective pulses are employed in numerous pulse sequences described below. Therefore, setting up a spin echo experiment using $\pi/2$ and π CT-selective on a model sample or better on target sample is always useful.

1.2.3. Non selective pulse

The excitation pulses using larger rf-field yield more intense NMR signals than CT-selective ones. In general, the maximal possible rf-field remains smaller than or comparable to the strength of the quadrupolar interaction. In this intermediate regime, the spin dynamics of quadrupolar nuclei becomes complex and highly dependent on the strength of the quadrupolar interaction. These non-selective rf pulses are notably employed for the acquisition of 1D NMR spectra. Furthermore, for quantitative NMR spectra, the quadrupolar nuclei are excited by a single non-selective pulse producing small flip angle of the CT magnetization. Non-selective pulses are also employed to excite the STs as well as MQ transitions.

1.3. Sensitivity enhancement methodology for half-quadrupolar nuclei

1.3.1. Population transfer from satellite transitions

The intensity enhancement of the CT of half-integer spin quadrupolar nuclei can be achieved via a change of the populations of the various energy levels.[13] Two limit cases are by saturation or inversion of the ST populations. Simultaneous saturation of the STs equalizes the populations of all the lower and upper energy levels and enhances CT signal intensity by a

factor of (I + 1/2). On the other hand, population inversion enhance CT signal intensity by a factor of 2*I*.

RAPT. In 1999, Madhu et al. used a phase-alternating pulse train (Fast Amplitude Modulation: FAM) to enhance MQ to 1Q coherence transfer in MQMAS experiment.[14] Yao et al. employed the same pulse train in 1D experiments to obtain enhancement and proposed Rotor Assisted Population Transfer (RAPT).[15] The RAPT pulse train with alternating phases creates sidebands generated from the carrier frequency, v_{ref} , at frequency intervals of

$$\nu_{\phi} - \nu_{\rm ref} = (\Delta \phi/360^\circ) \tau_{\rm p} \tag{1.51}$$

where ϕ is the phase increment between the pulses in degree and τ_p , which is equal to the sum of d_{RAPT} and P_{RAPT} , is the RAPT time in seconds shown in **Fig.1.4**.





Two parameters, the RAPT modulation frequency, $v_m = [2(d_{RAPT} + P_{RAPT})]^{-1}$, and the rfamplitude are expected to have a greater influence on the signal enhancement. Yao et al. observed maximum enhancement (*I*+1/2) around $v_m = C_Q/4$ for *I* = 3/2 nucleus. [15]

DFS. Kentgens et al. proposed Double Frequency Sweep (DFS).[16] These pulses simultaneously sweep both the high- and low- frequency STs in a symmetric manner with the use of an amplitude-modulated pulse. A linear DFS is obtained if the rf-amplitude is varied smoothly from a start frequency (ω_s) to a final frequency (ω_f) in a cosinusoidal fashion as follows

$$\omega_1(t) = \omega_1^{max} \cos\left(\omega_s t - (\omega_s - \omega_f) \frac{t^2}{2\tau_p}\right)$$
(1.52)

where ω_1^{max} is the maximum rf-amplitude and τ_p is the length of the DFS pulse. This generates rf carrier sidebands which are swept over the STs. The carrier sidebands are swept smoothly over the STs which yields a more complete ST population inversion. When a powdered sample is spun rapidly at the magic angle, different crystallites will experience largely different sweep rates, as well as a different number of sweeps. Different crystallites will experience different enhancements ranging from 1 to 2*I*. The effect of the DFS, when applied to spinning samples, is generally to saturate the STs. **HS.** Wasylishen and co-workers used hyperbolic secant (HS) inversion pulse to induce perfect inversion of spin population.[17] The pulse is smoothly turned on and off as the amplitude is modulated by a hyperbolic secant function, whereas the phase is modulated to induce a sweep with a hyperbolic tangent profile

$$\omega_{1}(t) = \omega_{1}^{max} \operatorname{sech}\left(\beta\left(\frac{2t}{\tau_{p}}-1\right)\right)$$
(1.53)

$$\phi(t) = \left(\frac{\lambda}{\beta}\right) \left(\frac{\tau_p}{2}\right) ln \left[\operatorname{sech}\left(\beta \left(\frac{2t}{\tau_p} - 1\right)\right)\right] + \Delta\omega_{\operatorname{ref}} t \tag{1.54}$$

where the parameters λ and β are associated with the maximum frequency and truncation of the sech function, respectively. $\Delta \omega_{ref}$ is a rf-offset. The amplitude may be further modulated with a cosine function so that the HS pulse affects both the high- and low-frequency STs.

Under MAS conditions, it was possible to approach the theoretical maximum enhancements expected for complete inversion of the STs in spinning samples. A key aspect of their breakthrough was that the largest enhancements were obtained if the HS sweep width equaled the spinning frequency such that only a single ST sideband was targeted. Generally, HS outperform RAPT and DFS under MAS condition.

1.3.2. (Q)CPMG acquisition

The CPMG (Carr-Purcell-Meiboom-Gill) experiment is a very common technique in NMR spectroscopy.[18] The CPMG experiment consists of a π pulses as in **Fig.1.4**, refocusing the signal during acquisition. The Fourier transformed spectrum is composed of a series of regularly spaced sharp peaks (spikelet). CPMG is most successful on samples with long T_2 ' relaxation times, as the signal can be refocused multiple times.

The CPMG experiment has been used to obtain signal enhancement for I = 1/2 nuclei as well as the measurement T_2 ' before being applied to quadrupolar nuclei.[19] CPMG experiments on quadrupolar nuclei are termed QCPMG, although the method is not fundamentally different from the conventional CPMG except for CT selective pulse.

The condition. Under MAS, the CPMG echo period (t_e) is chosen to be rotor synchronized as illustrated in **Fig.1.4**.

$$t_e = 2m\tau_R = t_\pi + t_a + 2de$$
 (1.55)

with t_a is the one echo acquisition period, and *de* the dead time during which the Free-Induction Decay (FID) is not recorded. A factor of 2 in $t_e = 2m\tau_R$ is originated from the rotor synchronization of the period between $\pi/2$ pulse and π pulse. *NE* is a number of echoes which is set to acquire as many echoes as possible.



Fig.1.4 Schematic diagram of the CPMG pulse sequence

The resolution of CPMG spectrum is determined by the spikelet spacing, $1/(t_e)$, and the width of the spikelet is related to T_2 '. There is also the option to add all of the echoes together to form a full-echo, and to recover the original lineshape instead of spikelets.

0Q coherence. If the refocusing pulse is not a perfect π pulse, some signal will be passed through 0Q coherence. This is so-called stimulated echoes. Modulation of the spikelet manifold arises due to the difference in time at which Hahn and stimulated echoes form. Hence, the severity of the spectral distortion is correlated to an increase in the magnitude of the 0Q coherences as the flip angle deviates from 180°. This 0Q coherence can be completely filtered by phase cycle (16 step phase cycle or PIETA method) after every π pulse keeping only the ± 1 Q coherences.[19,20] However, if filtration of 0Q coherence is carried out, the first echo remains completely unperturbed, while a significant loss of intensity is observed for subsequent echoes. Thus, the first echo is a pure Hahn echo, while subsequent echoes are a combination of Hahn and stimulated echoes, i.e., echoes which form due to coherence transfer pathways that pass through 0Q order. Moreover, 0Q coherence can result in slower decay rates since it depends on the spin-lattice relaxation T_1 which is larger than T_2 ' in solids. The amount of observable signal is therefore maximized by the use of a minimal phase cycling scheme.

Modified CPMG. The CPMG can refocus the anisotropic interaction such as CSA, secondorder quadrupolar coupling and heteronuclear dipolar coupling. On the other hand, homonuclear dipolar coupling cannot be refocused by CPMG as Hahn echo and paramagnetic center affect T_2 ' to be short as known paramagnetic relaxation enhancement (PRE). Hence, T_2 ' will be shorter and the width of spikelets will be broadened in the presence of homonuclear dipolar couplings and paramagnetic substances. R. Siegel et al. proposed modified CPMG sequence in which π pulse is replaced into $\pi/2$ pulse except for first π pulse.[21] By this sequence, the property of homonuclear dipolar decoupling is more effective than regular CPMG and T_2 ' will be longer for non-dilute system without spectral distortion although second and third echo intensity of a modified CPMG is a less than that of regular CPMG. Consequently, Modified CPMG is 1.5 ~ 2 times efficient than regular CPMG in non-dilute system.[22] However, utilizing CPMG is basically preferable for dilute spin system and non-paramagnetic system. This CPMG with minimal phase cycling have been combined with CP, PRESTO and MQMAS so far and significant sensitivity enhancement have been observed.

1.4. High resolution methodology for half-integer quadrupolar nuclei

A major issue with half-integer quadrupolar nuclei (I > 1/2) is that even under MAS, the second-order quadrupolar broadening is not completely eliminated. As a consequence, overlapping of resonances with distinct isotropic chemical shifts, δ_{iso} , often occurs and a simple determination of the number of sites in a compound is rendered difficult. In order to overcome this problem, a few research groups have proposed in the late 80s, two methods where the sample is rotated at two different angles either simultaneously (DOuble Rotation, DOR) [23] or sequentially (Dynamic Angle Spinning, DAS).[24] The set of angles are chosen to cancel both first and second-order terms of the quadrupolar interaction. Even if the development of DOR and DAS methods has been very important in the beginning of the 90s, their use is nowadays limited to rare applications due to the obvious technical challenge that is associated to them. From 1995 on, two 2D pulse sequences, the Multiple-Quantum MAS (MQMAS)[25] and the Satellite Transition MAS (STMAS)[26] have been proposed to cancel out the broadening due to the whole quadrupolar interaction.

1.4.1. MQMAS

MQMAS is designed to remove the second-order broadening of the CT transition in NMR spectra of half-integer spin quadrupolar nuclei (I > 1/2). From Eq.(1.40), the contribution from the 1st order quadrupolar perturbation for the symmetric transition vanishes. We then only consider the second order effect. In Eq.(1.41 – 1.47), The $d_{0,0}^{(2)}(\beta_{RL})$ terms vanishes owing to MAS and isotropic part can be ignored since it does not contribute to phase dispersion and only induce an isotropic quadrupolar induced shift. Therefore, only the rank-4 term in Eq.(1.44) remains. In conventional MQMAS sequence, first rf pulse excites symmetrical MQ coherence $(-p/2 \leftrightarrow p/2)$, which evolve during t_1 period, and then second rf pulse converts them to 1Q coherence which can be detected (**Fig.1.5**).



Fig.1.5. Schematic diagram of the original MQMAS experiment

The total evolution phase is given by

$$\Phi(t) = \omega_{p,0}^{(4)}(\beta_{RL})t_1 + \omega_{-1,0}^{(4)}(\beta_{RL})t_2$$
(1.56)

From this equation, the isotropic echo can be observed by satisfying following condition

$$t_{2} = -\frac{\omega_{p,0}^{(4)}(\beta_{RL})}{\omega_{-1,0}^{(4)}(\beta_{RL})}t_{1} = \frac{1}{9}\frac{p(-17p^{2} + 36I(I+1) - 10)}{4I(I+1) - 3} = kt_{1}$$
(1.57)

Thus, rank-4 terms are cancelled out. The values k for various spin I is shown in **Table.1.4**.

$I \setminus p$	3	5	7	9
3/2	-7/9			
5/2	19/12	-25/12		
7/2	101/45	11/9	-161/45	
9/2	91/36	95/36	7/18	-31/6

Table.1.4. The value k for various half-integer quadrupolar spin.

(...)

MQMAS spectra are presented after a shearing transformation to obtain pure absorption 2D spectrum [27]. However, the original MQMAS sequence does not give pure absorption 2D spectra. In order to overcome this problem, some modified MQMAS sequences have been proposed.

Z filter method.[28] The z-filter approach was thus added to the original sequence in order to symmetrize the echo and anti-echo coherence transfer pathways. This method can be used on samples with both long and very short T_2 '. It needs shearing.

Split- t_1 **method.**[29] The split- t_1 sequence divides the t_1 time between MQ and 1Q evolution periods in a proportion k, that avoids the post-acquisition shearing procedure. The disadvantage is that the shifted-echo type pulse sequences depend on the decay rate, $1/T_2$ ', of transverse losses, which is not refocused by a CT-selective π pulse, and the z-filter should thus be preferred when facing short T_2 ' relaxation values

There are several approaches for sensitivity improvement approach.

3Q to 1Q conversion. The main disadvantage of the MQMAS method lies in its lack of sensitivity that suffers from a very inefficient conversion rate from 3Q to 1Q (or 0Q for the z-filter sequence) coherences. Therefore, several studies have been carried out to increase this conversion by modifying conversion pulse with FAM, DFS or HS. [30]

MQMAS-QCPMG. Another sensitivity improvement approach is to combine MQMAS with QCPMG detection. F.H.Larsen et al. introduced QCPMG acquisition into MQMAS experiment.[31] This represents the amplitude-modulated split- t_1 preparation for 3Q-QCPMG-MAS sequence with z filter applied to spin I = 3/2.

1.4.2. STMAS

The main limitation of MQMAS is its low sensitivity, which is due to the low efficiency in excitation and conversion of MQ transitions. STMAS 2D experiment, which correlates the 1Q ST and CT coherences, was proposed in 2000 by Gan as an alternative to MQMAS to obtain a high-resolution spectrum for half-integer quadrupolar nucleus, since ST excitation and conversion show superior efficiencies. Like MQMAS, the STMAS pulse sequence is based on a quadrupolar echo but with pulse conditions and phase cycling optimized to excite STs. Likewise, we assume the spin system at magic angle and ignore isotropic part. First rf pulse excite non-symmetrical ($m-1 \leftrightarrow m$) ST coherence, which evolve during t_1 period, and then second rf pulse converts them to 1Q coherence which can be detected. The total evolution phase is given by

$$\Phi(t) = \omega_{-1,q}^{(4)}(\beta_{RL})t_1 + \omega_{-1,0}^{(4)}(\beta_{RL})t_2$$
(1.58)

From this equation, the isotropic echo can be observed by satisfying following condition

$$t_{2} = -\frac{\omega_{-1,q}^{(4)}(\beta_{RL})}{\omega_{-1,0}^{(4)}(\beta_{RL})}t_{1} = \frac{17}{3}\frac{q^{2}}{(4I(I+1)-3)} - 1 = k't_{1}$$
(1.59)

Thus, rank-4 terms are cancelled out. The values k' for various spin I is represented in **Table.1.5**.

$I \setminus m$	3/2	5/2	7/2	9/2
3/2	-8/9			
5/2	7/24	-11/6		
7/2	28/45	-23/45	-12/5	
9/2	55/72	1/18	-9/8	-25/9

Table.1.5. The value *k*' for various half-integer quadrupolar spin

Disadvantage of STMAS.

- (i) Since those STs are affected by the first-order quadrupolar interaction, the STMAS experiment is extremely sensitive to a precise setting of the magic angle. STs evolve during t_1 period and rotor-synchronization t_1 acquisition is mandatory to eliminate the first-order quadrupolar broadening of STs. The required precision is about 0.002–0.005°.
- (ii) Even when taking all necessary precautions, STMAS spectra always contain an unwanted autocorrelation signal stemming from the CT evolution during t_1 and t_2 periods, which cannot be cancelled out by phase cycling. In order to avoid this problem, some approaches have been proposed so far.

DQF methods.[32] the transfer between 1Q and 2Q coherences is performed with an additional soft CT-selective π pulse just before 1Q conversion pulse, called Double Quantum Filter (DQF), which also inverts the CT magnetization (1Q \leftrightarrow -1Q), and does not affect outer satellite 1Q coherences of spin 5/2, 7/2, and 9/2. Since ±2Q is selected by phase cycle, CT-CT correlations are removed.

Split- t_1 **method.**[33] An additional soft CT-selective π pulse is placed on after $t_1 = n/9\tau_R$ evolution. The magnetization spends $1/9^{\text{th}}$ of the evolution time on $\pm 1Q$ levels, and $8/9^{\text{th}}$ on $\pm 2Q$ levels. Likewise, since $\pm 2Q$ is selected by phase cycle, CT-CT correlations are removed. The post-acquisition shearing procedure is not needed for split- t_1 STMAS. Both DQF and split- t_1 have z filter duration after 1Q conversion pulse.

1.5. Heteronuclear dipolar recoupling

This thesis focuses on 2D HETCOR between spin-1/2 and half-integer quadrupolar nuclei. Under magic-angle spinning (MAS) for resolution purpose, these heteronuclear dipolar (D_{IS}) couplings between two isotopes *I* and *S* are averaged out and their exploitation requires the use of D_{IS} recoupling sequences. Here, we concentrate on recoupling schemes which can reintroduce dipolar interactions between spin-1/2 and quadrupolar nuclei. In that case, the D_{IS} recoupling must be achieved without the application of rf-field to the quadrupolar nucleus because of the intricate spin dynamics of quadrupolar nuclei in the presence of rf-field. An ideal D_{IS} recoupling method should have the following characteristics:

- (i) The spin interactions other than the desired D_{IS} coupling must be suppressed from the average Hamiltonian (AH) or must have no influence on the time evolution of the density matrix; (these undesired interactions comprise homonuclear dipolar (D_{II}) coupling, D_{IS} coupling, isotropic chemical shift, chemical shift anisotropy (CSA), quadrupole interaction, and interaction between nuclei and unpaired electrons in the case of paramagnetic compounds);
- (ii) The magnitude of the scaled recoupled D_{IS} coupling must be larger than the decay rate of the signal (due to effective T_2' or $T_{1\rho}$ under the recoupling if applied to the observed nucleus);
- (iii) The employed rf-field in the D_{IS} recoupling must be compatible with the probe specifications;
- (iv) The D_{IS} recoupling sequence must be robust to rf-inhomogeneities;
- (v) The D_{IS} recoupling sequence must be robust to MAS frequency instabilities;

(vi) When the goal is to measure internuclear distances, the sampling frequency of the recoupling sequence must be faster than the signal dephasing produced by the recoupled dipolar interaction.

However, there is no ideal D_{IS} recoupling method possessing the properties (i) to (vi) and choice of the method thus depends on its application.

 γ encoding in heteronuclear case. The property of D_{IS} recoupling methods depend on γ_{PR} Euler angle. The definition of γ encoding is that the norm of D_{IS} recoupled average Hamiltonian does not depend on γ_{PR} Euler angle.[34] This norm is equal to effective dipolar coupling ($\omega_{D,IS}$). The property regarding γ encoding is as follow.

- (i) Non- γ encoding recoupling sequence is 25 % less efficient than γ encoding recoupling;
- (ii) Dipolar oscillation of build-up curve of non- γ encoding is less pronounced, compared to γ encoding sequence;
- (iii) γ encoding recoupling is more robust to MAS fluctuation, since γ encoding does not depend on γ_{PR} angle around MAS axis;
- (iv) In case of D_{IS} recoupling, dipolar truncation effect $[\hat{H}_{(i)}, \hat{H}_{(j)}] \neq 0$ is linked to γ encoding. Non- γ encoded D_{IS} recoupled AH is formed by longitudinal-two-order-spin $(\hat{I}_z \hat{S}_z)$. On the other hand, γ encoded D_{IS} recoupled AH contains 1Q terms which lead to dipolar truncation.
- (v) Also, γ encoded D_{IS} recoupled AH does not commute with CSA recoupled AH. This lead to detrimental effect on the efficiency. On the other hand, non- γ encoded D_{IS} recoupling sequence is not affected by CSA since D_{IS} recouped AH commute with CSA recoupled AH.

For instance, as already described in Eq.(1.27-1.30), CP is γ -encoded recoupling and dipolar truncated although CP is not a single channel recoupling. In the following, frequently used single channel D_{IS} recoupling sequences are presented.

1.5.1. R³

Rotary-Resonance Recoupling (R³) [34, 35] consists in the rf irradiation of a single-spin system, the spin-1/2 here, with a rf-amplitude equal to a multiple (q = 1, 2) of the MAS frequency. The q = 1 condition recouples both D_{IS} coupling and D_{II} while the q = 2 recouples only D_{IS} coupling. Therefore, the latter condition must be used in the presence of a strong D_{II} coupling.

Under MAS, assuming rf irradiation of single channel $\omega_1 \hat{S}_x$ and S spin subject to CSA and D_{IS} coupling with I spin, first order AH is

$$\overline{\widehat{H}}^{(1)} = \frac{1}{2} \left(\omega_{CSA,S}^{(-q)} + \omega_{CSA,S}^{(q)} \right) \widehat{S}_z - \frac{i}{2} \left(\omega_{CSA,S}^{(-q)} - \omega_{CSA,S}^{(q)} \right) \widehat{S}_y + \left(\omega_{D,IS}^{(-q)} + \omega_{D,IS}^{(q)} \right) \widehat{I}_z \widehat{S}_z - i \left(\omega_{D,IS}^{(-q)} - \omega_{D,IS}^{(q)} \right) \widehat{I}_z \widehat{S}_y + (\omega_1 - q\omega_R) \widehat{S}_x$$
(1.60)

where $\omega_{CSA,S}^{(\pm q)}$ and $\omega_{D,IS}^{(\pm q)}$ are the complex amplitudes of the Hamiltonian. If not $\sup \left\{ \left| \omega_{CSA,S}^{(-q)} \pm \omega_{CSA,S}^{(q)} \right| , \left| \omega_{D,IS}^{(-q)} \pm \omega_{D,IS}^{(q)} \right| \right\} \gg |\omega_1 - q\omega_R|$, R³ is strongly sensitive to rf-inhomogeneity. Hence, in the case of small CSA and small D_{IS} coupling, R³ exhibits poor efficiency due to rf-inhomogeneity inside the MAS rotor. Therefore, R³ often practically is not chosen. D_{IS} recoupled AH of R³ (q = 1, 2) can be written as

$$\overline{\hat{H}_{D,IS}}^{(1)} = 2\omega_{D,IS}^{|m|} \left[\cos(q\varphi) \hat{I}_z \, \hat{S}_z - \sin(q\varphi) \hat{I}_z \, \hat{S}_y \right] \tag{1.61}$$

with

$$\varphi = \gamma_{PR} + \alpha_{RL}^0 - \omega_R t^0 \tag{1.62}$$

$$q = 1$$
: $\omega_{D,IS}^{|m|=1} = -\frac{1}{2\sqrt{2}} b_{IS} \sin(2\beta_{PR})$ (1.63)

$$q = 2$$
: $\omega_{D,IS}^{|m|=2} = \frac{1}{4} b_{IS} \sin^2(\beta_{PR})$ (1.64)

Since effective dipolar coupling $(\omega_{D,IS})$ is independent of γ_{PR} angle, R³ has γ encoding property. This means that R³ benefits from a good robustness to MAS fluctuations and dipolar truncation effect. Inverse supercycled R³ (SPI-R³) improve the robustness to rf-inhomogeneity, but γ encoding is lost. The setup of R³ consists in finding the optimal recoupling time as well as the optimum rf-field. Such setting must be precise in the case of small CSA.

1.5.2. REDOR

The REDOR scheme for D_{IS} recoupling has been extensively used for distance measurements.[36, 37] It is constituted of π pulses applied every half rotor period under with a variety of rf phasing scheme xx-4, $x\bar{x}$ -4 and supercycles (xy-4, xy-8 or xy-16) designed to increase the robustness to rf-offset and rf-inhomogeneity. D_{IS} recoupled AH of REDOR xy-4 and xx-4 are

REDOR xy-4
$$\overline{\hat{H}_{D,IS}}^{(1)} = 2\omega_{D,IS}\hat{I}_{z}\hat{S}_{z}$$
(1.65)

with

$$\omega_{D,IS}^{|m|=1} = -\frac{\sqrt{2}}{\pi} \kappa b_{IS} \sin(2\beta_{PR}) \cos(\varphi)$$
(1.66)

REDOR xx-4
$$\overline{\hat{H}_{D,IS}}^{(1)} = \omega_{D,IS} \left[\cos(\varphi) \, 2\hat{l}_z \hat{S}_z - \psi \sin(\varphi) \, \hat{l}_z \hat{S}_y \right]$$
(1.67)

$$\omega_{D,IS}^{|m|=1} = -\frac{\sqrt{2}}{\pi} \kappa b_{IS} \sin(2\beta_{PR})$$

with

$$\kappa = \frac{\cos(\psi \, \pi/2)}{1 - \psi^2} \tag{1.69}$$

where

$$\psi = \frac{2\tau_{\rm p}}{\tau_{\rm R}} \tag{1.70}$$

(1.68)

The factor κ describes the finite π pulse effect and ψ is the fraction of the rotor period occupied by the pulses. In the case of infinite π pulse (i.e. $\psi = 0$, $\kappa = 1$), REDOR *xy*-4 and *xx*-4 have non- γ encoding property and non-dipolar truncation effect. In case of windowless RF irradiation (i.e. $\psi = 1$, $\kappa = \pi/4$), REDOR *xx*-4 and REDOR *xy*-4 are analogous to R³ (q = 1) and SPI-R³ (q = 1) respectively. Thus, the factor κ decrease with increasing π pulse length.

REDOR also recouples D_{II} couplings, and the size of the recoupled terms depends on the ratio of pulse width with respect to the period of the sample rotation. Hence, only in the limit of short pulses with respect to the rotation period, D_{II} decoupling is achieved, while under very fast MAS substantial recoupling of the D_{II} occurs.

Nevertheless, in the D-HMQC context, the REDOR scheme may be an interesting option as it is a well-established technique in the measurement of distances and because its setup is easy, as only rf-amplitude and the length of the π pulses must be determined.

1.5.3. Symmetry based recoupling

The symmetry-based rotor-synchronized pulse sequence CN_n^{ν} and RN_n^{ν} has been developed by M Levitt et al.[38, 39] They make use of symmetry properties of the spin interactions of quantum numbers l, m, λ , and μ (**Table.1.6**). The beauty of CN_n^{ν} and RN_n^{ν} is that they can remove those components of spin interaction we do not want and to keep those we do. Hundreds of composition can be useful for different type of dipolar coupling manipulation. Here we concentrate on D_{IS} recoupled RN_n^{ν} sequence which is more restricted than C-type sequence.

Interaction	Space rank	Space component	Spin rank	Spin component
Interaction	l	m	λ	μ
δ _{iso}	0	0	1	-1, 0, 1
CSA	2	-2, -1, 1, 2	1	-1, 0, 1
D_{II}	2	-2, -1, 1, 2	2	-2, -1, 0, 1, 2
D _{IS}	2	-2, -1, 1, 2	1	-1, 0, 1
J_{II}	0	0	0	0
J_{IS}	0	0	1	-1, 0, 1

Table.1.6. Components of spin interactions in the interaction frame under MAS

 $\mathbf{R}N_n^{\nu}$ construction. $\mathbf{R}N_n^{\nu}$ can be constructed by following procedures:

- (i) Determine the pulse sequence element R with duration $n\tau_R/N$. R must rotate 180° about the *x*-axis of the rotating frame. R may be a single π pulse of phase $\phi = 0$ or a composite pulse (for example, 270°-90°). Note that scaling factor κ strongly depend on a basic element R.
- (ii) Derive a 'mirror image' element R' from R by reversing the sign of all phases.
- (iii) Concatenate N/2 phase switched RR' pairs, according to

$$RN_{n}^{\nu} = \left\{ R_{\phi} R_{-\phi}^{\prime} \right\}_{N/2}$$
(1.71)

where the phase shift ϕ is given by $\phi = \pi \nu / N$. The complete RN_n^{ν} sequence spans n rotational periods which characterize the rf-amplitude of R element. rf-amplitude is given by

$$\omega_1 = \frac{N\omega_R}{2n} \tag{1.72}$$

This symmetry imposes the following selection rule on the components of the recoupled first order AH

$$\overline{\widehat{H}_{lm\lambda\mu}}^{(1)} = 0 \quad \text{if } mn - \mu n \neq \frac{N}{2} \cdot Z_{\lambda}$$
(1.73)

Here *l* refers to the rank of the spin interaction with respect to spatial rotations, *m* refers to the spatial rotational component (m = -l, -l+1, , , +l); λ is the rank of the interaction with respect to rotations of resonant spins, and μ is the spin rotational component $(\mu = -\lambda, -\lambda+1, , , +\lambda)$. The symbol Z_{λ} indicates an integer with the same parity as λ , e.g., if λ is even, then $Z_{\lambda} = 0, \pm 2, \pm 4, \ldots$, while if λ is odd, then $Z_{\lambda} = 1, \pm 3, \pm 5, \ldots$ To understand this selection rule for each interaction, space-spin-selection diagram (SSS) diagrams is useful (see [38]).

R18⁵₂ symmetry. As an example, let us check R18⁵₂ = { $(180^{\circ})_{50^{\circ}}(180^{\circ})_{-50^{\circ}}$ }⁹ which is used in PRESTO transfer as mentioned later.[40] For D_{IS} and CSA interaction { l, m, λ, μ } = { $2, \pm 2, 1, \mp 1$ },

$$mn - \mu v = 2 \cdot 2 - 5 \cdot (-1) = 9 = \frac{N}{2} Z_{\lambda} \text{ or}$$

$$mn - \mu v = 2 \cdot (-2) - 5 \cdot 1 = -9 = \frac{N}{2} Z_{\lambda}$$
(1.74)

The recoupling for D_{IS} and CSA interaction are performed. Here, the association of each *m* term with a single value of μ indicate that the recoupling is ' γ -encoding'. In case of 0Q recoupling of D_{IS} interaction $\{l, m, \lambda, \mu\} = \{2, \pm 1 \text{ or } \pm 2, 1, 0\}$, the recoupling should be non- γ encoding. For D_{II} coupling, $mn - \mu n \neq N/2 \cdot Z_{\lambda}$. R18⁵₂ symmetry imposes D_{II} decoupling at the same time as γ -encoded recoupling of CSA and D_{IS} coupling. D_{IS} recoupled AH of R18⁵₂ is

$$\overline{\hat{H}_{D,IS}}^{(1)} = 2\omega_{D,IS}^{|m|=2} \left[\cos(2\varphi) \hat{I}_z \, \hat{S}_x - \sin(2\varphi) \hat{I}_z \, \hat{S}_y \right]$$
(1.75)

with

$$\omega_{D,IS}^{|m|=2} = \kappa \frac{3\sqrt{2}}{4} b_{IS} \sin^2(\beta_{PR})$$
(1.76)

where κ is equal to 0.1754 (for R18⁵₂) in case of R element of an simple π pulse. R18⁵₂ has dipolar truncation effect owing to 1Q D_{IS} recoupling. The Hamiltonian form of R18⁵₂ bracketed by $\pi/2$ pulse will be identical to R³ (q = 2) except for scaling factor.

$$\overline{\widehat{H}_{D,IS}}^{(1)}(\mathbf{R}^3) = \frac{1}{\kappa \, 3\sqrt{2}} \exp\left(i\frac{\pi}{2}\widehat{I}_y\right) \cdot \overline{\widehat{H}_{D,IS}}^{(1)}(\mathbf{R}18_2^5) \cdot \exp\left(-i\frac{\pi}{2}\widehat{I}_y\right)$$
(1.77)

Relationship of the symmetry. R^3 (q = 1, 2) corresponds to $R2_1^0$ (q = 1) and $R4_1^0$ (q = 2) symmetry, respectively. Note that R^3 is the special case in view of γ encoding. The CSA and D_{IS} interaction terms with quantum number $\{l, m, \lambda, v\} = \{2, \pm q, 1, 0\}, \{2, \pm q, 1, 1\}$ and $\{2, \pm q, 1, 1\}$ are symmetry-allowed. Therefore, there is no bijection between symmetry-allowed $\{l, m\}$ and $\{\lambda, v\}$ quantum numbers. However, R^3 is categorized γ encoding as explained in 1.5.1.

REDOR *xy*-4 corresponds to $R4_2^1$ symmetry. This symmetry implements selection of the {*l*, *m*, λ, μ } = {2, ±1, 1, 0} terms. However, the $R4_2^1$ symmetry also allows D_{II} coupling terms of the form {2, ±2, 2, 0}, {2, ±1, 2, ±2} and {2, ±1, 2 ∓2}. These recoupled D_{II} interactions interfere with the operation of REDOR in non-dilute spin systems. REDOR *xy*-8 and REDOR *xy*-16 correspond to supercycle version of $R4_2^1$ symmetry which are $R4_2^1R4_2^{-1}$ and $[R4_2^1R4_2^{-1}]_0[R4_2^1R4_2^{-1}]_{180}$ respectively.

Above discussion is only for first order AH. Second order AH is also important for characterizing detail performance of the recoupling sequence.

1.5.4. SR4²₁

The SR4²₁ has been introduced by Brinkmann and Kentgens to measure ¹H-¹⁷O distances. [41, 42] The method is based on the symmetry theory $(R4^2_1 = \{(180^\circ)_{90^\circ}(180^\circ)_{-90^\circ}\}_2)$ with two additional supercycling: a phase inversion $(R4^2_1R4^{-2}_1)$ to eliminate D_{II} couplings and a threefold cycling $(SR4^2_1 = [R4^2_1R4^{-2}_1]_0[R4^2_1R4^{-2}_1]_{120}[R4^2_1R4^{-2}_1]_{240})$ to improve the robustness to rf-offset. Moreover, it has a very good robustness to rf-inhomogeneities. The D_{IS} recoupled AH is

$$\overline{\hat{H}_{D,IS}}^{(1)} = 2\omega_{D,IS}^{|m|=2}\hat{I}_z\hat{S}_z$$
(1.78)

with

$$\omega_{D,IS}^{|m|=2} = \frac{1}{4} b_{IS} \sin^2(\beta_{PR}) \cos(2\varphi)$$
(1.79)

SR4²₁ is non- γ encoded and not dipolar truncated. SR4²₁ is very well suited to recouple D_{IS} coupling in the presence of strong ¹H D_{II} couplings.

It is also very easy and fast to optimize. The only parameter to consider for optimization is the recoupling time. Indeed, the theoretical optimum rf-amplitude, $\omega_1 = 2\omega_R$, shows a broad optimum and does not require further optimization. MAS frequency values used in the actual experiment lead to moderate rf-amplitude that do not represent technical limitation for probeheads. However, at slow spinning speeds, the theoretical rf-amplitude may not be large enough to properly eliminate ¹H D_{II} coupling.

1.5.5. SFAM

SFAM (Simultaneous Frequency and Amplitude Modulation) have been proposed to overcome REDOR limitation.[43] The rf-field is modulated in amplitude $\omega_1(t)$ and carrier frequency, $\omega_{ref} + \Delta \omega_{ref}(t)$, according to the MAS frequency ω_R :

$$\omega_1(t) = \omega_1^{max} \sin(N\omega_R t) \tag{1.80}$$

$$\Delta\omega_{\rm ref}(t) = \Delta\omega_{\rm ref}^{max}\cos(N\omega_R t) \tag{1.81}$$

where ω_1^{max} is the maximum of the rf-field amplitude modulation and $\Delta \omega_{ref}^{max}$ is the maximum amplitude of the rf-field frequency modulation around its average value. The modulation is done at N = 1 or 2 times the MAS frequency. According to the value of *N*, SFAM-*N* will behave differently. For each *N*, two regions of efficient D_{IS} recoupling can be distinguished.[44] D_{IS} recoupled AH is

Region 1:
$$\overline{\hat{H}_{D,IS}}^{(1)} = 2\omega_{D,IS}^{|m|} \left[\cos(\psi)\hat{I}_z\,\hat{S}_z - \sin(\psi)\hat{I}_y\,\hat{S}_z\right]$$
(1.82)

Regio

n 2:
$$\overline{\hat{H}_{D,IS}}^{(1)} = 2\omega_{D,IS}^{|m|} \hat{I}_z \hat{S}_z$$
 (1.83)

with

$$\psi = \frac{\omega_1^{max}}{N\omega_R} \tag{1.84}$$

N=1:
$$\omega_{D,IS}^{|m|=1} = \kappa b_{IS} \sin(2\beta_{PR}) \cos(\varphi)$$
 (1.85)

N=2:
$$\omega_{D,IS}^{|m|=2} = \kappa b_{IS} \sin^2(\beta_{PR}) \cos(2\varphi)$$
 (1.86)

where κ depend on *N* and region, and ψ is close to 90°. Therefore, SFAM-*N* is non- γ encoded recoupling and not dipolar truncated.[44] With N = 1, both D_{IS} and D_{II} coupling are recoupled (|m| = 1), while with N = 2, D_{IS} coupling only is recoupled (|m| = 2). Therefore, when D_{II} couplings are weak, the use of SFAM-1 recoupling is recommended since this |m| = 1 recoupling method benefits from a $\sqrt{2}$ shorter recoupling time than the |m| = 2 recoupling methods.

SFAM setup requires three parameters to be optimized: recoupling time, ω_1^{max} and $\Delta \omega_{ref}^{max}$. For practical applications, $\omega_1^{max} \sim 1.5N\omega_R$ and $\Delta \omega_{ref}^{max} \sim 0.5N\omega_R$ should be used for region 1 and $\omega_1^{max} = \Delta \omega_{ref}^{max} \sim kN\omega_R$ with k = 3, 5, 7... for region 2. These recoupling conditions will speed up the optimization of SFAM-*N* recoupling by reducing the number of adjustable parameters from three to one. The type of SFAM-*N* scheme and experimental parameters should be selected depending on D_{II} coupling and CSA, the MAS frequency and the probe limitations. The parameter values present a broad optimum, and once *N* and $\Delta \omega_{ref}(t)$ are chosen, the corresponding rf-amplitude barely needs adjustment.

1.6. 2D HETCOR between half-integer quadrupolar nuclei and spin-1/2

Two-dimensional (2D) heteronuclear correlation (HETCOR) nuclear magnetic resonance (NMR) spectroscopy is a valuable tool for the characterization and structural investigation of solid state compounds under MAS. Two possible way exist for building up internuclear high resolution correlation spectra:

- (i) The first method makes use of the non-vanishing isotropic terms of *J*-coupling, which directly characteristic of the existence of a chemical bond like in liquid state NMR;
- (ii) The second method is to restore the through-space dipolar interaction. This interaction vanishes under MAS and need to be reintroduced using continuous wave or modulated rf irradiation dipolar recoupling methods.

These methods facilitate spectral assignment owing to the improved resolution and extracted information. The HETCOR methods using coherence transfers via the *J*-coupling (*J*-HETCOR) or via the dipolar couplings (*D*-HETCOR) are complementary. The *J*-HETCOR techniques help in identifying the molecular entities in solid state compound, while the *D*-HETCOR techniques can be used to establish their 3 dimensional structures and to reveal the noncovalent intra- and intermolecular interaction.

A variety of *J*-HETCOR and *D*-HETCOR pulse sequences have been proposed so far. **Fig.1.6** is their classification.[42] The sequences are classified according to the mode of detection, direct or indirect, and the order of coherences during the t_1 evolution period.



Fig.1.6. Schematic classification of 2D HETCOR NMR experiments in solids (adapted from [42])

1.6.1. Through-bond correlation

One of the most informative classes of solution-state NMR experiments consists in correlating the signals of distinct isotopes through the use of heteronuclear multiple quantum coherences (HMQC) or using the Insensitive Nuclei Enhanced by Polarization Transfer (INEPT) pulse sequence. These methods have been adapted in the last decades for the study of solids under MAS conditions.[45,46]



Fig.1.7. Schematic diagram of (a) J-RINEPT and (b) J-HMQC

We start by considering the standard *J*-RINEPT experiment, shown in **Fig.1.7**(a), involving an isolated pair of chemically bonded *I* and *S* nuclei. Density operator evolution can be calculated and the signal intensity (build-up curve) observed in the *S* channel can be derived as

$$S(t_1, t_2)_{RINEPT} \sim \alpha \sin(\pi J_{IS}\tau') \sin(\pi J_{IS}\tau) \cos(\omega_I t_1) \exp\left(-\frac{\tau}{T'_{2,I}} - \frac{\tau'}{T'_{2,S}}\right)$$
(1.87)

where $\alpha = \gamma_I \gamma_S^2 \exp(i\omega_S t_2)$, J_{IS} is the scalar coupling, γ_I and γ_S are the nuclear gyromagnetic ratio, while τ and τ' denote the defocusing and refocusing delays, respectively.

In the *J*-HMQC experiment (**Fig.1.7**(b)), similarly, density operator evolution can be calculated and the signal is observed as

$$S(t_1, t_2)_{HMQC} \sim \beta \sin^2(\pi J_{IS}\tau) \cos(\omega_S t_1) \exp\left(-\frac{2\tau}{T'_{2,I}}\right)$$
(1.88)

where $\beta = \gamma_I^3 \exp(i\omega_I t_2)$. When the experiments are optimized, i.e., $\tau_{opt} = \tau'_{opt} = 1/(2 J_{IS})$ for an isolated spin pair. In addition, signal expression of many spin system given in [47].

The relative sensitivity of RINEPT (direct:DD) and HMQC(indirect:ID) per unit of time is derived from[48]

$$\xi = \frac{(S/N)_{ID}}{(S/N)_{DD}} \approx \frac{f_{ID}^2}{f_{DD}} \left[\frac{(FWHM)_S Q_I}{(FWHM)_I Q_S} \right]^{\frac{1}{2}} \left(\frac{\gamma_I}{\gamma_S} \right)^{\frac{3}{2}} \frac{1}{\sqrt{2\pi}}$$
(1.89)

where $(FWHM)_{I(S)}$ are full width at half maximum (in Hz), $Q_{I(S)}$ are the quality factors of the sample coil, and $f_{ID(DD)}$ the polarization transfer efficiencies. There is only one transfer in the case of direct detection (f_{DD}) , whereas two are required with indirect detection (f_{ID}) . The direct

and indirect transfer efficiencies is assumed the same value, $f_{ID} = f_{DD}$. From this equation, the gain increase when increasing γ_I / γ_S , $FWHM_S / FWHM_I$ and f_{ID} .

Both pulse sequence will be optimized in such way that

- (i) Under MAS, the delay in the experiments are performed with rotor synchronization.
- (ii) CT selective pulse must be sent on the quadrupolar nuclei channel. Therefore, CT selective pulse must be optimized on the sample prior to the experiments.
- (iii) The delay (τ and τ ') should be optimized on the sample. Theoretically set to $1/(2 J_{IS})$ for an isolated spin pair, which may be of several ms if one wants to transfer coherence through small *J*-couplings.

In addition, a quick determination of the T_2 ' for a target sample using an echo sequence, is also a good option. If the T_2 ' turns out to be short, for example in the presence of paramagnetic centers in the sample, or for amorphous samples, the *J*-RINEPT and *J*-HMQC build-up signal may be weak and it is difficult to obtain the 2D spectra. In the case of using ¹H, D_{II} decoupling sequence, such as FSLG, PMLG and DUMBO, should be applied on ¹H channel since D_{II} coupling significantly shorten T_2 ' decay.[46, 49]

It is well known that the magnetization transfer in the *J*-HMQC experiment between spin-1/2 and quadrupolar nuclei for solids is achieved not only through *J* coupling but also through residual dipolar splitting (RDS) resulting from the second-order cross-terms between the quadrupolar and dipolar interactions unlike in the solution.[50] In some case, RDS can be larger than *J* coupling. Nevertheless, regularly, RDS is still small and suffer from short T_2 ' decay in solids. The RDS is out of scope in this thesis.

Even if the 2D *J*-RINEPT and *J*-HMQC experiment provides a more selective means of correlation than its dipolar counterpart, the *D*-RINEPT and *D*-HMQC experiment, which highlights proximities between close nuclei, should be an alternative.

1.6.2. Through-space correlation

Two type of experiments are described here to obtain 2D correlations using dipolar couplings to highlight proximities between two different nuclei, one of them being a quadrupolar one. First type of experiments are based on direct method, which is similar to *J*-RINEPT. This type of experiments are CP, TEDOR, *D*-RINEPT and PRESTO. Second type of experiments are based on indirect method, which corresponds to Double CP, *D*-HSQC and *D*-HMQC pulse sequences. In the case of solid state NMR, *D*-HSQC is less advantageous than *D*-HMQC.[42] Therefore, *D*-HMQC is only described and emphasized for indirect method.
1.6.2.1. The CP-HETCOR experiment

CP-HETCOR between spin-1/2 and half-integer quadrupolar nuclei is identical to the familiar HETCOR scheme employed to correlate spin-1/2 isotopes.[51] However, CT selective rf-irradiation should be employed for the half-integer quadrupolar channel.

CP dynamics between one spin-1/2 nucleus (*I*) and one half-integer (S = n/2, n > 1) nucleus presents a considerable challenge due to the very complex spin dynamics involved in both the spin-locking of *S* nucleus and the $I \rightarrow S$ CP transfer itself. The set up procedure is as follow.

(i) The rf-amplitude on the quadrupolar channel during the CP transfer, $\omega_{1,S}$, must be optimized so that it achieves efficient spin-lock of the CT.

The effect of MAS on spin-locking of *S* magnetization can be categorized based on the magnitude of the adiabaticity parameter:

$$\alpha_{ad} = \frac{\omega_{1,S}^2}{\omega_0 \omega_R} \tag{1.90}$$

that is related to the speed at which the quadrupole interaction crosses zero as the sample rotates.[52] The efficiency of spin-locking increases when $\alpha_{ad} \ll 1$ or when $\alpha_{ad} \gg 1$, whereas the intermediate case $\alpha_{ad} \sim 1$ results in a loss of spin-locked states. In case of strong quadrupole interaction and fast spinning speed, only the first case, called sudden passage, is most of the time accessible.

Under typical conditions, in the sudden passage condition, selective manipulation of the CT requires rf-amplitudes in the order of a few kHz (ranging from 5 to 20 kHz), but must still be large enough so that nuclei resonating at different offsets are efficiently spin-locked. Furthermore, the detrimental R³ conditions where is multiple of MAS frequency, must be avoided.

$$\left(S + \frac{1}{2}\right)\omega_{1,S} = q\omega_R \quad (q: \text{integer})$$
 (1.91)

(ii) In the case of weak $\omega_{1,S}$, the nutation frequency acting on the central-transition (CT) is multiplied by (S + 1/2), and the fast MAS previous Hartmann–Hahn matching condition between spin-1/2 nucleus translates into:

$$\left(S + \frac{1}{2}\right)\omega_{1,S} = \varepsilon\omega_{1,I} + n\omega_R \quad (\varepsilon = \pm 1; \ n = \pm 1, \pm 2)$$
(1.92)

(iii) Finally CP contact time is optimized. Optimal values are on the order of a few milliseconds.

As a conclusion, the CP method applied to quadrupolar nuclei is not an easy and not robust experiment. The efficiency of the CP transfer being C_Q dependent, sites with very different C_Q

may not be observable simultaneously. To be efficient, the rf-amplitude must be weak, which leads to a large sensitivity to off-resonance irradiation and rf-mismatch. In order to overcome the sensitivity to rf-offset, Multi Pulse (MP)-CP have been proposed.[53]

1.6.2.2. D-RINEPT experiments

D-RINEPT is an alternative to CP. This method derives from *J*-RINEPT[54] but R^3 is applied on spin-1/2 channel during the defocusing, τ , and refocusing delays, τ ', of *D*-RINEPT sequence (**Fig.1.8**).





Density operator evolution can be calculated. During the R³ (q = 1) recoupling applied on the *S* channel (observed channel), the density operator evolves under the effect of the AH given by Eq.(1.61) and assuming $\tau = \tau'$:

$$\hat{I}_{x} \xrightarrow{\overline{H_{D,IS}}^{(1)}} - \frac{\cos(\omega_{D,IS}^{|m|=1}\tau) \hat{I}_{x}}{\cos(\omega_{D,IS}^{|m|=1}\tau) \hat{I}_{x}} + 2\sin(\omega_{D,IS}^{|m|=1}\tau) \{\cos(\varphi) \hat{I}_{y} \hat{S}_{z} + \sin(\varphi) \hat{I}_{y} \hat{S}_{y} \}$$

$$\xrightarrow{\frac{\pi}{2} \hat{I}_{x}, \frac{\pi}{2} \hat{S}_{x}}{\longrightarrow} 2\sin(\omega_{D,IS}^{|m|=1}\tau) \{\cos(\varphi) \hat{I}_{z} \hat{S}_{y} + \sin(\varphi) \hat{I}_{z} \hat{S}_{z} \}$$

$$\xrightarrow{\widehat{H_{D,IS}}^{(1)}} \sin^{2}(\omega_{D,IS}^{|m|=1}\tau) \{\cos^{2}(\varphi) + \sin^{2}(\varphi) \} \hat{S}_{x}$$
(1.93)

The first term in Eq.(1.93) is not transferred to the *S* nucleus and is discarded.

In the *D*-RINEPT sequences,

- (i) CSA dephasing of spin-1/2 is refocused by a hard π pulse in the middle of a one-rotor period delay (**Fig.1.8**), whereas D_{IS} refocusing is prevented by a CT selective π pulse on the quadrupolar nucleus;
- (ii) The spin-1/2 isotropic chemical shifts and J_{IS} couplings, which are not modulated by MAS, have their dephasings canceled by R³-irradiation;

(iii) To prevent any quadrupolar modulation, the delays in between the three CT-selective pulses must be rotor synchronized: $p\tau_R$ and $p'\tau_R$. By also taking into account the gap delays (τ_R), each R³ period must therefore last $(p - 1)\tau_R$ and $(p' - 1)\tau_R$. D_{IS} dephasings onto the spin-1/2 nucleus, related to other not manipulated active nuclei, are cancelled due to the π pulse in the middle of each echo period;

(iv) For 2D correlation experiment, t_1 evolution block is inserted after first $\pi/2$ pulse.

The *D*-RINEPT is easier to optimize than CP-HETCOR and less dependent on the C_Q value. Moreover, R³ methods are less sensitive to rf-offset. On the other hand, a disadvantage of R³ is poor efficiency owing to poor robustness to rf-inhomogeneity. Recently, Rossini et al reported *D*-RINEPT method using SR4²₁ recoupling, instead of R³.[55]

1.6.2.3. PRESTO experiments

Xin Zhao et al. proposed heteronuclear polarization transfer methods utilizing single channel recoupling based on symmetries R18⁷₁ and R18⁵₂ which produces 1Q Hamiltonian.[56] This class of methods was called PRESTO (Phase-shifted Recoupling Effects a Smooth Transfer of Order). PRESTO also has an advantage of no continuous irradiation to quadrupolar nuclei, compared to CP. There are three type of PRESTO (I, -II, -III) sequence (**Fig.1.9**).



Fig.1.9. Schematic diagram of (a) PRESTO-I, (b) PRESTO-II, (c) PRESTO-III where *I* and *S* channel are assumed to be spin-1/2 and half-integer quadrupolar nuclei, respectively.

If CSA is neglected, density operator evolution ($\tau = \tau'$) of PRESTO-I is calculated as

$$\hat{I}_{z} \xrightarrow{\left(\widehat{H}_{D,IS}^{(1)}\right)_{0}} e^{(-i2\varphi\hat{I}_{z})} \{ \cos\left(\omega_{D,IS}^{|m|=2}\tau\right) \hat{I}_{z} - 2\sin\left(\omega_{D,IS}^{|m|=2}\tau\right) \hat{I}_{y} \hat{S}_{z} \} e^{(i2\varphi\hat{I}_{z})}$$

$$\xrightarrow{\frac{\pi}{2}\hat{S}_{x}} e^{(-i2\varphi\hat{I}_{z})} \{ -2\sin\left(\omega_{D,IS}^{|m|=2}\tau\right) \hat{I}_{y} \hat{S}_{x} \} e^{(i2\varphi\hat{I}_{z})}$$

$$(1.94)$$

$$\xrightarrow{\left(\widehat{H}_{D,IS}^{(1)}\right)_{\pi/2}} \sin^2\left(\omega_{D,IS}^{|m|=2}\tau\right) \widehat{S}_y$$

where

$$\left(\overline{\hat{H}_{D,IS}}^{(1)}\right)_0 = \omega_{D,IS}^{|m|=2} \exp(-i2\varphi I_z) 2\hat{I}_x \hat{S}_z \exp(i2\varphi \hat{I}_z)$$
(1.95)

$$\left(\overline{\hat{H}_{D,IS}}^{(1)}\right)_{\pi/2} = \omega_{D,IS}^{|m|=2} \exp\left(-i2\varphi \hat{I}_z\right) 2\hat{I}_y \hat{S}_z \exp\left(i2\varphi \hat{I}_z\right)$$
(1.96)

Thus, *S*-spin transverse magnetization is generated at the beginning of the acquisition period. The feature of each PRESTO sequence is below.

PRESTO-I. *S*-spin isotropic chemical shift evolve during the refocusing delay. This is not preferable in the case of *S* spin with different chemical shifts.

PRESTO-II. This sequence includes an additional spin echo element on the *S*-spin channel in order to refocus *S*-spin isotropic chemical shift, but PRESTO-II cannot refocus *I*-spin CSA which can interfere with the D_{IS} recoupling since D_{IS} recoupled AH generated by R18⁷₁ and R18⁵₂ does not commute with *I*-spin CSA recoupled AH.

PRESTO-III. A π pulse on the S-spin channel is inserted at the exact center of the τ interval. The phase of the *I*-spin irradiation is shifted by π at the same instant. Such procedure refocuses S-spin isotropic chemical shift as well as the CSA of *I*-spin. A disadvantage of PRESTO-III is the larger step for the recoupling time, compared to PRESTO-II. In the case of the system with large heteronuclear dipolar coupling, such large steps can prevent the adjustment of the recoupling time to its value leading to maximal transfer efficiency.

For 2D correlation experiment, t_1 evolution period with $\pi/2$ bracket is inserted before the defocusing delay.[57]

The PRESTO is easier to optimize than CP-HETCOR. R18⁷₁ and R18⁵₂, which have D_{II} decoupling property, is suitable 1Q D_{IS} recoupling for the nuclei subject to strong D_{II} coupling, such as ¹H. Furthermore, these symmetry-based recoupling are more robust to rf-mismatch and rf inhomogeneity than R³. So far, the PRESTO sequence has only been reported with recoupling applied to the non-observed channel. Recently, the usefulness of PRESTO sequence to transfer DNP-enhanced ¹H polarization to quadrupolar nuclei has been demonstrated.[57]

1.6.2.4. D-HMQC experiment.

D-HMQC sequence with R³

In 2006, Z. Gan et al. and S. Cavadini et al. proposed *D*-HMQC with R³ recoupling.[50, 58] Although these experiments were initially proposed for the indirect observation of ¹⁴N via ¹H or ¹³C, they can be also employed for half-integer quadrupolar nuclei. **Fig.1.10(a)** shows *D*-

HMQC sequence, for which the recoupling is applied on the direct channel (denoted DR for direct recoupling hereafter) proposed by Z Gan.[58] The evolution of the density operator during *D*-HMQC sequence with R^3 (q = 2)is as follow (assuming $t_1 = 0$).

$$\hat{I}_{x} \xrightarrow{\overline{H_{D,IS}}^{(1)}} \cos\left(\omega_{D,IS}^{|m|=2}\tau\right) \hat{I}_{\overline{x}} + \sin\left(\omega_{D,IS}^{|m|=2}\tau\right) \{\cos(2\varphi) 2\hat{I}_{y}\hat{S}_{z} + \sin(2\varphi) 2\hat{I}_{z}\hat{S}_{z}\}$$

$$\xrightarrow{\frac{\pi}{2}\hat{S}_{x}}} \sin\left(\omega_{D,IS}^{|m|=2}\tau\right) \{-\cos(2\varphi) 2\hat{I}_{y}\hat{S}_{y} - \sin(2\varphi) 2\hat{I}_{z}\hat{S}_{y}\}$$

$$\xrightarrow{\pi\hat{I}_{y}}} \sin\left(\omega_{D,IS}^{|m|=2}\tau\right) \{\cos(2\varphi) 2\hat{I}_{y}\hat{S}_{y} + \frac{\sin(2\varphi) 2\hat{I}_{z}\hat{S}_{y}}{2}\}$$
(1.97)

Second term can be removed by the phase cycle of π pulse in *I* channel

$$\xrightarrow{\frac{\pi}{2}\hat{S}_{x}} \sin\left(\omega_{D,IS}^{|m|=2}\tau\right)\cos(2\varphi) 2\hat{I}_{y}\hat{S}_{z}$$

$$\xrightarrow{\overline{\hat{H}_{D,IS}}^{(1)}} - \sin^{2}\left(\omega_{D,IS}^{|m|=2}\tau\right)\cos^{2}(2\varphi) \hat{I}_{x}$$

where

$$\overline{\hat{H}_{D,IS}}^{(1)} = 2\omega_{D,IS}^{|m|=2} \left[\cos(2\varphi) \hat{S}_z \hat{I}_z - \sin(2\varphi) \hat{S}_z \hat{I}_y \right]$$
(1.98)

It is noted that final result of the density operator evolution in this *D*-HMQC sequence depend on γ_{PR} angle owing to selecting ± 1 coherence on the *I* channel by the phase cycle.



Fig.1.10. Schematic diagram of ${}^{1}H-{}^{14}N$ *D*-HMQC presented by Z Gan

Although *D*-HMQC sequence looks similar to *J*-HMQC sequence, there are some important differences for the optimization of the pulse sequence:

(i) Rotary-resonance has the specific property that a delay introduced during the R³ irradiation may change the AH acting on the spins. As an example, a gap in R³ irradiation of half (q = 1) or a quarter (q = 2) rotor period changes the sign of the CSA and D_{IS} recoupled AH, as would do a π pulse in a Hahn echo experiment.[59, 60] This sign change create a rotary resonance echo for CSA and D_{IS} . When a spin echo π pulse is added in the middle of the gap, the timing of the two R³ periods must be continuous in rotor position. The spin echo segment (between the end of defocusing and beginning of refocusing of R³ block) must be integer (q = 1) or half integer (q = 2) numbers of rotor period. In practical applications,

even numbers of rotor period $(2k\tau_R)$ are often used to avoid any kind of modulation. This rotary resonance concept is also applied to *D*-RINEPT sequence as seen in 1.6.2.2.

- (ii) The spin-echo segment increments $2\tau_R$ for every two t_1 increments. However, this increment could lead to sidebands occurring at $\nu_R/2$ since detected signal decrease by the contribution from T_2 ' decay of ¹H every $2\tau_R$. T_2 ' decay of ¹H is relatively shorter owing to homonuclear dipolar coupling. Similarly, short T_2 ' decay of the observed nucleus broaden the resolution in the indirect dimension in 2D spectra of *D*-HMQC.
- (iii) R³ irradiation must be q = 2 condition ($\omega_1 = 2\omega_R$) which include D_{II} decoupling.
- (iv) Finite pulse length should be included in the rotor-synchronization conditions. Therefore, t_1 period set to $t_1 = n\tau_R$ (the pulse length on the ¹⁴N channel must be counted) in order to refocus first order quadrupolar interaction as well as the careful adjustment of the delay between the recoupling and $\pi/2$ pulse before t_1 evolution.

Thus, unlike *J*-HMQC, there are several careful set-up points owing to recoupling sequence, MAS and some kind of anisotropic interactions. After building the sequence, the *D*-HMQC is easier to optimize than CP-HETCOR. However, R^3 is sensitive to rf maladjustement and inhomogeneity.

Recoupling on direct channel and Indirect channel.

The recoupling sequence can only be efficiently applied to the spin-1/2 nucleus. The observed signal can either be that of the spin-1/2 nucleus (**Fig.1.11(a**)) or that of the quadrupolar nucleus (**Fig.1.11(b**)).[42, 44, 54] -DR and -IR stand for Direct (observed) channel Recoupling and Indirect (non-observed) channel Recoupling.

As exhibited in Fig.1.11, the rotor synchronization in *D*-HMQC is redefined as follows.[44]

$$T_{\rm A} + \tau + T_{\rm B} + \frac{t_1}{2} = n\tau_{\rm R}$$
 (1.99)

$$\tau = k\tau_R \tag{1.100}$$

$$2T_{\rm A} + t_1 = \mathrm{p}\tau_{\rm R} \tag{1.101}$$

Eq.(1.99) insures that the observed spin anisotropy (quadrupolar or CSA) does not modulate the signal that could lead to sidebands occurring at $v_R/2$ for example. Eq.(1.100) is required by the definition of rotor synchronized recoupling sequences. Eq.(1.101) is critical for non- γ encoded recoupling. Delay T_A and T_B are recalculated every t_1 increment based on the minimum delay required to fit t_1 and pulses between the recoupling pulses. If S spin is integer quadrupolar nucleus, as mentioned in D-HMQC-DR with R³, t_1 must be rotor synchronized ($t_1 = j\tau_R$) to refocus first order quadrupolar interaction. In case of ¹H-{X} D-HMQC-DR, relation.(1.99) can be relaxed to $T_A + \tau + T_B + \frac{t_1}{2} = \frac{1}{2}n\tau_R$ since the main signal modulation originates from homonuclear dipolar coupling that has a $\tau_R/2$ modulation. In that case, a $\tau_R t_1$ increment can be fulfilled with $T_B = 0$. Moreover it is important to have a steady increment of n with t_1 in relation.(1.99) to remove a potential modulation induced by T_2 ' relaxation.



Fig.1.11. Schematic diagram of (a) D-HMQC-DR, (b) D-HMQC-IR

Most of the time, *D*-HMQC-IR benefits from higher sensitivity owing to the short quadrupolar longitudinal relaxation time and the possibility of using population transfer technique before first $\pi/2$ pulse, in order to enhance the population difference across the CT. Moreover, this version also leads to a better robustness with respect to spinning speed fluctuation since the *D*_{*IS*} recoupling is sent on the non-observed channel and the CSA of the observed nucleus is not reintroduced.

Conversely, *D*-HMQC-DR can be frequently used in the case of the experiment involving integer quadrupolar, such as ¹⁴N, because of the absence of refocusing π pulse for such isotopes. In the case of quadrupolar nuclei subject to large quadrupolar interactions, *D*-HMQC-DR profits from the shorter maximum value of t_1 , owing to observation along F1 of a second-order line-width. Furthermore, for protonated compounds, *D*-HMQC-DR might benefit from higher sensitivity since the quadrupolar nuclei can be detected via ¹H isotope or the sensitivity can be increased by replacing the first $\pi/2$ pulse by an initial ¹H \rightarrow *I* CP transfer. For ¹H-{X} *D*-HMQC-DR experiment, *D*_{II} decoupling scheme can be applied during both t_1 and t_2 periods in order to enhance the spectral resolution.[61] However, *D*-HMQC-DR is more sensitive to MAS frequency instabilities since the CSA of the observed I nucleus (CSA_I) is reintroduced and can only be refocused by the perfect rotor-synchronization of the two D_{IS} recoupling periods. Such rotor-synchronization is more difficult to achieve for long t_1 period.

Comparison of several recoupling sequence in D-HMQC.

The choice of the D_{IS} recoupling influences the performances of *D*-HMQC experiment. Although *D*-HMQC-DR with R³ recoupling have been successfully applied to observe ¹⁴N nuclei indirectly via ¹H, R³ is less robust to rf inhomogeneity and has the property of dipolar truncation effect (long range recoupling is not possible).

Therefore several recoupling sequences have been explored and their performances have been compared. These methods can be classified in four different groups: R^3 , symmetry-based sequences (R12⁵₃, R20⁹₅ and SR4²₁), REDOR, and SFAM.

Except for \mathbb{R}^3 (q = 1, 2), these recouplings are non- γ -encoded and can accomplish a 'longitudinal two-spin-order' ($\hat{I}_z \hat{S}_z$) recoupling of the dipolar interactions. Therefore, density operator evolution of *D*-HMQC is the same as that of *J*-HMQC. This D_{IS} recoupled AH commutes across different spin pairs and therefore does not suffer from dipolar truncation and hence, both short- and long- range distance can be observed simultaneously. In non- γ encoded recoupling schemes, SR4²₁ and SFAM recoupling show better performance than REDOR and other non- γ encoded symmetry based recoupling.[62] Moreover, X. Lu et al. further investigated the performance of SFAM and SR4²₁ in *D*-HMQC-DR and -IR.[44] Recommended recouplings are shown in **Table.1.7** with respect to the size of D_{II} and CSA.

Channel	D-HMQC-DR				D-HMQC-IR			
D _{II}	large		small		large		small	
CSA or rf-offset	large	small	large	small	large	small	large	small
recoupling	$SR4_1^2$ or SFAM- 2 ^{reg2} or R ³ (q=2)	SR4 ²	SFAM- 1^{reg2} or $R^{3}(q=1)$	SFAM- 1 ^{reg2}	SR4 ² or SFAM- 2 ^{reg2}	SR4 ²	SFAM-1 ^{reg2}	

Table.1.7. Recommended recouplings as function of the magnitude of D_{II} and CSA or rf-offset.

In case of *D*-HMQC-IR, $SR4_1^2$ or SFAM recoupling schemes should be used for their robustness to rf inhomogeneity. Furthermore, the robustness to MAS fluctuation of these recoupling methods is generally sufficient. If D_{II} coupling are small, SFAM-1^{reg2} scheme should

be selected since it results in shorter mixing time. This will limit the losses due to T_2 ' relaxation on the observed spin. Otherwise, SR4²₁ or SFAM-2 can be employed but SR4²₁ often outperform SFAM-2. If the spin-1/2 exhibits large CSA or rf-offsets, SFAM-2^{reg2} allows selecting a recoupling condition for larger rf-amplitude ($\omega_1 = 3, 5, 9\omega_R$) than SR4²₁ ($\omega_1 = 2\omega_R$) that will increase the robustness with respect to these interactions. For *D*-HMQC-DR, the choice of the recoupling sequences is similar when the CSA is small. In the case of large CSA, R³ offers high robustness to MAS fluctuations and rf inhomogeneity.

R³ and SR4²₁ schemes only require the optimization of two parameters (recoupling time and rf-amplitude). In case of SFAM, a third parameter should be optimized, the frequency offset.

Note that among these recoupling schemes, R^3 (q = 1, 2) method is the only which is γ encoded. γ encoded recoupling are more robust to MAS fluctuation and exhibits 25 % higher efficiency than non- γ encoded ones. Furthermore, they are affected by dipolar truncation, which allows selecting correlation with 1st neighbors, thus facilitating the spectral assignment.

Comparison of CP-HETCOR and D-HMQC

G Tricot et al. demonstrated the performance of *D*-HMQC compared to CP-HETCOR.[63] The performances of 27 Al-{ 31 P} *D*-HMQC-IR using SFAM-1 recoupling have been compared to those 31 P-{ 27 Al}CP-HETCOR for a potassium alumino-phosphate glass (with composition 50K₂O-10Al₂O₃-40P₂O₅). **Fig.1.12** display the 27 Al-{ 31 P}*D*-HMQC and 31 P-{ 27 Al} CP-HETCOR 2D spectra obtained at 18.8 T using the same MAS frequency of 20 kHz and the same sample volume (3.2 mm probe-head). The spectrum was acquired, setting the rf-offset on resonance for AlO₅ species. Experimental time is 17 and 68 hours for *D*-HMQC and CP-HETCOR respectively.



Fig.1.12. ³¹P/²⁷Al correlation NME spectra of $50K_2O-10Al_2O_3-40P_2O_5$ glass acquired using (a) ²⁷Al-{³¹P}*D*-HMQC-IR and (b)³¹P-{²⁷Al}CP-HETCOR at 18.8 T under MAS frequency of 20 kHz. (Adapted from [63])

The comparison of these two spectra clearly indicates the superiority of the *D*-HMQC technique at high field. Indeed, the *D*-HMQC spectrum shows a correlation scheme similar to that obtained at 9.4 T with an improved resolution in both dimensions, whereas the CP-HETCOR spectrum only displays a weak correlation involving AlO₅ species. The absence of cross-peaks for AlO₆ and AlO₄ environments illustrates the high sensitivity to rf-offset for CP transfer. The enhanced *D*-HMQC spectral resolution at 18.8 T allows improving the structural analysis by showing clear evidence of two P species in the vicinity of tetrahedral aluminium, whereas the experiment performed at 9.4 T only evidences a single P-AlO₄ species.

As mentioned in section *D*-HMQC with R^3 , the resolution in the indirect dimension of a 2D *D*-HMQC spectrum suffer from the T_2 ' decay of the observed nucleus during the echo. Hence, analysis of indirect linewidth must be done with care. On the other hand, for CP, only singlequantum coherences are involved such that the resolution in the indirect dimension is the same as for one-dimensional experiment.

The experiments with frequency splitter

In the periodic table of elements, there are many NMR-active nuclei with small Larmor frequency difference. However, due to the limitation of commercial solid state-NMR probes, double-resonance experiment for ${}^{13}C_{-}{}^{27}Al$, ${}^{13}C_{-}{}^{51}V$, ${}^{27}Al_{-}{}^{51}V$, ${}^{23}NA_{-}{}^{27}Al$ and ${}^{23}Na_{-}{}^{51}V$ is hardly achieved. A solution consists in the use of an external frequency splitter (such as the REDORbox device commercialized by NMR Service GmbH) connected to a single rf channel of probe head. Such device enables double resonance experiments involving nuclei with close Larmor frequencies. The major limitation of the frequency splitter is the impossibility of simultaneous rf irradiation at both resonance frequencies, precluding some experiments, such as CP. *D*-HMQC is compatible with frequency splitter since *D*-HMQC does not require simultaneous rf irradiation on the channels of correlated isotopes. Organoaluminium compounds have been analyzed by ${}^{13}C_{-}{}^{27}Al$ *J*- and *D*-HMQC with frequency splitter.[64, 65] Recently, 2D ${}^{13}C_{-}{}^{27}Al$ correlation spectra for Al-based MOFs have been acquired using a frequency splitter, ${}^{13}C_{-}{}^{27}Al$ CP-*D*-HMQC sequence, in which ${}^{13}C$ transverse magnetization is created using ${}^{1}H_{-}{}^{13}C$ CP transfer, the ${}^{1}H$ magnetization being enhanced by Dynamic Nuclear Polarization.[66]

t₁ noise problem in 2D experiment

One key drawback of the *D*-HMQC pulse sequence is that both the MAS frequency and spectrometer must be very stable to avoid excessive t_1 -noise because the signals from uncorrelated spins are imperfectly suppressed by phase cycling alone. Especially, in case of *D*-

HMQC-DR, non- γ encoded recoupling is very sensitive to MAS fluctuation since each crystallite must have the same orientation at the beginnings of defocusing and refocusing periods. Such condition is especially difficult to achieve in *D*-HMQC-DR experiment when the t_1 evolution time and recoupling time are long due to narrow peaks and weak dipolar interactions, respectively. Such MAS fluctuations lead to random change in the detected signal intensity and it is difficult to suppress the t_1 noise by phase cycle.

In the case of double CP, uncoupled spin magnetization is reduced by inserting purging (2Q filter) period into between t_1 evolution and signal detection.[67] However, this purging period cannot be applied to *D*-HMQC sequence in principle. Therefore, it may be difficult to apply *D*-HMQC-DR to the isotopes with very low abundance, when the heteronuclei are dilute or when there are multiple overlapping ¹H signals.

If completely uncoupled signal exist in the spectrum, the signal can be suppressed by inserting a single, long, low amplitude selective saturation pulse before the start of *D*-HMQC (**Fig.1.13**).[68] If completely uncoupled signal is removed, t_1 -noise from completely uncoupled signal is suppressed and this method cleans the 2D spectrum. However, this approach does not suppress the t_1 -noise for coupled nuclei. Hence, the t_1 -noise problem of 2D *D*-HMQC experiments still unsolved.



Fig.1.13. Schematic diagram of D-HMQC-DR with selective saturation pulse

Constant time D-HMQC approach

Recently, A. Rossini. et al. proposed constant time *D*-HMQC approach to indirectly detect via spin-1/2 nuclei wideline spectrum which consists of many sidebands owing to large anisotropic interaction, such as CSA.[69] **Fig.1.14** illustrates constant time *D*-HMQC pulse sequence. The spin echo block in the middle of the sequence is fixed to a constant duration $(2k\tau_R > t_{1,max})$ and the θ pulses are stepped outwards to enable arbitrary, rotor asynchronous t_1 increments. θ pulse should be optimized to achieve broadband excitation. Owing to constant time between recouplings, detected signal is not modulated with T_2 ' decay. The sensitivity gain, ξ , provided by the indirect detection of wideline spectrum using constant time *D*-HMQC experiment with respect to direct detection strongly depends on the investigated sample.

They demonstrated that constant time *D*-HMQC-DR with SR4²₁ enabled rapid acquisition of 2D ¹H-¹⁹⁵Pt correlation of cis-platin and trans-platin in experimental time of 2 hours. This indirect detection strategy provides sensitivity gains between 1 to 2 orders of magnitude compared to direct detection. On the other hand, constant time ¹H-⁷¹Ga *D*-HMQC-DR experiments required slightly longer experimental time than direct detection due to relatively low ξ . However, the advantage of this method is that overlapping sites could potentially be resolved by correlation to different ¹H chemical shifts. This method also suffers from *t*₁ noise. If large *t*₁ noise appears in the 2D spectra, the sensitivity is significantly decreased.



Fig.1.14. Schematic diagram of constant time D-HMQC-DR sequence

Indirect ST spectrum in D-HMQC

In the case of integer quadrupolar nucleus, such as ¹⁴N, the spectrum does not exhibit central transition but only the transitions between energy levels $1 \leftrightarrow 0$ and $0 \leftrightarrow -1$. Hence, for the indirect observation of ¹⁴N spectrum, the complete rotor-synchronized t_1 acquisition is required to average out first order quadrupolar interaction.

In the case of half-integer quadrupolar nucleus, first order quadrupolar interaction also affect the ST. Therefore, ST can be indirectly detected using complete rotor synchronized t_1 acquisition and hard $\pi/2$ pulse instead of CT selective pulse in indirect channel of half-integer quadrupolar nuclei.

If only CT spectrum is required (sometimes, observation of ST spectrum contaminate CT spectrum), rotor-asynchronous t_1 acquisition is preferable. On the other hand, the duration between two recoupling blocks should be rotor- synchronized.

Recently, Y. Nishiyama and co-worker demonstrated that CT spectrum and ST spectrum (center band and spinning side band) can be indirectly detected using conventional and constant

time *D*-HMQC-DR with various condition of t_1 acquisition (synchronous or asynchronous) and the rf pulses (hard or soft pulse with appropriate rf-offset) of indirectly detected channel.[70, 71]

The observation of center band of ST₁ spectrum has the benefit from a more accurate determination of quadrupolar coupling constant. Quadrupolar product $P_Q = C_Q (1 + \eta_Q^2/3)^{1/2}$ can be estimated from the frequency difference between CT and the center band of ST₁. In the case of I = 5/2, the CT and the center band of ST₁ are preferred since ST₂ line-width is broader than the other two transition. However, sometimes CT and center band ST₁ may not be resolved. This prevents the accurate determination of ST₁ shift. They resolved this problem by measuring spinning sideband of ST₁.

1.6.3. More advanced 2D-HETCOR method

MQ-HETCOR

It has been shown by several groups that CP-HETCOR can be coupled with the MQMAS experiment.[72] Numerous applications of the so-called MQ-HETCOR have been published, many of them related to the characterization of the aluminophosphate molecular sieves. The 3Q-HETCOR spectrum exhibits a better resolution in the ²⁷Al dimension compared to the ²⁷Al-³¹P CP HETCOR spectrum.

Alternatively, the MQMAS block was combined with a *J*-RINEPT sequence in order to avoid the complexity of spin locking the quadrupolar nucleus.[73]

The MQMAS block has also been combined with *D*-RINEPT, for which the coherence of quadrupolar isotope is transferred to that of spin-1/2 nuclei via D_{IS} couplings reintroduced by the application of D_{IS} recoupling sequences, such as R³, to the spin-1/2 isotope during the defocusing and refocusing delays of the RINEPT block (**Fig.1.15**).[34]



Fig.1.15. Schematic diagram of MQ-D-RINEPT sequence

HMQC-ST

HMQC and HSQC sequences are fundamentally symmetrical with respect to time, and it is, therefore, difficult to introduce an unsymmetrical MQMAS or STMAS second order quadrupolar filter. For spin-3/2, this limitation can nevertheless be overcome by inserting during the t_1 period a symmetrical t_1 STMAS sequence on the non-observed channel [74]: $0Q \rightarrow \pm 1Q (n\tau_R/18) \rightarrow \pm 2Q (8n\tau_R/9) \rightarrow \pm 1Q (n\tau_R/18) \rightarrow \pm 0Q$ (Fig.1.16). This symmetrical t_1 -split STMAS sequence was also used in STARTMAS experiment.[75]





Fig.1.16. Schematic diagram of HMQC-ST sequence.

PT J/D-HMQC

Q. Wang et al. have shown recently that for *J*- or *D*-HMQC experiments indirectly detecting half-integer spin quadrupolar nuclei, the population transfer can be accelerated by manipulating their satellite transition (**Fig.1.17**).[76] Such approach is notably useful to enhance the sensitivity of ²⁷Al-¹⁷O *J*-HMQC experiments.



Fig.1.17. Schematic diagram of PT *J/D*-HMQC sequence.

1.7. Objectives of the thesis

We have reviewed at solid-state NMR method for quadrupolar nuclei, including highresolution techniques, methods to enhance sensitivity as well as 2D HETCOR experiments. In the past, these techniques were only used by the experts, but today they have more and more often used for structural analysis of materials. In recent years, many improvements of these methods have been reported. In this thesis, we aim to further improve these methods. A disadvantage of these methods is often the lack of sensitivity. In recent years the sensitivity issue has been partially improved by the development of high field Dynamic Nuclear Polarization (DNP). Nevertheless, DNP is not a universal sensitivity improvement method since it requires the impregnation of radical solution to the sample and the use of specific equipment. In particular, DNP is difficult to apply for bulk samples, such as inorganic glass and crystals since it is impossible to impregnate radical solution.

However, high resolution methods such as MQMAS and STMAS that analyze these materials are low sensitivity, and also for 2D HETCOR methods, there are systems that cannot be applied owing to low sensitivity problem at present. For these methods, the improvement in this thesis are two points of interest.

In Chapter 2, we show how to analyze Gallium Selenide material which was difficult for MQ or STMAS and HETCOR experiment because of low sensitivity. Specifically, the pulse sequence of STMAS and various HETCOR method will be developed by adding the CPMG acquisition and population transfer irradiation.

Chapter 3 presents a new *D*-HMQC sequence with γ encoded recoupling, which is experimentally demonstrated to acquire ²⁷Al-³¹P 2D correlation on aluminophosphate material. As reviewed in section 1.5 and 1.6, R³ has low sensitivity due to poor robustness to rfinhomogeneity and is not used much in practice. Therefore, we investigated symmetry-based γ encoded recoupling techniques, which must be more robust to rf inhomogeneity than R³. Nevertheless, these methods should benefit from good robust to MAS fluctuations, thus limiting the magnitude of t_1 noise.

1.8. References

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Chapter 2: ⁷¹Ga-⁷⁷Se connectivities and proximities in gallium selenide crystal and glass probed by solid-state NMR

2.1. Introduction

Chalcogenide glasses are technologically important materials that can be suitably designed to exhibit many interesting physical properties including high transparency in the infrared range, low phonon energy, high optical nonlinearity, large photo-sensitivity, and high ionic conductivity.^[1–7] Beyond the usual systems based on Ge-Sb-Se or Ge-As-Se moieties, one of the pseudo-binary systems that display glass-forming ability over a significant composition range is Ga₂Se₃-GeSe₂.[8] Previous studies using Raman, X-ray photo-electron (XPS), extended X-ray absorption fine-structure (EXAFS), as well as ⁷⁷Se and ⁷¹Ga solid-state NMR (SS-NMR) spectroscopies, have shown that the structure of these gallium and germanium selenide glasses (denoted GGS hereafter) is composed predominantly of a network of cornersharing (CS) GaSe₄ and/or GeSe₄ tetrahedra and a small fraction of edge-shared (ES) GaSe₄ and/or GeSe₄ tetrahedra, in which the Ga, Ge, and Se atoms are covalently bonded to 4, 4, and 2 neighboring atoms, respectively. [9–13] The tetra-coordinated Ga and Ge sites as well as the di-coordinated Se ones are denoted Ga^{IV}, Ge^{IV} and Se^{II} hereafter. XPS and ⁷¹Ga SS-NMR spectroscopy have demonstrated that the addition of Ga₂Se₃ increases the deficiency in Se and leads to the formation of Ge-Ge bonds and ₃(Se^{II})-Ge-Ge-(Se^{II})₃ units, which are distributed in such way that any clustering of these units is avoided. [11,12] Furthermore, Raman spectroscopy and ⁷⁷Se SS-NMR studies, including two-dimensional (2D) ⁷⁷Se MATPASS/CPMG (Magic-Angle Turning-Phase Adjusted Spinning Sidebands with Carr-Purcell-Meiboon-Gill detection) experiments, have shown the formation of tri-coordinated Se atoms (Se^{III}) in GGS glasses with high content of Ga_2Se_3 (> 25 % mol).[12,13] The formation of these sites provides another mechanism to accommodate the deficiency in Se atoms. These Se^{III} atoms mainly replace the Se^{II} ones in the CS GaSe₄ and/or GeSe₄ tetrahedra.

As mentioned above, SS-NMR is a precious tool to characterize the local environment of atoms in GGS glasses. ⁷⁷Se isotope possesses a nuclear spin of 1/2, a gyromagnetic ratio similar to that of ²⁹Si nucleus ($\gamma_{77Se} \approx 0.96\gamma_{29Si} \approx 0.76\gamma_{13C}$) and a low natural abundance, $NA_{77Se} \approx 7.63$ %.[14] As ²⁹Si nuclei, ⁷⁷Se isotope exhibits long longitudinal relaxation times, T_1 , in solids. Furthermore, ⁷⁷Se NMR resonances are often broad, notably for glasses. Such broadening further reduces the sensitivity since the total integrated intensity is spread over a broad spectral width. Ga element has two stable NMR-active isotopes, ⁶⁹Ga and ⁷¹Ga, both with spin-3/2. ⁶⁹Ga

is more abundant than ⁷¹Ga (*NA*_{69Ga} \approx 60.4 % and *NA*_{71Ga} \approx 39.6 %), but the latter possesses higher gyromagnetic ratio ($\gamma_{69Ga} \approx 0.96\gamma_{13C}$ and $\gamma_{71Ga} \approx 1.22\gamma_{13C}$) and smaller quadrupole moment ($Q_{69Ga} = 17.1$ and $Q_{71Ga} = 10.7$ fm²). Therefore, ⁷¹Ga NMR experiments are more sensitive than ⁶⁹Ga ones. Nevertheless, even for ⁷¹Ga isotope, the quadrupole interaction broadens the NMR resonance over hundreds of kHz and the detection of these broad powder patterns is often challenging. Finally, the detection of ⁷³Ge nuclei by SS-NMR spectroscopy remains extremely challenging owing to the unfavorable properties of this isotope: low gyromagnetic ratio ($\gamma_{73Ge} \approx 0.14\gamma_{13C}$), low natural abundance (*NA*_{73Ge} \approx 7.76%) and large quadrupole moment ($Q_{73Ge} = -19.6$ fm²). Nevertheless, ⁷³Ge SS-NMR spectra of germanium selenide glasses have been reported.[15]

A major limitation of this study is the lack of resolution of 1D NMR spectra of GGS glasses since the resonances are broaden by the distribution of local environments as well as the anisotropic interactions, such as Chemical Shift Anisotropy (CSA) for ⁷⁷Se nuclei and quadrupole interaction for ⁷¹Ga and ⁷³Ge isotopes. Recently, 2D ⁷⁷Se CPMG experiments have allowed the measurement of one-bond *J*-coupling between ⁷⁷Se nuclei in arsenic selenide glasses.[16] Furthermore, it has been shown that the 2D MATPASS/CPMG sequence can improve the resolution of ⁷⁷Se signals for germanium selenide and GGS glasses by separating the isotropic chemical shift and the CSA in two distinct dimensions.[13,17] Nevertheless, to the best of our knowledge, the *J*-couplings between ⁷⁷Se and ⁷¹Ga nuclei have not been measured so far. Similarly, neither through-bond nor through-space ⁷⁷Se-⁷¹Ga hetero-nuclear correlation (*J*-HETCOR and *D*-HETCOR, respectively) 2D spectrum has been reported hitherto.

In this article, we introduce 2D ⁷⁷Se-⁷¹Ga *J*-HETCOR and *D*-HETCOR experiments. These sequences are first tested on β -Ga₂Se₃ crystalline sample. Using high-magnetic field (21.1 T) and high Magic-Angle Spinning (MAS) frequency, $v_R = 62.5$ kHz, we observe for this sample, two distinct ⁷¹Ga NMR signals, a narrow peak, accounting for 12 % of the total intensity, and a broad one. The narrow peak is assigned to Quenched phase in β -Ga₂Se₃ crystal. Previous SS-NMR studies at lower field and MAS frequency have only reported the observation of the narrow peak.[12] We also report high-resolution ⁷¹Ga 2D spectrum of β -Ga₂Se₃ acquired by introducing Satellite Transition MAS (STMAS) experiment [18,19] using quadrupolar CPMG (QCPMG) detection [20] at 21.1 T and $v_R = 62.5$ kHz. The 2D ⁷¹Ga STMAS-QCPMG spectrum allows separating the NMR signals of the Quenched phase and Annealed phase, but not those of the two Ga sites in Annealed phase.[21]

The 2D ⁷⁷Se-⁷¹Ga through-bond spectra are acquired by introducing (i) the Refocused Insensitive Nuclei Enhanced by Polarization Transfer (*J*-RINEPT) experiment [22] with ⁷¹Ga excitation and ⁷⁷Se CPMG detection [16], called ⁷⁷Se-{ 71 Ga}, as well as (ii) the Hetero-nuclear Multiple-Quantum Correlation (*J*-HMQC) experiment $\begin{bmatrix} 23 \end{bmatrix}$ with ⁷¹Ga excitation and QCPMG detection, the ⁷⁷Se signal being indirectly detected, called ⁷¹Ga-{⁷⁷Se}. Both ⁷⁷Se-{⁷¹Ga} J-RINEPT-CPMG and ⁷¹Ga-{⁷⁷Se} J-HMQC-QCPMG 2D spectra show the expected correlation between the broad ⁷¹Ga signal of β -Ga₂Se₃ and the ⁷⁷Se^{II} and ⁷⁷Se^{III} signals. Furthermore, those spectra also exhibit a cross-peak between the ⁷¹Ga narrow signal of the Quenched phase and the ⁷⁷Se^{III} signals. Such observation indicates that the Quenched phase is composed of Se^{III} sites. In addition, by fitting the evolution of the 77 Se-{ 71 Ga} J-RINEPT-CPMG and 71 Ga-{ 77 Se} J-HMQC-QCPMG signals as function of the defocusing and/or refocusing delays, τ and τ ' (see **Fig.2.1**), we measure for the first time the one-bond and three-bonds J-couplings, denoted ${}^{1}J$ and ³*J*, respectively, between ⁷¹Ga isotope and ⁷⁷Se^{II} as well as ⁷⁷Se^{III} nuclei. The 2D ⁷⁷Se-⁷¹Ga through-space spectrum is acquired by introducing the ⁷¹Ga-{⁷⁷Se} dipolar-mediated HMQC experiment (*D*-HMQC) [24,25] with QCPMG detection. The ⁷¹Ga-⁷⁷Se dipolar couplings are reintroduced under MAS conditions by applying the Simultaneous Frequency and Amplitude Modulation (SFAM₁) recoupling [26-28] during the defocusing and refocusing delays. The sensitivity between through-space and through-bond correlation experiment is compared.

These 2D ⁷⁷Se-⁷¹Ga *J*- and *D*-HETCOR experiments are then applied to characterize the GGS glass $xGa_2Se_3-(1-x)$ GeSe₂ with x = 0.2 (denoted GGS_{0.2} hereafter). The GGS_x glass-ceramics are a good alternative to single-crystalline Ge and polycrystalline ZnSe materials for making lenses transparent in the IR range for thermal imaging applications. The GGS_{0.2} composition leads to a homogeneous and reproducible glass-ceramic using suitable heat treatment over its glass transition temperature. For this sample, the controlled nucleation rate is assumed to be due to a specific phenomenon of phase separation.[8] The same behavior has been observed as well in sulfide based glasses of the same composition, highlighting the important role of gallium during the nucleation process.[11,29] The obtained glass-ceramics present enhanced mechanical properties, while keeping an excellent transparency in the mid-infrared range. The ⁷⁷Se-⁷¹Ga *J*- and *D*-HETCOR 2D spectra permit to resolve and identify molecular units containing Ga and Se atoms in GGS_{0.2} glass. Furthermore, the evolution of ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG and ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG signals as function of the τ delay allows the estimate of the ¹*J*_{71Ga-77Se} couplings and indicates that the ⁷¹Ga-⁷⁷Se covalent bonds in GGS_{0.2} glass are similar to those of β -Ga₂Se₃.

2.2. Methods

2.2.1. NMR methods

2.2.1.1. Acquiring ⁷¹Ga 1D MAS spectra

As seen below, ⁷¹Ga isotope in β -Ga₂Se₃ crystal and GGS_{0.2} glass is subject to large quadrupole interactions. In order to improve the spectral resolution, ⁷¹Ga 1D spectra were acquired at high magnetic field, $B_0 = 21.1$ T, and high MAS frequency, $v_R = 62.5$ kHz, since for quadrupolar nuclei the resolution is proportional to $(B_0)^2$ and MAS can improve the spectral resolution by a factor of ca. 3 by partially averaging the second-order broadening, at least when the spinning sidebands are separated from the center-bands. As seen in **Fig.2.5(b)**, (d), the MAS averaged line-width of the central transition (CT) between energy levels $\pm 1/2$ of ⁷¹Ga nuclei extends over 60 kHz in β -Ga₂Se₃ crystal and GGS_{0.2} glass, and hence a high MAS frequency of $v_R \ge 60$ kHz is required.

2.2.1.2 CPMG and QCPMG.

As explained in the introduction, ⁷¹Ga and ⁷⁷Se spectra of GGS glasses exhibit wide powder patterns, which result in low sensitivity. Nevertheless, for these isotopes, the decay of the maximum of the echo signal for increasing spin echo delay is often much slower than that the Free-Induction Decay. Consequently, the sensitivity can be enhanced by acquiring multiple rotor-synchronized echoes in the form of the CPMG scheme for ⁷⁷Se nuclei [16] and QCPMG sequence for ⁷¹Ga one.[30]

2.2.1.3. ⁷¹Ga STMAS-QCPMG.

A high-resolution ⁷¹Ga spectrum was acquired by introducing the STMAS-QCPMG sequence. The STMAS method offers the advantage to be typically 2-8 times more sensitive than the Multiple-Quantum MAS (MQMAS) scheme. Another advantage of STMAS for the acquisition of high-resolution ⁷¹Ga spectra is that the sensitivity of this technique does not depend on the MAS frequency, and hence, STMAS-QCPMG spectra can be acquired at MAS frequency ($v_R \ge 60$ kHz) sufficiently high to separate the spinning sidebands from the centerbands. Conversely, for MQMAS, the sensitivity decreases with increasing MAS frequency.[**31**] The employed STMAS-QCPMG sequence is shown in **Fig.2.1**. A z-filter is used to produce pure absorption line-shapes.[**18**] Furthermore, the split- t_1 approach is used so that the isotropic spectrum results from a projection onto the F_1 dimension, without any shearing data treatment.[**19**] As ⁷¹Ga is a spin-3/2 isotope, the t_1 period is partitioned into two delays $t_1/9$ and $8t_1/9$. The CT-selective pulse separating the two parts converts the ±1Q single-quantum

coherences evolving during $t_1/9$ into $\pm 2Q$ double-quantum coherences evolving during $8t_1/9$. The coherence pathways are selected using phase cycling. The selection of 2Q coherences eliminates the undesired CT-CT diagonal ridge. QCPMG recycling was applied during the acquisition period, t_2 . The delay between the QCPMG π -pulses was long enough so that both echo and anti-echo signals could be detected without truncation. The quadrature along the indirect dimension was achieved using the States-TPPI procedure [32] by incrementing the phase of the initial $\pi/2$ -pulse.



Fig.2.1. Employed pulse sequence and coherence pathways diagram for 2D ⁷¹Ga split- t_1 amplitude-modulated *z*-filter STMAS-QCPMG experiment. The first and third pulses are applied with high rf-fields to excite and reconvert both CT and satellite transition (ST) of ⁷¹Ga nuclei, whereas the other pulses are applied with low rf-field so that they are CT selective.

2.2.1.4. ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG.

The ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG scheme is shown in **Fig.2.2(a)**. It derives from the *J*-RINEPT sequence [22] by applying the CPMG recycling of magnetization during the t_2 period. The initial selective $\pi/2$ -pulse excites the ⁷¹Ga CT magnetization, which is encoded by ⁷¹Ga isotropic chemical shifts and second-order quadrupolar couplings as well as $J_{71Ga-77Se}$ couplings during the t_1 period. During the defocusing period, τ , the simultaneous π -pulses on the ⁷¹Ga and ⁷⁷Se channels refocus the evolution under ⁷¹Ga isotropic shifts but not that under the $J_{71Ga-77Se}$ couplings and hence, the ⁷¹Ga in-phase CT with respect to ⁷⁷Se is converted into antiphase CT. The simultaneous $\pi/2$ -pulses on ⁷¹Ga and ⁷⁷Se channels convert this antiphase CT of ⁷¹Ga nuclei into antiphase ⁷⁷Se 1Q coherences. During the refocusing period, τ ', ⁷⁷Se isotropic shift is refocused and the antiphase ⁷⁷Se 1Q coherences evolve under ⁷¹Ga-⁷⁷Se *J*-couplings into inphase ⁷⁷Se magnetization. Thus, the refocusing period yields in phase multiplets, for which the intensities of the different components add constructively, and hence, enhance signal intensity since the different components of the multiplets overlap and the decay of ⁷⁷Se 1Q coherence during τ ' delay is slow.

2.2.1.5. ⁷¹Ga-{⁷⁷Se} *J*- or *D*-HMQC-QCPMG.

The ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG scheme is displayed in **Fig.2.2(b)**. The sequence is similar to the *J*-HMQC scheme,[23] but the QCPMG recycling of magnetization is employed during the t_2 period. During the defocusing delay, τ , the in-phase ⁷¹Ga CT evolves into antiphase one and is then converted into ⁷¹Ga-⁷⁷Se multiple-quantum coherences by the $\pi/2$ -pulse on ⁷⁷Se channel. These coherences are encoded by the ⁷⁷Se isotropic chemical shift before being converted back into anti-phase ⁷¹Ga CT by the second ⁷⁷Se $\pi/2$ -pulse. The ⁷¹Ga-{⁷⁷Se} *D*-HMQC-QCPMG sequence is similar to that shown in **Fig.2.2(b)**, but SFAM₁ recoupling is applied on the ⁷⁷Se channel during the two delays τ in order to refocus the evolution under $J_{71Ga-77Se}$ and J_{71Se} couplings, while reintroducing the ⁷¹Ga-⁷⁷Se dipolar couplings.

2.2.1.6. Measurement of *T*'_{2,71Ga} and *T*'_{2,77Se} time constants.

The T'_2 time constant characterizes the exponential decay of the maximum signal in spinecho experiments. As explained below, these time constants for ⁷¹Ga and ⁷⁷Se nuclei appear in the analytical expression of ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG and ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG experiments. Therefore, the independent measurement of these T'_2 values yields more accurate ⁷¹Ga-⁷⁷Se *J*-couplings by better constraining the fit of signals to the analytical expression. Here, the T'_{2,71Ga} constant was measured using a spin echo experiment with QCPMG detection (see **Fig.2.2(d)**). The $T'_{2,77Se}$ constants were determined using a spin echo experiment with CPMG detection. However, the sensitivity was improved by replacing the initial π /2-pulse by a ⁷¹Ga \rightarrow ⁷⁷Se *J*-RINEPT polarization transfer. Such transfer improves the sensitivity since the ⁷¹Ga gyromagnetic ratio is higher than that of ⁷⁷Se isotope and the longitudinal relaxation times of ⁷¹Ga nuclei (about 0.6 s for the investigated samples) are much shorter than those of ⁷⁷Se isotopes (larger than 100 s).





Fig.2.2. (a,b) Employed 2D ⁷¹Ga-⁷⁷Se through-bond correlation sequences: (a) ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG and (b) ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG. (c,d) Sequences used to measure the (c) ⁷⁷Se and (d) ⁷¹Ga *T*'₂ values. All sequences employ ⁷¹Ga excitation in order to improve the sensitivity since the longitudinal relaxation of ⁷¹Ga nuclei is much faster than that of ⁷⁷Se. All pulses applied to the ⁷¹Ga nuclei in these sequences selectively excite the CT.

2.2.2. Analytical expression of ⁷⁷Se-{⁷¹Ga} J-RINEPT and ⁷¹Ga-{⁷⁷Se} J-HMQC

The analytical expressions of ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG and ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG transfer efficiencies are required for the determination of $J_{71Ga-77Se}$ couplings by the fit of the evolution of their experimental signals as function of the τ and τ ' delays.

The global transfer efficiencies are the sum of those for the different spin systems in the sample, weighted by their abundance since the analytical expression of the transfer efficiency depends on the number of ⁷¹Ga and ⁷⁷Se nuclei in the spin system. As seen below, the fit of the evolution of *J*-RINEPT and *J*-HMQC signals as function of the τ and τ ' delays only allows the determination of a limited number of adjustable parameters. In order to reduce this number, we assumed that the *J*-couplings through a given number of bonds between ⁷¹Ga isotope and ⁷⁷Se nucleus occupying both sites, Se^{II} or Se^{III}, are all identical. Such assumption is a simplification since for instance, the ³*J*_{71Ga-77Se} coupling through the ⁷¹Ga-Se-Ga-⁷⁷Se three bonds must depend a priori on the torsion angle around the Se-Ga middle bond. Furthermore, for β -Ga₂Se₃, the ¹*J*_{71Ga-77Se} couplings were not sufficient to describe the evolution of the *J*-RINEPT and *J*-HMQC signals and the contribution of coherence transfer through ³*J*_{71Ga-77Se} couplings had to be included.

Using the above assumption, it can be shown that the transfer efficiency, f, of ⁷¹Ga-{⁷⁷Se} J-HMQC-QCPMG scheme is given by

$$f(\tau) = \begin{cases} m \left[\sum_{p=1}^{m} p \alpha_p^m s_{1J}^2 c_{1J}^{2p-2} \left(\alpha_0^n + \sum_{q=1}^{n} q \alpha_q^n c_{3J}^{2q} \right) \right] \\ + n \left[\sum_{q=1}^{n} q \alpha_q^n s_{3J}^2 c_{3J}^{2q-2} \left(\alpha_0^m + \sum_{p=1}^{m} p \alpha_p^m c_{1J}^{2p} \right) \right] \end{cases} \exp \left(-\frac{2\tau}{T'_{2,71Ga}} \right)$$
(2.1)

where *m* and *n* denotes the numbers of Se atoms connected to one ⁷¹Ga nucleus by one- and three-bonds, respectively, α_r^l with l = m or *n* and r = p or *q* denotes the fraction of r^{77} Se nuclei among the *l* Se atoms connected to the Ga atom, $c_{xJ}^y = \cos^y(\pi^x J\tau)$ and $s_{xJ}^y = \sin^y(\pi^x J\tau)$. In Eq.(2.1), the first and second terms correspond to ¹J and ³J transfers, respectively. The α_r^l fraction are given by

$$\alpha_r^l = C_r^l (1 - NA_{77Se})^{l-r} . NA_{77Se}^r$$
(2.2)

where C_r^l denotes the *r*-combination of a set *l*. In β -Ga₂Se₃, according to the crystal structure [21], we have m = 4 and n = 18.

Similarly, it can be shown that the transfer efficiency of 77 Se-{ 71 Ga} J-RINEPT-CPMG scheme is given by

$$\begin{split} f(\tau,\tau') &= \\ \left\{ m \left[\sum_{p=1}^{m} p \alpha_p^m \left[m' \sum_{p'=1}^{m'} p' \alpha'_{p'}^{m'} s_{1J} s_{1J}' c_{1J}^{p-1} c'_{1J}^{p'-1} \left(\alpha_0^n + \right. \right. \right. \\ \left. \sum_{q=1}^{n} q \alpha_q^n c_{3J}^q \right) \left(\alpha'_0^{n'} + \sum_{q'=1}^{n'} q' \alpha'_{q'}^{n'} c_{3J}^{q'} \right) \right] \right] + \\ n \left[\sum_{q=1}^{n} q \alpha_q^n \left[n' \sum_{q'=1}^{n'} q' \alpha'_{q'}^{n'} s_{3J} s_{3J}' c_{3J}^{q-1} c'_{3J}^{q'-1} \left(\alpha_0^m + \right. \right. \right. \\ \left. \sum_{p=1}^{m} p \alpha_p^m c_{1J}^p \right) \left(\alpha'_0^{m'} + \sum_{p'=1}^{m'} p' \alpha'_{p'}^{m'} c_{1J}^{p'} \right) \right] \right\} \exp \left(- \frac{\tau}{T'_{2,71Ga}} - \frac{\tau'}{T'_{2,77Se}} \right) \end{split}$$

$$(2.3)$$

where *m*' and *n*' denotes the numbers of Ga atoms connected to a given ⁷¹Se site by one- and three-bonds, respectively. In β -Ga₂Se₃, we have m' = 2 and n' = 11 for Se^{II} sites, m' = 3 and n' = 13 for Se^{III,1} sites and m' = 3 and n' = 11 for Se^{III,2} sites. As the ⁷⁷Se NMR signals of the two Se^{III} sites are not resolved (see **Fig.2.5**) and the unit cell contains identical number of Se^{III,1} and Se^{III,2} sites, we consider m' = 3 and n' = 12 for Se^{III} sites hereafter. The α'_r^l fraction are given by

$$\alpha'_{r}^{l} = C_{r}^{l} (1 - NA_{71Ga})^{l-r} NA_{71Ga}^{r}$$
(2.4)

2.3. Experimental section

2.3.1. Synthesis of crystalline β-Ga₂Se₃

β-Ga₂Se₃ crystals were synthesized according to the already published process.[3,16] High purity raw elements Ga (5N purity), and Se (N purity) were weighted (5 g), transferred into a 9 mm diameter silica tube, and sealed under a vacuum of 10^{-3} Pa. The ampoule was heated (+1.5 °C/min) up to 1100 °C and maintained at this temperature for 10 hours. The temperature was then decreased down to 950 °C and maintained for 12 hours in order to promote the crystallization of the Ga₂Se₃ compound. Then, the temperature was decreased with a ramp of -0.5 °C/min down to 880 °C. After 30 minutes at this temperature, the solid was quenched into water, then annealed at 550 °C for 840 hours, and finally removed out from the silica tube. The GGS_{0.2} glass has been prepared following the classical melt-quenching way used for making infrared chalcogenide glasses. Further details have been given previously.[8]

2.3.2. Solid-state NMR

NMR spectra were recorded on Bruker BioSpin spectrometers operating either at $B_0 = 9.4$ T (wide-bore magnet equipped with Avance-II console) or 21.1 T (narrow-bore magnet equipped with Avance-IV console). Samples were spun either at $v_R = 20$ kHz using 3.2 mm triple-resonance HXY probes for the 9.4 T magnet or at $v_R = 62.5$ kHz using 1.3 mm double-resonance HX probe for the 21.1 T magnet. The ⁷¹Ga and ⁷⁷Se isotropic chemical shifts were referenced to the resonance (0 ppm) of saturated aqueous solutions of Ga(NO₃)₃ and H₂SeO₃.

The 1D direct excitation ⁷¹Ga MAS spectra were acquired using spin echo experiments, in which the refocusing pulse is bracketed by T_E delays. All other spectra were acquired using CPMG recycling in the case of ⁷⁷Se detection or QCPMG one in the case of ⁷¹Ga detection. These schemes enhance the sensitivity by collecting a large number of echoes, *NE*. In the case of β -Ga₂Se₃ 1D spectra, we have always used trains of π -pulses for the CPMG and QCPMG parts. However, ⁷⁷Se and ⁷¹Ga spectra of GGS_{0.2} are ca. twice broader than those of β -Ga₂Se₃. Therefore, (i) we have then used the maximum rf-fields available with our probes, and (ii) in the case of 1D spectra we have used trains of π /2-pulses for the CPMG/QCPMG recycling to broaden the excitation rf-profiles. Indeed, it has been recently shown that ' π -pulses only provide a maximum intensity at the transmitter frequency' and that one observes 'only a slight loss in intensity at the transmitter frequency. (i) and the transmitter frequency. (ii) and the transmitter frequency. (iii) and (i

nucleus. Therefore, the rf-profile cannot be broadened by the use of $\pi/2$ pulses in the train of echoes, and hence we used π -pulses in these trains to maximize the S/N. A delay of 2ms rotorperiods between the CPMG or QCPMG pulses was used (**Fig.2.2**), leading to a total echo-time of $T_E = 2mT_R$. The amount of signal was maximized by using a minimal phase cycling of the (Q)CPMG scheme, i.e. a fixed phase of the pulses in the (Q)CPMG train. The phase of the Q)CPMG pulses was shifted by 90° with respect to the preceding 90° pulse. This limited phase cycling avoids the destructive interferences between the two coherence pathways, and all possible coherence transfer pathways (i.e., 0Q and ±1Q) form echoes simultaneously if the sequence is correctly rotor-synchronized.[33] After the CPMG/QCPMG recycling, all echoes can be added on top of each other's with data processing and the spectra are then represented in a classical way, without any spikelet.

For split- t_1 STMAS experiment, the lengths and the radiofrequency (rf) nutation frequencies were equal to 1.25/0.8 µs and 215 kHz, respectively, whereas 155 kHz was used for the CT selective pulse.

 $T'_{2,71Ga}$ measurements were recorded with a spin-echo-QCPMG sequence (**Fig.2.2(d**)). $T'_{2,77Se}$ measurements were performed with the J-RINEPT spin-echo-CPMG sequence as mentioned above (**Fig.2.2(c**)). In both cases, the spin-echo block was phase-cycled with four steps and always rotor synchronized.

For β -Ga₂Se₃, the separate evolutions for Se^{II} and Se^{III} species of the *J*-HMQC-QCPMG signal as function of τ delay were acquired by recording twenty-nine ⁷¹Ga-{⁷⁷Se} 2D spectra. The pulse programs are given in the Appendix. All experimental specifications corresponding to spectra are given in **Table.2.1**.

Fig	B_0	ν_{R}	V1,77Se	V1,71Ga	CPMG	$T_{\rm E}$	NS	NE	$ au_{RD}$	Texp	τ
	/T	/kHz	/kHz	/kHz	Tilt angle	/ms			/s	/h	/ms
2.5a	9.4	20	40	Х	180	1	256	200	300	21.6	Х
2.5b	21.1	62.5	Х	155	90	0.48	102400	Х	0.5	14.2	X
2.5c	9.4	20	63	Х	90	0.2	72	1200	1200	24	Х
2.5d	21.1	62.5	Х	155	90	0.48	102400	Х	0.5	14.2	Х
2.6a,b	9.4	20	40	95	π	0.3	128	800	1.2	0.73	0.8
2.6c,d	9.4	20	Х	95	π	0.2	64	600	1.0	0.57	Х
2.7	21.1	62.5	Х	215(1 st ,3 rd)	180	1.09	3072	20	0.6	14.3	X
				155 others							
2.8a	9.4	20	Х	25	π	0.8	256	200	1	0.07	Х
2.8b	9.4	20	Х	95	π/2	0.8	256	200	1	0.07	Х
2.9a-f	9.4	20	40	95	180	0.3	128	800	1.2	5.6	Х
2.9g,h	9.4	20	40	95	180	0.1	128	600	1	17	Х
2.10a-d	9.4	20	40	95	π	0.3	128	800	1.2	5.6	Х
2.10e,f	9.4	20	40	95	π	0.1	128	600	1	17	Х
2.11a	9.4	20	40	95	180	0.4	128	800	1	4.6	0.7
2.11b	9.4	20	40	95	180	0.1	128	600	1	1.2	0.8
2.11c	9.4	20	40	95	180	0.1	256	600	1	2.3	4
2.13	9.4	20	Х	95	π/2	0.5	4096	100	1	1.13	X
2.14a	9.4	20	Х	95	π	0.1	64	800	1.0	0.44	X
2.14b	9.4	20	63	95	π	0.2	512	1200	1.2	2.73	0.8
2.15a	9.4	20	40	95	180	0.3	128	800	1	4.6	Х
			63			0.2	1024	1200	1.2	25.5	
2.15b	9.4	20	40	95	180	0.1	32	600	1	1.4	Х
			63				1024			20.6	
2.16	9.4	20	63	95	π	0.4	30000	500	1.2	10	0.8
2.17a	9.4	20	63	95	180	0.3	2048	800	1	9.9	0.8
2.17b	9.4	20	63	95	180	0.1	512	500	1	10.7	0.8
2.17c	9.4	20	63	95	180	0.1	1024	500	1	21.5	3

Table.2.1. Experimental parameters for the spectra

2.4. Results and discussion

2.4.1. Crystalline β-Ga₂Se₃

The crystal structure of β -Ga₂Se₃ is composed of Annealed phase and Quenched phase according to this reference.[34] X-ray diffraction data of β -Ga₂Se₃ is shown in **Fig.2.3**.

For Annealed phase, the crystal system is the monoclinic (space group: B11b). There are two types of 4 fold coordinated Ga sites which are called Ga^{IV,2} and Ga^{IV,2}. There are one 2 fold coordinated Se (Se^{II}) and two types of 3 fold coordinated Se site (Se^{III,1} and Se^{III,2}).

In Gallium environment, Ga^{IV,1} is connected to Se^{II}, Se^{III,1} and two Se^{III,2}. On the other hand, Ga^{IV,2} is connected to Se^{II}, two Se^{III,1} and Se^{III,2} Ga^{IV,1} and Ga^{IV,2} possess similar symmetry environment. In Selenium environment, Se^{II} is connected to Ga^{IV,1} and Ga^{IV,2}. Se^{III,1} is connected to Ga^{IV,1} and two Ga^{IV,2}. Se^{III,2} is connected to two Ga^{IV,1} and Ga^{IV,2}. Se^{III,1} and Se^{III,2} possess similar symmetry environment. (see **Fig.2.4**).

In addition, $Se^{II} - Ga^{IV}$ bond length is shorter than $Se^{III} - Ga^{IV}$ bond length. This different bond length lead to distort the Ga tetrahedral environment. Each bond length value is represented in **Table.2.2**.

Ga vacancy get organized. It can be described as a ABCA'B'C' stacking (**Fig.2.5**). This ordering has effect on the cell

For Quenched phase, the crystal system is the cubic (Space group: F-43m) where all Ga^{IV} sites form regular tetrahedron with four Se. All Se are composed of Se^{III}. All Se^{III} – Ga^{IV} bond length is 2.358 (Å). Ga vacancy is random where Ga occupancy is 0.666 in the structure.



Fig.2.3. X-ray diffraction data of β -Ga₂Se₃.

Table.2.2. Each bond length of $Se^{II} - Ga^{IV}$ in Annealed phase for β -Ga₂Se₃. Each value is adopted from [34].

Se ^{II} – Ga ^{IV}	bond length (Å)	$Se^{III} - Ga^{IV}$ bond length (Å)			
$Se^{II} - Ga^{IV,1}$	2.316	$\mathrm{Se}^{\mathrm{III},1}-\mathrm{Ga}^{\mathrm{IV},1}$	2.466		
$Se^{II} - Ga^{IV,2}$	2.338	$Se^{III,1} - Ga^{IV,2}$	2.464		
		$\mathrm{Se}^{\mathrm{III},1}-\mathrm{Ga}^{\mathrm{IV},2}$	2.468		
		$\mathrm{Se}^{\mathrm{III},2}-\mathrm{Ga}^{\mathrm{IV},1}$	2.422		
		$\mathrm{Se}^{\mathrm{III},2}-\mathrm{Ga}^{\mathrm{IV},1}$	2.477		
		$\mathrm{Se}^{\mathrm{III},2}-\mathrm{Ga}^{\mathrm{IV},2}$	2.454		



Fig.2.4. Representation of the three distinct selenium sites in Annealed phase of β -Ga₂Se₃.



Fig.2.5. Organization of Ga vacancy in Annealed phase of β-Ga₂Se₃. Adopted from [34]

2.4.1.1. 1D MAS spectra

⁷⁷Se. The ⁷⁷Se 1D MAS spectrum is shown in **Fig.2.6(a)**. The Se^{II} and Se^{III} resonances are resolved but not those of crystallographically inequivalent Se^{III,1} and Se^{III,2} sites (see **Fig.2.4**). A quantitative measurement of the relative amounts of the different selenium sites is precluded using a CPMG sequence since the T'_2 values can differ between the Se^{II} and Se^{III} environments. Here, the T'_2 values of ⁷⁷Se^{II} and ⁷⁷Se^{III} nuclei were measured using *J*-RINEPT-CPMG sequence (**Fig.2.2(c)**). The attenuation of the ⁷⁷Se signals versus the echo-delay τ_e is shown in **Fig.2.7(a,b)** and it provides $T'_{2,Se} = 21$ and 24 ms for Se^{III} and Se^{III}, respectively (**Table.2.3**).



Fig.2.6. 1D MAS spectra of (a,b) β -Ga₂Se₃ and (c,d) GGS_{0.2}. (a,c) ⁷⁷Se CPMG spectra with B_0 = 9.4 T and ν_R = 20 kHz. (b,d) ⁷¹Ga QCPMG spin echo spectra with B_0 = 21.1 T and ν_R = 62.5 kHz.

⁷¹Ga. The MAS spectrum was recorded with a spin-echo at 21.1 T and $v_R = 62.5$ kHz. The spectrum shows two signals: one narrow resonance on the top of a broad 2nd-order quadrupolar spectrum with only one spinning sideband of the broad resonance on each side (**Fig.2.6(b**)). The sharp signal is probably due to Quenched phase, whereas the broad resonance is attributed to both Ga^{IV,1} and Ga^{IV,2} species of Annealed phase since these species has distorted tetrahedron.

In an attempt to disentangle these two broad contributions, we have recorded at 21.1 T and $v_R = 62.5$ kHz a 2D high-resolution ⁷¹Ga STMAS spectrum with a full-echo detection and QCPMG recycling. The spectrum shown in **Fig.2.8** displays two different contributions: one presenting a small C_Q value with a large distribution of isotropic chemical shift, and another one exhibiting a large C_Q value. These two signals correspond to the narrow and broad

resonances in **Fig.2.6(b)**, respectively. The isotropic chemical shifts of both narrow and broad resonances correspond to GaSe₄ environments. The smaller C_Q value for the narrow resonance with respect to the broad one indicates that the GaSe₄ environments are more symmetrical in the Quenched phase than in the Annealed phase of β -Ga₂Se₃ crystal. Unfortunately, the 2D STMAS spectrum does not permit us to resolve the Ga^{IV,1} and Ga^{IV,2} sites in Annealed phase of β -Ga₂Se₃ crystal, and the 1D spectrum was thus fitted assuming only two species (one narrow and one broad) with the DMfit software.[**35**] Such fit (not shown) provided the relative amounts of the two sites and their quadrupolar parameters (Conc (%), C_Q (MHz), η_Q) \approx (88, 17.4, 0.5) and (12, 4.4, 0.3) for the broad and narrow resonances, respectively.

Whereas at $B_0 = 21.1$ T and $v_R = 62.5$ kHz, the sidebands are well resolved from the centerband in the 1D ⁷¹Ga spectrum, at $B_0 = 9.4$ T and $v_R = 20$ kHz, only the narrow resonance was detected for $v_{1,71Ga} = 25$ kHz (see **Fig.2.9(a)**) as well as a part of the broad signal for $v_{1,71Ga} =$ 95 kHz (see **Fig.2.9(b)**). The first spectrum is rather similar to the one already published.[12] These results highlight the need of high magnetic field and high MAS frequency for the acquisition of ⁷¹Ga MAS spectra. $T'_{2,71Ga}$ measurements were performed at 9.4 T with $v_R = 20$ kHz, and the evolutions are surprisingly identical for the narrow and broad resonances (**Fig.2.7(c,d)**, **Table.2.3**): $T'_{2,71Ga} = 5.7$ and 5.0 ms, respectively. It must be noted that those values are approximately four times smaller than the $T'_{2,77Se}$ ones (**Fig.2.7(a,b**), **Table.2.3**).



Fig.2.7. β -Ga₂Se₃: experimental decay of (a,b) ⁷⁷Se signals in *J*-RINEPT-spin-echo-CPMG experiment and of (c,d) ⁷¹Ga signals in spin-echo-QCPMG sequence as function of the spin echo delay. The red continuous curves correspond to the best fit of experimental data points to a decaying mono-exponential function with T'_2 = (a) 21, (b) 24, (c) 5.7, and (d) 5.0 ms.

	<i>T</i> ' ₂ /ms		
	β-Ga ₂ Se ₃	GGS _{0.2}	
Se ^{II}	21	18	
Se ^{III}	24	10	
Ga (Broad resonance)	5	8	
Ga (Narrow resonance)	5.7	0	

Table.2.3. Experimental T'_2 values of β -Ga₂Se₃ and GGS_{0.2}.



Fig.2.8. 2D ⁷¹Ga STMAS-QCPMG spectrum of β -Ga₂Se₃ recorded at $B_0 = 21.1$ T and $\nu_R = 62.5$ kHz.



Fig.2.9. 1D ⁷¹Ga QCPMG spectrum of β -Ga₂Se₃ recorded at $B_0 = 9.4$ T and $v_R = 20$ kHz using (a) $v_{1,71Ga} = 25$ or (b) 95 kHz.
2.4.1.2. *J*-RINEPT and *J*-HMQC build-up curves

J-RINEPT

The ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG build-up curves of Se^{II} and Se^{III} signals for β -Ga₂Se₃ are shown in **Fig.2.10**(a-f). They were obtained by acquiring 1D ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG spectra with $t_1 = 0$. When $\tau = \tau'$ (**Fig.2.10**(a,b)), maximum transfer is achieved for $\tau = \tau' \approx 0.7$ ms. These values suggest that the one-bond ¹*J*_{71Ga-77Se} couplings are much larger than 100 Hz. Therefore, it is possible to keep fixed a recoupling time (τ or τ') to this optimum value and to vary the other one (τ' or τ respectively) (**Fig.2.10**(c-f) and **Fig.2.11**(a-d)). The experimental points are normalized with respect to the maximum intensity observed with the Se^{III} site. The Se^{II} signal maximum intensities are always equal to ca. 0.40 that for Se^{III}. This value is smaller than that (0.5) predicted from the crystal structure of Annealed phase, which contains two Se^{III} sites for one Se^{II} site. This may be due to the shorter T'_2 , value for ⁷⁷Se^{III} nuclei with respect to ⁷⁷Se^{III} ones (**Fig.2.7(a,b)** and **Table.2.3**).

For the fit of the ⁷⁷Se-{⁷¹Ga} J-RINEPT build-up curves to Eq. (2.3), we used the T'_2 values of **Table.2.3** and then the only adjustable parameters in Eq.(2.3) are ${}^{1}J_{71\text{Ga}-77\text{Se}}$ and ${}^{3}J_{71\text{Ga}-77\text{Se}}$ values. One additional parameter was the intensity of the signal. The best fits are displayed in Fig.2.10 as continuous red curves. The best fit ${}^{1}J_{71\text{Ga-77Se}}$ and ${}^{3}J_{71\text{Ga-77Se}}$ values as well as the ratio of the signal intensities of Se^{II} and Se^{III} sites, I^{II}/I^{III} , are given in **Table.2.4**. As seen in that table and **Table.2.4**, we obtained similar *J*-coupling values and I^{II}/I^{III} ratios from the fit of buildup curves with $\tau = \tau'$, $\tau' = 0.7$ ms and $\tau = 0.7$ ms. The scalar couplings with the first neighbors are slightly larger for ⁷⁷Se^{II} nuclei with respect to Se^{III} ones ${}^{1}J_{71Ga-77SeII} \approx 760 \pm 30$ Hz and ${}^{1}J_{71Ga-77SEI} \approx 760 \pm 30$ Hz and $_{77\text{SeIII}} \approx 530 \pm 20$ Hz. This result is consistent with the shorter Se^{II}-Ga distances with respect to Se^{III}-Ga ones, as seen in the crystal structure. [36] In addition, ${}^{3}J_{71Ga-77Se}$ couplings are much smaller than with the ${}^{1}J({}^{71}\text{Ga}-{}^{77}\text{Se})$ ones: ${}^{3}J({}^{71}\text{Ga}-{}^{77}\text{Se}) \approx 11 \pm 5$ and 5 ± 1 Hz, for Se^{II} and Se^{III} sites, respectively. I^{II}/I^{III} ratios are slightly smaller than the ratio between the number of Se^{II} and Se^{III} sites in the crystal structure, probably owing to the shorter T'_2 value for ⁷⁷Se^{II} nuclei with respect to ⁷⁷Se^{III} ones, as mentioned above. The best fit curves deviate from the experimental build-up curves. Such deviation stems from (i) the contribution of the Quenched phase signal to these curves and (ii) the distribution of ${}^{1}J_{71\text{Ga-77Se}}$ and ${}^{3}J_{71\text{Ga-77Se}}$ coupling values, whereas we assumed identical J-coupling values through a given number of bonds.

J-HMQC

In 1D⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG experiments, the ⁷⁷Se signal is encoded in the indirect dimension, and hence 1D experiments do not allow the separation of Se^{II} and Se^{III} *J*-HMQC build-up curves. Such separation can only be achieved by recording a series of 2D experiments. These measurements require a long experimental time since many (29 here) 2D experiments had to be recorded. However, these 2D experiments permit us to separate the build-up curves for the broad ⁷¹Ga resonance of β -Ga₂Se₃ (see **Fig.2.10(g,h)**) and the narrow one corresponding to the Quenched (**Fig.2.11(e,f)**). The fit of these curves to Eq.(2.1) yields ¹*J*_{71Ga-77Se} couplings and *I*^{II}/*I*^{III} ratio similar to those determined from 1D ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG build-up curves (see **Table.2.5**). It must be noted that the ³*J*_{71Ga-77Se} values determined from the fit of 2D ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG build-up curves are much larger than those fitted from 1D ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG ones: 28 and 16 with respect to 11 and 5 Hz, for Se^{II} and Se^{III} sites, respectively.

The fit of the *J*-HMQC build-up curves for the ⁷¹Ga narrow resonance to Eq.(2.1) yields ${}^{1}J_{71\text{Ga-77Se}}$ couplings for Quenched phase (see **Table.2.5**), which are similar to those measured for the broad resonance (**Table.2.4**). Hence, the ⁷¹Ga-⁷⁷Se bonds are similar in Annealed phase and in Quenched phase. However, the I^{II}/I^{III} ratio is smaller for the Quenched phase than for Annealed phase. In the Annealed phase, the Ga sites are bonded to one Se^{II} and three Se^{III} sites. The narrow resonance must correspond to Ga atoms attached to four Se^{III} sites. Thus, the lower amount of Se^{II} sites in the Quenched phase is consistent with the more symmetrical environment of ⁷¹Ga nuclei, deduced from its lower C_Q value.



Fig.2.10. (a-f) Evolution of 1D ⁷⁷Se-{⁷¹Ga} J-RINEPT-CPMG Se^{II} (left) and Se^{III} (right) signals of β -Ga₂Se₃ versus either (a,b) $\tau = \tau$ ', (c,d) τ with $\tau' = 0.7$ ms, or (e,f) τ' with $\tau = 0.7$ ms. (g,h) Evolution of 2D ⁷¹Ga-{⁷⁷Se} J-HMQC-QCPMG signals of cross-peaks between the broad ⁷¹Ga resonance and (g) Se^{II} (left) or (h) Se^{III} (right) signals. The points are the experimental values, normalized to their maximum observed for Se^{III}, whereas the continuous curves correspond to the best fits with the parameters given in **Table.2.4**.

Table.2.4. Best fit ${}^{1}J({}^{71}\text{Ga}-{}^{77}\text{Se})$ and ${}^{3}J({}^{71}\text{Ga}-{}^{77}\text{Se})$ values and I^{II}/I^{III} ratio for the fit of the experimental curves of **Fig.2.10** to Eq.(2.3) for 1D ${}^{77}\text{Se}\{{}^{71}\text{Ga}\}$ *J*-RINEPT-CPMG build-up curves and to Eq.(2.1) for ${}^{71}\text{Ga}\{{}^{77}\text{Se}\}$ *J*-HMQC-QCPMG build-up curves.

Fig Se Method	$I^{\mathrm{II}}/I^{\mathrm{III}}$	${}^{1}J_{71\text{Ga-77Se}}$ /Hz	${}^{3}J_{71\text{Ga-77Se}}/\text{Hz}$
(a) Se^{II} <i>J</i> -RINEPT	0.32	734	18
(b) Se ^{III}		518	5
(c) Se^{II}	0.40	752	8
(d) Se ^{III}		528	5
(e) Se^{II}	0.36	744	7
(f) Se ^{III}		523	5
(g) Se ^{II} J-HMQC	0.35	801	28
(h) Se ^{III}		543	16



Fig.2.11. (a-d) Evolution of 1D ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG Se^{II} (left) and Se^{III} (right) signals of β -Ga₂Se₃ versus (a,b) τ with $\tau' = 10$ ms or (c,d) τ' with $\tau = 10$ ms. (e,f) Evolution versus τ of 2D ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG cross-peaks between the narrow ⁷¹Ga resonance and (g) Se^{II} (left) and (h) Se^{III} (right) signals. The points are the experimental values, normalized to their maximum observed for Se^{III}, whereas the continuous curves correspond to the best fits with the parameters given in **Table.2.5**.

Table.2.5. Best ${}^{1}J_{71\text{Ga-77Se}}$ and ${}^{3}J_{71\text{Ga-77Se}}$ values and $I^{\text{II}}/I^{\text{III}}$ ratio for the fit of the experimental curves of **Fig.2.11** to Eq.(2.3) for 1D ${}^{77}\text{Se-}\{{}^{71}\text{Ga}\}$ *J*-RINEPT-CPMG build-up curves and to Eq.(2.1) for ${}^{71}\text{Ga-}\{{}^{77}\text{Se}\}$ *J*-HMQC-QCPMG build-up curves.

Fig Se	Method	$I^{\mathrm{II}}/I^{\mathrm{III}}$	${}^{1}J_{71\text{Ga-77Se}}$ /Hz	$^{3}J_{71\text{Ga-77Se}}$ /Hz
(a) Se ^{II}	J-RINEPT	0.55	755	10
(b) Se ^{III}			565	8
(c) Se ^{II}		0.51	747	13
(d) Se ^{III}			551	6
(e) Se ^{II}	J-HMQC	0.11	773	22
(f) Se ^{III}			580	9

2.4.1.3. Comparison of the 2D J-RINEPT and D- or J-HMQC spectra

The 2D spectra of the ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG and ⁷¹Ga-{⁷⁷Se} *J*- and *D*-HMQC-QCPMG experiments are displayed in **Fig.2.12**. The ⁷⁷Se projections of these 2D spectra are shown in **Fig.2.13**. In agreement with the crystal structure of Annealed phase,[**21**], the 2D *J*-RINEPT and *J*-HMQC spectra show cross-peaks between the broad ⁷¹Ga resonance and both ⁷⁷Se^{II} and ⁷⁷Se^{III} signals, indicating that the Ga atoms are bonded to both Se^{II} and Se^{III} sites. The 2D *D*-HMQC spectrum allows the observation of the through-space proximities between Ga atom and both Se^{II} and Se^{III} sites. In the three 2D heteronuclear correlation spectra, the narrow ⁷¹Ga resonance assigned to the Quenched phase correlates mainly with the Se^{III} signal. This observation is consistent with the low *I*^{II}/*I*^{III} ratio determined from the fit of the build-up curves of the narrow resonance in 2D ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG spectra (see **Table.2.5**).



Fig.2.12. 2D spectra of β -Ga₂Se₃ at $B_0 = 9.4$ T and $v_R = 20$ kHz: (a) ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG with $\tau = \tau' = 0.7$ ms, (b) ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG with $\tau = 0.8$ ms, (c) ⁷¹Ga-{⁷⁷Se} *D*-HMQC-QCPMG with $\tau = 4$ ms.



Fig.2.13.⁷⁷Se projections of the 2D spectra of β -Ga₂Se₃ shown in **Fig.2.12**. The intensities are normalized so that Se^{III} signal has the same intensity in the three projections.

	<i>S</i> / <i>N</i> in one hour		
	Se ^{II}	Se ^{III}	
⁷¹ Ga{ ⁷⁷ Se} <i>J</i> -HMQC	139	307	
⁷¹ Ga{ ⁷⁷ Se} <i>D</i> -HMQC	24	36	
⁷⁷ Se{ ⁷¹ Ga} J-RINEPT	20	47	

Table.2.6. S/N ratios in one hour for the Se^{II} and Se^{III} signals of 2D ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG and ⁷¹Ga-{⁷⁷Se} *J*- and *D*-HMQC-QCPMG spectra of β -Ga₂Se₃.

For the three experiments, the S/N ratios in one hour of experiment are reported in **Table.2.6**. ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG experiment yields the highest *S/N* ratio since (i) the detected isotope is ⁷¹Ga, which has a higher gyromagnetic ratio than ⁷⁷Se ($\gamma_{71Ga} \approx 1.6\gamma_{77Se}$) and (ii) the ¹*J*_{71Ga-77Se} couplings (760 and 530 Hz) greatly exceed the dipolar couplings (ca. 200 Hz) between the same nuclei and hence, the ⁷¹Ga-⁷⁷Se coherence transfer is much faster through the *J*-couplings than through the dipolar couplings, i.e. optimal τ delay of 0.7-0.8 ms for *J*-HMQC experiment instead of 4 ms for *D*-HMQC one, which limits the signal losses.

Despite (i) the low natural abundance of ⁷⁷Se, (ii) the broad line-shape of ⁷¹Ga spectra, and (iii) the relatively low Larmor frequency of ⁷⁷Se, experimental times of these 2D experiments were always less than 5 hours. These preliminary encouraging results prove the high efficiency of the developed sequences and such methods were thus applied to characterize a non-crystalline sample.

2.4.2. ⁷¹Ga-⁷⁷Se correlations for 0.2Ga₂Se₃ - 0.8GeSe₂ glass (GGS_{0.2})

The methods employed for the characterization of β -Ga₂Se₃ were applied to that of the binary glass system 0.2Ga₂Se₃-0.8GeSe₂ (GGS_{0.2}). The ⁷⁷Se 1D spectrum of GGS_{0.2} exhibits only one resonance, as already reported for a similar glass composition (*x* = 0.3).[**12,13**] This resonance is ca. twice broader than the ⁷⁷Se spectrum of β -Ga₂Se₃ (compare **Fig.2.6(a,c)**). Such broadening stems from the presence of additional molecular units with the incorporation of Ge element, such as CS and ES GaSe₄ and GeSe₄ tetrahedra and (Se^{II})₃-Ge-Ge-(Se^{II})₃ units, as well as the glass structural disorder producing a distribution in ⁷⁷Se isotropic chemical shifts. The ⁷¹Ga spectrum displays a broad resonance at *B*₀ = 21.1 T and v_R = 62.5 kHz, as already observed for the crystalline β -Ga₂Se₃ (compare **Fig.2.6(b,d)**). At *B*₀ = 9.4 T and v_R = 20 kHz, the ⁷¹Ga spectrum is broader (**Fig.2.14**) and it displays many spinning sidebands. *T*'₂ constant times of ⁷¹Ga and ⁷⁷Se nuclei were measured in GGS_{0.2} using sequences in **Fig.2.2(c,d)**, and we found *T*'_{2,71Ga} ≈ 8 ms and *T*'_{2,77Se} ≈ 18 ms (**Fig.2.15**). These values are similar to those found in β -Ga₂Se₃ (**Table.2.4**).



Fig.2.15. Experimental decay of (a) ⁷¹Ga spin-echo-QCPMG signal and (b) ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-spin-echo-CPMG signal of GGS_{0.2}. The red continuous curves correspond to the best fit curves with $T'_2 =$ (a) 8 and (b) 18 ms.

Fig.2.16 displays the build-up curves of ⁷⁷Se-{⁷¹Ga} *J*-RINEPT experiments with $\tau = \tau'$ and ⁷¹Ga-{⁷⁷Se} *J*-HMQC ones of crystalline β-Ga₂Se₃ and GGS_{0.2} glass. As Se^{II} and Se^{III} resonances are not separated in the 1D spectra of GGS_{0.2}, the build-up curves of the glass are compared to the sum of Se^{II} and Se^{III} *J*-RINEPT build-up curves in crystalline β-Ga₂Se₃ weighted by the fractions of the Se^{II} and Se^{III} signals in the 1D ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG. Moreover, ⁷¹Ga-{⁷⁷Se} *J*-HMQC spectra of GGS_{0.2} (see **Fig.2.21(a)** and (c)) are displayed for comparison purpose. Therefore, the oscillations are slightly smoothed as compared to **Fig.2.10**. At short defocusing and refocusing times ($\tau < 1.2$ ms), glass and crystal exhibit identical buildup curves, which indicates that the ¹*J*_{71Ga-77Se} couplings, and hence Ga-Se bonds, are similar in both samples. However, for longer times ($\tau > 1.2$ ms), the curves of both materials deviate. Such difference stems notably from different ³*J*_{71Ga-77Se} couplings since the torsion angles differ between the glass and the crystal. Similarly, the lack of signal oscillation for long τ values in the case of the glass stems from the distribution of ³*J*_{71Ga-77Se} coupling values.



Fig.2.16. Evolution of (a) 1D ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG signals of β -Ga₂Se₃ (black) and GGS_{0.2} (blue) versus $\tau = \tau$ ' and (b) 1D ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG versus τ . To compare both materials, the weighted intensity of the two selenium resonances (**Fig.2.10**(**a** + **b**) and **Fig.2.10**(**g** + **h**)) were added for crystalline β -Ga₂Se₃.

To be sure that all ⁷¹Ga and ⁷⁷Se sites are well excited, 1D ⁷⁷Se-{⁷¹Ga} *J*-RINEPT and 2D ⁷¹Ga-{⁷⁷Se} *J*-HMQC spectra were recorded with different carrier frequencies. **Fig.2.17** shows the 1D ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG spectra acquired with different carrier frequencies and it indicates that the total frequency range of ⁷⁷Se spectrum of $GGS_{0.2}$ glass is excited by *J*-RINEPT sequence using centered carrier frequency.



Fig.2.17. ⁷⁷Se-{⁷¹Ga} 1D *J*-RINEPT-CPMG spectra of GGS_{0.2} at $B_0 = 9.4$ T and $v_R = 20$ kHz, $v_{1,71Ga} = 95$, $v_{1,77Se} = 63$ kHz and various ⁷⁷Se rf offsets indicated on the figure.

Fig.2.18 shows the 2D ⁷⁷Se-{⁷¹Ga} *J*-RINEPT and ⁷¹Ga-{⁷⁷Se} *J*- and *D*-HMQC spectra of GGS_{0.2} glass. The ⁷⁷Se projections of these 2D spectra are shown in **Fig.2.19**. These projections exhibit higher resolution than the 1D ⁷⁷Se CPMG spectrum shown in **Fig.2.6(c)**. Furthermore, as seen in **Fig.2.20**, the ⁷⁷Se nuclei connected or close to ⁷¹Ga isotopes resonate at lower isotropic chemical shifts than those that are only bonded to Ge atoms.



Fig.2.18. 2D spectra of GGS_{0.2} at $B_0 = 9.4$ T with $v_R = 20$ kHz: (a) ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG with $\tau = \tau' = 0.8$ ms, (b) ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG with $\tau = 0.8$ ms, (c) ⁷¹Ga-{⁷⁷Se} *D*-HMQC-QCPMG spectrum with $\tau = 3$ ms.



Fig.2.19. Comparison of the ⁷⁷Se projections of the ⁷¹Ga-⁷⁷Se HETCOR 2D spectra of $GGS_{0.2}$ shown in **Fig.2.18**.



Fig.2.20. Comparison of 1D ⁷⁷Se spectra of $GGS_{0.2}$: CPMG (blue) and ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG (black).

Fig.2.21 shows the deconvolution of the ⁷⁷Se projection of 2D ⁷¹Ga-⁷⁷Se HETCOR spectra as well as the 1D ⁷⁷Se CPMG spectrum of GGS_{0.2} glass. In a first step, the ⁷⁷Se projections of *J*-RINEPT-CPMG and *J*-HMQC-QCPMG 2D spectra were simulated using the NMR parameters of already observed local environments of ⁷⁷Se nuclei in GGS_x glass, i.e. ⁷⁷Se^{II} sites of CS GeSe₄ and GaSe₄ tetrahedra resonating at 400 ppm and bonded to Ge-Ge bond resonating at 250 ppm as well as ⁷⁷Se^{III} sites of these CS tetrahedra resonating at –20 ppm.[**13**] Nevertheless, additional signals resonating at 128, –144 and –250 ppm were required to simulate the ⁷⁷Se projections of 2D *J*-RINEPT and *J*-HMQC spectra. The resonance at –144 ppm can be assigned to Se^{III} nuclei bonded to Ga-Ga bond since the GaSe, which consists of layers of (Se^{III})₃-Ga-Ga-(Se^{III})₃, moieties exhibits a single resonance at -80 ppm. The 2D spectra

exhibit ⁷¹Ga signal at 1200 ppm characteristic of Ga nuclei in such environment.[**37**] The resonances at 128 and –250 ppm are tentatively assigned to Se^{III} sites of ES GeSe₄ and GaSe₄ tetrahedra and bonded to Ge-Ge bond. Nevertheless, further studies, including Density Functional Theory (DFT) calculations, would be required to confirm this assignment. The simulation of the ⁷⁷Se projection of 2D *D*-HMQC spectra includes the same contributions as those employed to simulate the ⁷⁷Se projections of the ⁷¹Ga-⁷⁷Se J-HETCOR 2D spectra. However, the signal of ES GeSe₄ tetrahedra resonating at 600 ppm must also be included.[**12**] The absence of this signal for the through-bond correlations indicates that most of Se atoms in ES tetrahedra are bonded to Ge metal and the coherence transfer to ⁷¹Ga is achieved through the dipolar couplings. In the simulation of 1D ⁷⁷Se CPMG spectrum, the relative integrated intensity of ⁷⁷Se^{II} sites of CS GeSe₄ and GaSe₄ tetrahedra and ES GeSe₄ is larger than in the ⁷⁷Se projections of the 2D spectra since most ES tetrahedra and a large fraction of CS ones contain Ge metal. Additional contribution resonating at 850 ppm is also required to simulate the 1D ⁷⁷Se CPMG spectrum. It is assigned to Se-Se^{II}-Se environment.[**38**]



Fig.2.21. Deconvolution of the ⁷⁷Se projections of 2D spectra of GGS_{0.2}: (a) ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG, (b) ⁷¹Ga-{⁷⁷Se} *D*-HMQC-QCPMG, (c) ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG, so that (d) the 1D ⁷⁷Se CPMG spectrum.

Table.2.7. Simulation parameters for the deconvolution of 1D ⁷⁷Se CPMG spectra of $GGS_{0.2}$ shown in **Fig.2.21**. $-Ge^{IV/3} = -GeSe_3$ and $-Ge^{IV/2} = -GeSe_2$ - mean one Ge atom *additionally* bonded to 3 and 2 Se atoms. $Ge/Ga^{IV/3} = -GeSe_3$ or $-GaSe_3$ means either a Ge or a Ga atom *additionally* bonded to 3 Se atoms.

	δ_{iso}/ppm	δ_{aniso}/ppm	η	FWHM/ppm	Fraction /%
$Ge^{IV/3}$ - $Ge^{IV/2}$ - Se^{III} - $(Ge/Ga^{IV/3})_2$	-250	-120	0	145	1.65
$Ga^{IV/3}$ - $Ga^{IV/2}$ - Se^{III} - $(Ge/Ga^{IV/3})_2$	-144	-120	0	133	1.91
Se^{III}- (Ge/Ga ^{IV/3}) ₃ (CS)	-20	-120	0	158	5.60
Se^{III}- (Ge/Ga ^{IV/3}) ₃ (ES)	128	-120	0	163	9.09
$Ge^{IV/3}$ - $Ge^{IV/2}$ - Se^{II} - $(Ga/Ge^{IV/3})$	250	250	0.9	194	18.98
$\mathbf{Se^{II}}$ -(Ge/Ga ^{IV/3}) ₂ (CS)	400	250	0.9	243	44.17
$\mathbf{Se^{II}}$ -(Ge ^{IV/3}) ₂ (ES)	600	280	0.9	298	14.74
Se-Se ^{II} -Se	850	-150	0.8	400	3.85

2.5. Conclusion

We have introduced 2D ⁷¹Ga-⁷⁷Se through-bond and through-space correlation experiments, including ⁷⁷Se-{⁷¹Ga} *J*-RINEPT-CPMG and ⁷¹Ga-{⁷⁷Se} *J*- or *D*-HMQC-QCPMG methods. These experiments have been demonstrated experimentally on β -Ga₂Se₃ crystal and GGS_{0.2} glass. For the glass, these experiments improve the resolution of the ⁷⁷Se signal by selecting the ⁷⁷Se nuclei connected or close to ⁷¹Ga nuclei. We show that the ⁷¹Ga-{⁷⁷Se} *J*-HMQC-QCPMG experiment exhibit the highest sensitivity. Furthermore, the analysis of the build-up curves of the ⁷¹Ga-⁷⁷Se through-bond correlation experiments allows the estimate of both ¹*J*_{71Ga-77Se} and ³*J*_{71Ga-77Se} couplings in β -Ga₂Se₃ crystal. By introducing ⁷¹Ga STMAS-QCPMG experiment at high field and high MAS frequency, we also resolve the ⁷¹Ga signal of Annealed phase and that of Quenched phase. ⁷¹Ga-⁷⁷Se correlation experiments identify Annealed phase and Quenched phase in β -Ga₂Se₃ crystal.

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Chapter 3: γ-independent through-space heteronuclear correlation between spin-1/2 and quadrupolar nuclei in solids

3.1. Introduction

Two-dimensional (2D) through-space dipolar heteronuclear correlation (*D*-HETCOR) NMR experiments allow in solids the unambiguous identification of proximities between sites occupied by different isotopes. Therefore, these methods are essential tools to facilitate the assignment of solid-state NMR spectra and to investigate the local atomic-level structures of materials. In this article, we focus on correlations between quadrupolar nuclei (e.g. ¹¹B, ¹⁴N, ¹⁷O, ²⁷Al...) and spin-1/2 isotopes (e.g. ¹³C, ³¹P, ²⁹Si...), other than ¹H and ¹⁹F, which represent about 3/4 and 1/4 of stable NMR-active nuclei, respectively.[1–3] For instance, correlations between ³¹P nuclei and ²⁷Al, ¹¹B or ⁵¹V have been used to investigate the association between P₂O₅ and other glass-former oxides, such as Al₂O₃, B₂O₃ or V₂O₅.[4–6] ³¹P-²⁷Al and ³¹P-⁵¹V correlations have also been used to investigate the structure of crystalline alumino- and vanado-phosphate materials, respectively.[7–9] Similarly, correlations between ²⁹Si and ²⁷Al nuclei have been employed to study crystalline and amorphous silicate materials, such as zeolites, clays and glasses.[10–13] More recently, ¹³C-²⁷Al proximities in organo-aluminum solids and zeolites have also been probed using *D*-HETCOR experiments.[14–17]

These *D*-HETCOR experiments between spin-1/2 and quadrupolar nuclei should be efficient and robust to quadrupole interactions, electron shielding, inhomogeneity of the radiofrequency (rf) field, and instabilities of the Magic-Angle Spinning (MAS) frequency. Several pulse sequences have been proposed to correlate spin-1/2 and quadrupolar nuclei. Initially, such correlations have been achieved using cross-polarization (CP).[**18**] However, the efficiency and the robustness of CP transfers between spin-1/2 and quadrupolar nuclei are limited by the complex spin dynamics during spin locking, which depends on several factors, including (i) the amplitude and the orientation of the electric field gradient, (ii) the MAS frequency, v_R, and (iii) the rf field amplitude, v₁.[**19**] These shortcomings can be alleviated by the use of other *D*-HETCOR methods, such as the Dipolar-mediated Refocused Insensitive-Nuclei Enhanced by Polarization-Transfer (*D*-RINEPT) [**8**,**9**] and the Dipolar-mediated Heteronuclear Multiple Quantum Correlation (*D*-HMQC) experiments.[**20**,**21**] In these sequences, the heteronuclear dipolar couplings with the quadrupolar nuclei are reintroduced by irradiating only the spin-1/2 isotope, hence limiting the interference of the quadrupole interaction with the recoupling sequence. The *D*-RINEPT and *D*-HMQC methods complement each other since the former employs direct detection, i.e. the excited and detected isotopes differ, whereas the latter uses indirect detection, i.e. the detected isotope is the same as the excited one. The relative sensitivities of the direct and indirect detections depend on the gyromagnetic ratios, the longitudinal relaxation times, and the spectral widths of the correlated nuclei.^[22] This work focuses on sequences based on indirect detection.

In *D*-HMQC sequence, the dipolar couplings between spin-1/2, other than ¹H and ¹⁹F, and quadrupolar nuclei have been reintroduced by applying to the spin-1/2 isotope heteronuclear dipolar schemes, such as Rotational-Echo DOuble Resonance (REDOR),[20] Simultaneous Frequency and Amplitude Modulation (SFAM₁),[23–25] and the Rotary Resonance Recoupling, $R^3(q = 1)$, with $v_1 = v_R$.[21] These recoupling schemes reintroduce the space component |m| = 1 for the dipolar coupling and the chemical shift anisotropy (CSA) of the spin-1/2 isotope. The |m| = 1 recoupling schemes benefit from larger scaling factors for the heteronuclear dipolar coupling than the |m| = 2 schemes and hence, require shorter recoupling periods in indirectly detected experiments, thus limiting the signal losses during coherence transfers.[25] Contrary to the |m| = 2 schemes, the |m| = 1 ones do not remove the homonuclear dipolar couplings between the irradiated spin-1/2 nuclei. Nevertheless, for nuclei other than ¹H and ¹⁹F, the remaining homonuclear dipolar couplings are usually much smaller than the recoupled ones between spin-1/2 and quadrupolar nuclei, especially at high spinning speeds, and they lead to limited signal losses during the recoupling periods of indirectly detected *D*-HETCOR experiments.

Among the existing |m| = 1 recoupling schemes, it has been shown that SFAM₁ offers high robustness to rf inhomogeneity and resonance offset. In particular, it has been shown that when incorporated into the *D*-HMQC sequence, the SFAM₁ recoupling provides higher efficiencies than REDOR and R³(q = 1) methods.[25] However, the SFAM₁ recoupling is non- γ -encoded since the contribution of the heteronuclear dipolar coupling to the average Hamiltonian has a norm which depends on the Euler angle, $\gamma_{PR}^{D,IS}$, relating the internuclear vector between the coupled spins to the MAS rotor-fixed frame.[26] Because of this non- γ -encoding, each crystallite must have the same orientation at the beginnings of the two SFAM₁ parts, i.e. at the beginnings of defocusing and refocusing periods.[25] In other words, the delay between the beginnings of the two SFAM₁ parts must be rotor-synchronized, i.e. be an integer multiples of a rotor period, T_R. Such condition is especially difficult to achieve in *D*-HETCOR experiments when the t_1 evolution time is long due to weak dipolar interactions. Consequently, the *D*-HMQC sequence employing SFAM₁ recoupling is sensitive to fluctuations of the MAS frequency. On the contrary to the REDOR recoupling, the $R^3(q = 1)$ scheme is γ -encoded,[26] but this does not mean that when introduced in an NMR experiment the signal is independent on the $\gamma_{PR}^{D,IS}$ angle. A sequence, the signal of which does not depend on this angle, will be termed γ -independent hereafter. The γ -encoding of the recoupling scheme is a necessary, but not sufficient, condition for the γ -independence of the whole sequence. *D*-HMQC sequences with $R^3(q = 1)$ recoupling have been reported but these sequences are not necessarily γ -independent.[20,21] Furthermore, a major limitation of $R^3(q = 1)$ scheme is its sensitivity to rf inhomogeneity, especially when the irradiated spin is subject to small CSA.[23,26] The CSA of ¹³C and ¹⁵N nuclei have been reintroduced using γ -encoded |m| = 1 symmetry-based recoupling sequences, such as $R8_1^3$, $R10_1^4$, $R12_1^5$ or $R14_2^5$.[27,28] However, to the best of our knowledge, these sequences have not been used so far to reintroduce the heteronuclear dipolar coupling.

In the present article, we introduce novel γ -independent *D*-HETCOR experiments to correlate spin-1/2 nuclei, other than ¹H and ¹⁹F, and quadrupolar ones. To reintroduce the dipolar interaction under MAS, these experiments employ γ -encoded $|m| = 1 RN_n^{\gamma}$ schemes, which are applied either on the detected or the undetected channel.

In the theoretical section, we explain how the RN_n^{ν} schemes are selected and give the expression of the contribution of the heteronuclear dipolar coupling to the first-order average Hamiltonian. We describe how these recoupling schemes have been incorporated into the *D*-HETCOR sequences. In particular, how γ -independent *D*-HETCOR experiments with RN_n^{ν} schemes on the detected spin are achieved by introducing a novel sequence, named Dipolar-mediated Heteronuclear Universal-Quantum Correlation (*D*-HUQC). We then provide the analytical signal expressions for the various sequences.

Numerical simulations are then employed to test the validity of these expressions and the robustness of the various recouplings to offset, CSA, rf-field inhomogeneity and MAS instabilities.

The performances of the various recouplings and *D*-HMQC and *D*-HUQC sequences are finally compared between ¹³C and ¹⁵N nuclei in glycine and between ³¹P and ²⁷Al in VPI-5 and Na₇(AlP₂O₇)₄PO₄.

3.2. Theory

In the following, we will always assume that the recoupling is applied to I spin.

3.2.1. Recoupling schemes

The heteronuclear dipolar interaction is characterized by a space rank l = 2 and a spin rank $\lambda = 1$. Hence, it can be regarded as the superposition of 15 components, with component indexes m = -2, -1, 0, +1 or +2 and $\mu = -1, 0$ or +1. As mentioned in the introduction, the γ -encoding of the heteronuclear recoupling scheme is desirable in order to improve the robustness of the sequence to instabilities of the MAS frequency. It has been shown that a bijection between the m and μ indexes is a sufficient condition to achieve γ -encoded recoupling.[29,30] In other words, schemes reintroducing two components, {2, m, 1, μ } and {2, -m, 1, $-\mu$ }, of the heteronuclear dipolar interaction are γ -encoded. Furthermore, the scaling factor of the |m| = 1 components is usually $\sqrt{2}$ higher than that of the |m| = 2 ones. High scaling factors limit the signal losses during the recoupling periods. Hence, γ -encoded |m| = 1 schemes require selecting the {2, 1, 1, μ } and {2, -1, 1, $-\mu$ } components of the heteronuclear dipolar interaction, with $\mu = \pm 1$.

Setting up periodic symmetry relationships between the space and spin rotations facilitates the design of heteronuclear dipolar recoupling since these symmetry arguments allow generating a first-order average Hamiltonian containing the desired rotational components, {2, 1, 1, μ } and {2, -1, 1, - μ }, while other components are suppressed.[29,31] Among the symmetry-based recoupling sequences, the RN_n^{ν} class leads to selection rules on the first-order average Hamiltonian, which are more selective than the CN_n^{ν} class.[32,33] Consequently, the number of higher-order terms in the effective Hamiltonian tends to be larger for CN_n^{ν} schemes than for RN_n^{ν} ones, which are thus often more robust.

A total of 269 R N_n^{ν} schemes were found, with $2 \le N \le 30$, $1 \le n \le 10$ and $1 \le \nu \le 21$, which only recouple the two components of the heteronuclear dipolar coupling and CSA in the firstorder average Hamiltonian. Here, we only considered RN_n^{ν} schemes, where *N* must be even, built around π -pulses. These schemes result from the *N*/2-fold repetition of the pair $\pi_{\phi}\pi_{-\phi}$ of pulses, involving the phase shift $\phi = \pi \nu/N$. Each of the π -pulses has the same duration, nT_R/N , and rf-field requirement, $\nu_1 = N\nu_R/(2n)$. **Fig.3.1(a)** shows that the phase ϕ of the γ -encoded |m|= 1 recoupling scheme monotonically increases with rf-field when $\nu_1 \ge \nu_R$ and asymptotically converges towards 90°. The scaling factor, κ , of the allowed components of the heteronuclear dipolar coupling was calculated by using the 'C and R symmetries' Mathematica package. [32– 35] As seen in **Fig.3.1(b**), κ monotonically increases with rf-field and asymptotically converges towards 0.26. We also calculated the number, $N^{(2)}$, of symmetry-allowed 2nd-order cross-terms involving commutators of two CSA Hamiltonians, two offset ones, and between one CSA and one offset Hamiltonians.[35] Among the 269 R N_n^{ν} schemes mentioned above, the minimal $N^{(2)}$ value is 42. Therefore, a total of 51 R N_n^{ν} recoupling were pre-selected with $\kappa > 0.24$, $\nu_1 < 3.6\nu_R$ and $N^{(2)} = 42$, and the properties of the finally chosen 4 schemes are listed in **Table.3.1**. The related *D*-HMQC and *D*-HUQC sequences were further investigated by numerical simulations and experiments.



Fig.3.1. (a) Phase ϕ (°) and (b) scaling factor κ versus the ratio v_1/v_R for γ -encoded |m| = 1 RN_n^{ν} heteronuclear recoupling schemes with $2 \le N \le 30$, $1 \le n \le 10$ and $1 \le \nu \le 21$. It must be noted that for each v_1/v_R ratio the complementary phase, 180 - ϕ , also works with the same κ scaling factor.

$\mathbb{R}N_n^{\nu}$	φ °	v_1/v_R	к
R18 ⁵ ₄	50.0	2.25	0.248
R10 ³ ₂	54.0	2.50	0.250
R16 ⁵ ₃	56.25	2.67	0.251
R14 ⁵ ₂	64.28	3.5	0.254

Table.3.1. Properties of the selected RN_n^{ν} heteronuclear schemes recoupling the {2, 1, 1, -1} and {2, -1, 1, 1} components.

The γ -encoded $|m| = 1 RN_n^{\nu}$ contribution of *I-S* dipolar interaction to the average Hamiltonian is equal to:

$$\overline{\hat{H}_{D,IS}}^{(1)}(\mathbb{R}N_n^{\nu}) = \omega_{D,IS} [\hat{S}_z \hat{I}^+ \exp(i\varphi) + \hat{S}_z \hat{I}^- \exp(-i\varphi)]$$
$$= 2\omega_{D,IS} [\hat{S}_z \hat{I}_x \cos(\varphi) - \hat{S}_z \hat{I}_y \sin(\varphi)]$$
(3.1)

where the magnitude, $\omega_{D,IS}$, and the phase, φ , of the recoupled *I-S* coupling are given by

$$\omega_{D,IS} = \kappa \frac{\sqrt{3}}{2} b_{IS} \sin\left(2\beta_{PR}^{D,IS}\right) \tag{3.2}$$

and

$$\varphi = \gamma_{PR}^{D,IS} + \alpha_{RL}^0 - \omega_R t^0 \tag{3.3}$$

In Eqs.(3.2) and (3.3), (i) b_{IS} is the dipolar coupling constant in rad.s⁻¹, (ii) the Euler angles {0, $\beta_{PR}^{D,IS}, \gamma_{PR}^{D,IS}$ } relate the internuclear direction to the MAS rotor-fixed frame, (iii) $\omega_R = 2\pi v_R$, and (iv) t^0 refers to the starting time of the RN_n^{ν} scheme. As seen in Eq.(3.1), the γ -encoded |m| $= 1 RN_n^{\nu}$ scheme reintroduces single-quantum (1Q) heteronuclear dipolar coupling terms. The evolutions of product operators for two coupled spin-1/2 nuclei *I* and *S* are given in **Table.3.1**. Under $\overline{\hat{H}_{D,IS}}^{(1)}(RN_n^{\nu})$, the z-magnetization of the *I*-spin is converted into heteronuclear multiple-quantum (MQ) coherences described by $2\hat{S}_y \hat{I}_y$ and $2\hat{S}_y \hat{I}_x$ operators, whereas the *x*magnetization of the *S*-spin evolves into heteronuclear MQ coherences described by $2\hat{S}_y \hat{I}_x$ and $2\hat{S}_y \hat{I}_y$ operators. In both cases, the phase of the heteronuclear MQ coherences depends on φ angle. $\overline{\hat{H}_{D,IS}}^{(1)}(RN_n^{\nu})$ depends on φ phase, and hence $\gamma_{PR}^{D,IS}$ angle, but conversely its norm does not, which confirms the γ -encoding of these RN_n^{ν} sequences.[26]

In the case of \mathbb{R}^3 scheme applied to *I* spin, the contribution of *I-S* dipolar interaction to the average Hamiltonian is tilted by $-\pi/2$ around \hat{I}_y with respect to Eq.(3.1):

$$\overline{\widehat{H}_{D,IS}}^{(1)}(R^3) = \exp\left(\iota \frac{\pi}{2} \widehat{I}_y\right) \cdot \overline{\widehat{H}_{D,IS}}^{(1)}(RN_n^{\nu}) \cdot \exp\left(-\iota \frac{\pi}{2} \widehat{I}_y\right)$$
(3.4)

with $\kappa = 1/\sqrt{6} \approx 0.408$. Hence, the R³ scheme is also γ -encoded.

The simultaneous frequency and amplitude modulation (SFAM₁) scheme has been proposed to recouple the hetero-nuclear dipolar interactions.[36] The carrier frequency, $v_{ref} + \Delta v_{ref}(t)$, of the rf-field is modulated with a cosine, while its amplitude, $v_1(t)$, is modulated with a sine, both in a rotor-synchronized way:

$$v_1(t) = v_1^{\max} \sin(2\pi v_R t) \qquad \Delta v_{ref}(t) = \Delta v_{ref}^{\max} \cos(2\pi v_R t)$$
(3.5)

When the SFAM₁ scheme in the region 2 is applied to the *I* spin, $\Delta v_{ref}^{max} \approx v_1^{max} \approx 3v_R$, the average Hamiltonian of the *I-S* dipolar interaction is

$$\overline{\widehat{H}_{D,IS}}^{(1)}(\text{SFAM}) = 2\omega_{D,IS}\widehat{S}_{z}\widehat{I}_{z}$$
(3.6)

where

$$\omega_{D,IS} = \kappa b_{IS} \sin(2\beta_{PR}^{D,IS}) \cos(\varphi)$$
(3.7)

with $\kappa = -C_1/(2\sqrt{2})$ and $C_1 \approx 1$ is the first coefficient of the Fourier series expansion of $\cos[\theta(t)]$, where $\theta(t)$ is the tilt angle between B_0 and the effective field.[25] As seen in Eq.(3.7), the SFAM₁ scheme is non- γ -encoded since its norm depends on φ , and hence on $\gamma_{PR}^{D,IS}$ angle. RN_n^{γ} and R^3 schemes are dipolar-truncated (single-quantum coherences $\hat{S}_z \hat{I}_{x/y}$ in Eq.(3.1 and 3.4), whereas SFAM₁ is not (two-spin-order coherences $\hat{S}_z \hat{I}_z$ in Eq.(3.6)). In the first case, a small dipolar coupling between two spins is only weakly reintroduced if one or both spins are also strongly dipolar coupled to other spins. On the contrary, in the second case long distances correlations can be observed.

$\widehat{\boldsymbol{\theta}}(0)$	$\exp\left(-i\overline{\widehat{H}_{D,IS}}^{(1)}\tau\right)\widehat{\boldsymbol{\partial}}(0)\exp\left(i\overline{\widehat{H}_{D,IS}}^{(1)}\tau\right)$
\hat{S}_{χ}	$\hat{S}_x \cos(\omega_{D,IS}\tau) + 2\hat{S}_y \{ \hat{I}_x \cos(\varphi) - \hat{I}_y \sin(\varphi) \} \sin(\omega_{D,IS}\tau)$
\hat{S}_y	$\hat{S}_{y}\cos(\omega_{D,IS}\tau) - 2\hat{S}_{x}\{\hat{I}_{x}\cos(\varphi) - \hat{I}_{y}\sin(\varphi)\}\sin(\omega_{D,IS}\tau)$
\hat{S}_z	\hat{S}_z
$2\hat{S}_{x}\hat{I}_{z}$	$2\hat{S}_{x}\hat{I}_{z}$
$2\hat{S}_{y}\hat{I}_{z}$	$2\hat{S}_{y}\hat{I}_{z}$
$2\hat{S}_{z}\hat{I}_{z}$	$2\hat{S}_{z}\hat{I}_{z}\cos(\omega_{D,IS}\tau) - \{\hat{I}_{y}\cos(\varphi) + \hat{I}_{x}\sin(\varphi)\}\sin(\omega_{D,IS}\tau)$
\hat{I}_{x}	$\hat{I}_{x}\left\{\cos^{2}(\varphi) + \cos\left(\omega_{D,IS}\tau\right)\sin^{2}(\varphi)\right\} - \hat{I}_{y}\sin^{2}\left(\frac{\omega_{D,IS}\tau}{2}\right)\sin(2\varphi)$
	$+ 2\hat{S}_{z}\hat{I}_{z}\cos(\varphi)\sin(\omega_{D,IS}\tau)$
\hat{I}_y	$\hat{I}_{y}\left\{\cos\left(\omega_{D,IS}\tau\right)\cos^{2}(\varphi) + \sin^{2}(\varphi)\right\} - \hat{I}_{x}\sin^{2}\left(\frac{\omega_{D,IS}\tau}{2}\right)\sin(2\varphi)$
	$+2\hat{S}_{z}\hat{I}_{z}\cos(\varphi)\sin(\omega_{D,IS}\tau)$
\hat{I}_z	$\hat{I}_z \cos(\omega_{D,IS}\tau) - 2\hat{S}_y \{\hat{I}_y \cos(\varphi) + \hat{I}_x \sin(\varphi)\} \sin(\omega_{D,IS}\tau)$
$2\hat{S}_{z}\hat{I}_{x}$	$2\hat{S}_{z}\hat{I}_{x}\left\{\cos^{2}(\varphi) + \cos\left(\omega_{D,IS}\tau\right)\sin^{2}(\varphi)\right\} - 2\hat{S}_{z}\hat{I}_{y}\sin^{2}\left(\frac{\omega_{D,IS}\tau}{2}\right)\sin(2\varphi)$
	$+ \hat{l}_z \sin(\varphi) \sin(\omega_{D,IS} \tau)$
$2\hat{S}_{z}\hat{I}_{y}$	$2\hat{S}_{z}\hat{I}_{x}\left\{\cos\left(\omega_{D,IS}\tau\right)\cos^{2}(\varphi) + \sin^{2}(\varphi)\right\} + 2\hat{S}_{z}\hat{I}_{y}\sin^{2}\left(\frac{\omega_{D,IS}\tau}{2}\right)\sin(2\varphi)$
	$+ \hat{I}_z \cos(\varphi) \sin(\omega_{D,IS} \tau)$
$2\hat{S}_{x}\hat{I}_{x}$	$2\hat{S}_{x}\hat{I}_{x}\left\{\cos\left(\omega_{D,IS}\tau\right)\cos^{2}(\varphi)+\sin^{2}(\varphi)\right\}+2\hat{S}_{y}\hat{I}_{x}\sin^{2}\left(\frac{\omega_{D,IS}\tau}{2}\right)\sin(2\varphi)$
	$+ \hat{S}_y \cos(\varphi) \sin(\omega_{D,IS} \tau)$
$2\hat{S}_{x}\hat{I}_{y}$	$2\hat{S}_{x}\hat{l}_{y}\left\{\cos^{2}(\varphi) + \cos\left(\omega_{D,IS}\tau\right)\sin^{2}(\varphi)\right\} + 2\hat{S}_{x}\hat{l}_{x}\sin^{2}\left(\frac{\omega_{D,IS}\tau}{2}\right)\sin(2\varphi)$
	$-\hat{S}_{y}\sin(\varphi)\sin(\omega_{D,IS}\tau)$
$2\hat{S}_{y}\hat{I}_{x}$	$2\hat{S}_{y}\hat{l}_{x}\left\{\cos\left(\omega_{D,IS}\tau\right)\cos^{2}(\varphi) + \sin^{2}(\varphi)\right\} + 2\hat{S}_{y}\hat{l}_{y}\sin^{2}\left(\frac{\omega_{D,IS}\tau}{2}\right)\sin(2\varphi)$
	$-\hat{S}_{x}\cos(\varphi)\sin(\omega_{D,IS}\tau)$
$2\hat{S}_{y}\hat{I}_{y}$	$2\hat{S}_{y}\hat{I}_{y}\left\{\cos^{2}(\varphi) + \cos\left(\omega_{D,IS}\tau\right)\sin^{2}(\varphi)\right\} + 2\hat{S}_{x}\hat{I}_{y}\sin^{2}\left(\frac{\omega_{D,IS}\tau}{2}\right)\sin(2\varphi)$
	$+ \hat{S}_x \sin(\varphi) \sin(\omega_{D,IS}\tau)$

Table 3.2. Evolution of product operators for two coupled spin-1/2 nuclei, *I* and *S*, during γ -encoded $|m| = 1 \text{ R}N_n^{\nu}$ heteronuclear recoupling when such scheme is applied to the spin *I*.

3.2.2. *D***-HETCOR** sequences

3.2.2.1. Recoupling applied to the indirectly detected isotope.

As said before, the dipolar recoupling is applied to *I* spin, which is indirectly detected in this part, whereas the *S* spin is detected.

Fig.3.2(b) displays the pulse sequence of *D*-HMQC experiments in which the SFAM₁ scheme is applied to the indirectly detected spin (denoted HMQC-I-SFAM₁ hereafter). During the first SFAM₁ defocusing period, the in-phase *S*-spin magnetization (\hat{S}_x) for a pair of coupled *IS* spins evolves into antiphase one $(2\hat{S}_y\hat{I}_z)$, which is converted into heteronuclear MQ coherences $(2\hat{S}_y\hat{I}_x)$ by the $\pi/2$ -pulse with phase y on the *I* channel (I- $\pi/2_y$ pulse hereafter). The isotropic shift is then encoded by allowing these MQ coherences to evolve during the evolution time, t_1 . The S- π_y pulse applied in the middle of the t_1 period refocuses the evolution of the *S*-spin magnetization under isotropic shift during the τ and t_1 delays as well as its evolution under *J*_{*I*-*S*} coupling. At the end of t_1 , the MQ coherences are converted back into anti-phase *S*-spin magnetization by the I- $\pi/2_{-y}$ pulse and these coherences evolve during the second SFAM₁ refocusing period, into observable transverse *S*-spin magnetization. On a powder sample, the NMR signal of this experiment is proportional to [25]

$$S(\tau) \propto \frac{1}{2} \left\{ 1 - \frac{\pi\sqrt{2}}{4} J_{1/4}(\kappa b_{IS}\tau) J_{-1/4}(\kappa b_{IS}\tau) \right\}$$
(3.8)

where $J_{\pm 1/4}(x)$ denotes the Bessel functions of the first kind and $\pm 1/4$ -order. In the absence of losses, the shorter τ value producing maximal $S(\tau)$ intensity is $\tau^{\text{opt}} = 2.36/(\kappa b_{IS})$.

Fig.3.2(a) displays the pulse sequence of *D*-HMQC-I experiments with the γ -encoded |m|= 1 RN_n^{ν} recoupling (denoted HMQC-I-RN_n^{ν} hereafter). During the defocusing delay, the inphase *S*-spin magnetization is converted into heteronuclear MQ coherences, $2\hat{S}_y\hat{I}_{-\varphi}$, where $\hat{I}_{-\varphi} = \hat{I}_x \cos(\varphi) - \hat{I}_y \sin(\varphi)$. These coherences are encoded by isotropic shift during t_1 . As seen in **Table.3.2**, $2\hat{S}_y\hat{I}_x$ and $2\hat{S}_y\hat{I}_y$ operators are converted back into \hat{S}_x during the refocusing delay, with coefficients $-\cos(\varphi)$ and $\sin(\varphi)$, respectively. Hence, the NMR signal of this experiment is proportional to

$$S(\tau) \propto \langle \{\cos^2(\varphi) + \sin^2(\varphi)\}\sin^2(\omega_{D,IS}\tau) \rangle = \frac{1}{2} \left[1 - \langle \cos(2\omega_{D,IS}\tau) \rangle \right]$$
(3.9)

where the angular bracket $\langle ... \rangle$ denotes the powder average over all orientations of the *I-S* internuclear vectors. As seen win Eq.(3.2), $\omega_{D,IS}$ does not depend on $\gamma_{PR}^{D,IS}$ angle and hence, the HMQC-I-R N_n^{ν} sequence is γ -independent. Using the closed analytical form for γ -encoded |m|= 1 recoupling sequence,[30] Eq.(3.9) can be recast as

$$S(\tau) \propto \frac{1}{2} - \frac{1}{3^{1/4}} \sqrt{\frac{\pi}{8\kappa b_{IS}\tau}} \left\{ F_c \left(3^{1/4} \sqrt{\frac{2\kappa b_{IS}\tau}{\pi}} \right) \cos(\sqrt{3}\kappa b_{IS}\tau) + F_s \left(3^{1/4} \sqrt{\frac{2\kappa b_{IS}\tau}{\pi}} \right) \sin(\sqrt{3}\kappa b_{IS}\tau) \right\}$$
(3.10)

where $F_c(x)$ and $F_s(x)$ are the Fresnel cosine and sine integrals, respectively.[30] The shorter τ value producing maximal $S(\tau)$ intensity is $\tau^{\text{opt}} = 2.18/(\kappa b_{IS})$.

Given Eq.(3.4), the RN_n^{ν} recoupling can be replaced by a R³ one bracketed by $\pi/2$ -pulse with phases -y and y. Nevertheless, I- $\pi/2$ pulses applied at the beginning of the defocusing period and the end of the refocusing one do not affect the signal intensity since at such times, the terms in the density matrix which contribute to the signal, are proportional to \hat{S}_x operator. Hence, these pulses can be removed and the sequence using R³ recoupling on the indirectly detected channel (denoted HMQC-I-R³ hereafter) is similar to that using SFAM₁ scheme. This sequence is γ -independent and its NMR signal is given by Eq.(3.10).

3.2.2.2. Recoupling applied to the detected isotope.

As said before, the dipolar recoupling is applied to *I* spin, which is detected in this part, whereas the S spin is indirectly detected.

Fig.3.2(c) displays the *D*-HMQC sequence using SFAM₁ recoupling (denoted HMQC-D-SFAM₁ hereafter). The evolution of the density matrix during this sequence is identical to that during HMQC-I-SFAM₁, and hence, the NMR signal is proportional to Eq.(3.8).

Fig.3.2(d) shows the pulse sequence of a novel through-space HETCOR experiments, named HUQC-RN^v_n hereafter, in which the γ -encoded |m| = 1 RN^v_n heteronuclear dipolar recoupling is applied to the detected spin. During the defocusing delay, the longitudinal magnetization of the *I* spin (\hat{I}_z) is converted into antiphase 1Q *I*-spin coherences, $2\hat{I}_{\frac{\pi}{2}+\varphi}\hat{S}_z$, where $\hat{I}_{\frac{\pi}{2}+\varphi} = \hat{I}_x \sin(\varphi) + \hat{I}_y \cos(\varphi)$. The simultaneous $\pi/2$ -pulses on *I* and *S* channels partly convert these antiphase 1Q coherences into heteronuclear MQ coherences, $2\hat{I}_y\hat{S}_y\cos(\varphi)$, and antiphase 1Q *S*-spin coherences, $2\hat{I}_z\hat{S}_y\sin(\varphi)$. Therefore, this sequence is named *D*-HUQC since all coherences of the detected spin are allowed during the t_1 period. The isotropic shift is encoded by the evolution of these coherences during t_1 time. At the end of t_1 , these coherences are converted back into $2\hat{I}_x\hat{S}_z$ and $2\hat{I}_y\hat{S}_z$ operators, which evolve into \hat{I}_z one with coefficients $\sin(\varphi)$ and $\cos(\varphi)$, respectively. This longitudinal *I*-spin magnetization is converted into observable transverse *I*-spin magnetization by the last I- $\pi/2_y$ pulse. Therefore, the NMR signal

of HUQC experiment is proportional to Eq.(3.9), and hence to Eq.(3.10). In particular, the HUQC experiment using γ -encoded $|m| = 1 RN_n^{\nu}$ heteronuclear dipolar recoupling is γ -independent.

As explained above, the RN_n^{ν} recoupling can be replaced by a R³ one bracketed by two $\pi/2$ pulses with phase -y and y. Hence, the sequence of HUQC experiment using R³ recoupling (denoted HUQC-R³ hereafter) is identical to the HMQC-D-SFAM₁ sequence (**Fig.3.2(c)**), but both heteronuclear MQ coherences and 1Q *S*-spin coherences evolve during the t_1 time.

We also introduce experiments using RN_n^{ν} or R^3 recoupling to correlate *I-S* MQ coherences with the *I*-spin 1Q ones. The pulse sequences of these variants of *D*-HMQC experiments (denoted HMQC-D- RN_n^{ν} and HMQC-D- R^3 hereafter) are shown in **Fig.3.3**. These sequences require the application of four I- π pulses during the t_1 period. In principle, their signals are identical to that of HUQC experiments. However, we show below using spin dynamics simulations that the additional I- π pulses decrease its robustness to CSA of the *I* spin (hereafter called CSA_I). Furthermore, in order to refocus the CSA_I, the four I- π pulses must be rotorsynchronized. Consequently, the period between defocusing and refocusing of the recouplings must be $4kT_R$, whereas that of HMQC-I and HUQC sequences is $2kT_R$, while the spectral width of the indirect dimension is equal to v_R . The pulse programs corresponding to HMQC-I- RN_n^{ν} and HUQC are given in the Appendix.





Fig.3.2. Pulse sequences and coherence transfer pathways of (a-b) HMQC-I experiment using (a) RN_n^{ν} and (b) R^3 or SFAM₁, (c) HMQC-D experiment using SFAM₁ as well as HUQC with R^3 , and (d) HUQC using RN_n^{ν} . In (a) the coherence orders $p_I = \pm 1$ during the t_1 period are selected by a two-step phase cycling, in which the phase of the I- π pulses during the defocusing period and the phase of the receiver are incremented by 180°. Similarly in (b) the phases of $R^3/SFAM_1$ irradiation, the first I- $\pi/2$ - $_y$ pulse and the receiver were incremented by 180° to select $p_I = \pm 1$ during t_1 . For (b,c), $p_S = \pm 1$ was selected during t_1 by incrementing the phase of the first S- $\pi/2_x$ pulse and the receiver by 180°. Quadrature detection along the indirect dimension was achieved using the States-TPPI procedure, [48] by incrementing the phase of the I-pulses following the t_1 period.



Fig.3.3. Pulse sequences and coherence transfer pathways of HMQC-D experiment using (a) RN_n^{ν} or (b) R³ recoupling. The coherence orders of the *S*-spin, $p_S = \pm 1$, during the t_1 period were selected by incrementing the phase of the first S- $\pi/2$ pulse and the receiver by 180°. Quadrature detection along the indirect dimension was achieved using the States-TPPI procedure,[48] by incrementing the phase of the second S- $\pi/2$ pulse.

3.3. Simulations and experimental section

3.3.1. Numerical simulations for an isolated ¹³C-¹⁵N spin pair

All numerical simulations of spin dynamics were performed with the SIMPSON software (version 4.1.1).[**36**] The powder average was calculated using 168 { α_{MR} , β_{MR} } pairs and 13 γ_{MR} angles. The 168 { α_{MR} , β_{MR} } Euler angles, which relate the molecular and rotor frames, were selected according to the REPULSION algorithm,[**37**] while γ_{MR} angle was equally stepped from 0 to 360°. The spin system was an isolated ¹³C-¹⁵N spin pair. Simulations were performed for two spin-1/2 isotopes in order to limit the size of the density matrix and accelerate the simulations. The ¹³C-¹⁵N dipolar coupling constant was $b_{IS}/(2\pi) = 409$ Hz, which corresponds to the typical ²⁷Al-³¹P dipolar couplings for Al-O-P bonds found in alumino-phosphate materials. The CSA_I value is indicated in the figure captions, its asymmetry parameter is null, and the orientation of its principal axis systems with respect to the ¹³C-¹⁵N vector is described by the Euler angles (0, 30°, 0).

For all simulations, the static magnetic field was fixed at $B_0 = 18.8 \text{ T} (v_{0,13\text{C}} = 201.2, v_{0,15\text{N}} = 81.14 \text{ MHz})$. The MAS frequency was $v_R = 20 \text{ kHz}$, except in **Figs.3.11** - **3.14**. We simulated the powder averaged signal corresponding to HMQC-I sequence with ¹³C detection, ¹³C-{¹⁵N} hereafter, using SFAM₁, R18⁵₄, R10²₂, R16⁵₃, R14⁵₂ and R³ recoupling schemes. We also simulated ¹³C-{¹⁵N} HMQC-D sequences using the same recoupling schemes as well as ¹³C-{¹⁵N} HUQC using RN^{ν}_n and R³ schemes. Except during the recoupling periods, the rf nutation frequencies were equal to 100 kHz during the pulses applied to ¹³C and ¹⁵N isotopes. The transfer efficiency is defined with respect to the ¹³C signal detected after a spin echo. The rf nutation frequencies during the recoupling period were fixed to their theoretical value (see **Table 3.1**) for RN^{ν}_n schemes and v_R for R³ scheme, except in **Figs.3.6** - **3.8**. For SFAM₁, the peak rf amplitude, v_1^{max} , and carrier frequency modulation, Δv_{ref}^{max} , were fixed to 70 and 50 kHz at $v_R = 20$ kHz and 210 and 150 kHz at $v_R = 60$ kHz, except in **Figs.3.9** and **3.11**.

3.3.2. NMR experiments

Experiments were performed on a wide-bore 9.4 T and a narrow-bore 18.8 T Bruker spectrometers equipped with Avance II and III consoles, respectively. Spectra were recorded with 3.2 mm triple resonance HXY MAS probes. Rotors were fully filled with the sample.

3.3.2.1. ¹³C-{¹⁵N} correlations.

The ¹³C and ¹⁵N isotropic chemical shifts were directly referenced to 43.67 ppm and 32.3 ppm for α -Glycine peaks, respectively. ¹³C-{¹⁵N} HMQC-I, HMQC-D and HUQC experiments were performed on a sample of 98% $[2^{-13}C, {}^{15}N]$ glycine (C₂H₅NO₂) containing a mixture of α and γ polymorphs. The sample was purchased from CortecNet and used without purification. The experiments were carried out at $B_0 = 9.4$ T and $v_R = 10$ kHz except in Figs.3.17. The sequences of Figs.3.2 and 3.3 have been combined with a preliminary ramped ${}^{1}H \rightarrow {}^{13}C CP$ transfer to create ¹³C transverse magnetization, which was converted into ¹³C longitudinal magnetization in the case of HMQC-I-R N_n^{ν} experiment (see Fig.3.2(d)). The CP contact time was 1.5 ms. The ¹³C nutation frequency during CP was 44 kHz, whereas the ¹H nutation frequency was ramped from 54 to 77 kHz. During the remaining parts of the sequences, a SPINAL-64 decoupling with rf nutation frequency of 90 kHz was applied to the ¹H channel.[38] Except during the recoupling, the rf nutation frequencies of the $\pi/2$ and π pulses were $v_{1,13C}$ = 42 and $v_{1,15N} = 32$ kHz. The rf nutation frequencies during the recoupling periods were fixed to their theoretical value (**Table.3.1**) for RN_n^{ν} scheme and $v_1 = v_R = 10$ kHz for R^3 scheme. For SFAM₁ recoupling, the v_1^{max} and $\Delta v_{\text{ref}}^{\text{max}}$ values were fixed to 16 or 26(for ¹⁵N indirect or ¹³C direct) and 40 kHz. The ¹³C-{¹⁵N} HMQC-I, HMQC-D and HUQC 1D and 2D spectra resulted from averaging 8 transients with a recycle delay of 3 s and 64 t_1 increments for the 2D ones. The spectral intensities were normalized with respect to those observed after the same ${}^{1}H \rightarrow$ ¹³C CP 1D spectrum.

3.3.2.1. ³¹P-{²⁷Al} and ²⁷Al-{³¹P} correlations.

The ³¹P and ²⁷Al isotropic chemical shifts were referenced to 85% H₃PO₄ and a 1 M solution of Al(NO₃)₃, respectively. ²⁷Al-{³¹P} HMQC-I, ³¹P-{²⁷Al} HMQC-D and HUQC experiments were performed on two crystalline alumino-phosphate materials, VPI-5 (Al₃(PO₄)₃(H₂O)₅) and Na₇(AlP₂O₇)₄PO₄ (called (1) in the following) at $v_R = 20$ kHz and $B_0 = 9.4$ T for VPI-5 and $B_0 = 18.8$ T for (1), which has been prepared according to the procedure previously reported.[39] Contrary to VPI-5, (1) contains ³¹P sites subject to large CSA_{31P} (up to 85 ppm).[25] The heteronuclear dipolar recoupling was always applied on the ³¹P channel since the number of

pulses applied to the quadrupolar nucleus must be minimized. The rf nutation frequencies of $\pi/2$ and π pulses were $v_{1,31P} = 74$ and $v_{1,27A1} = 9.3$ kHz (to achieve selective excitation of the central transition (CT)). For ²⁷Al-{³¹P} experiments, a preliminary Hyper-Secant (HS) pulse lasting 3 ms was used to enhance the polarization of the ²⁷Al CT by manipulating the population of satellite transitions.[40] The optimal HS enhancement was obtained with an rf field of 11 kHz and a frequency sweep from 180 to 160 kHz during 3 ms. The nutation frequencies during the recoupling periods were fixed to their theoretical value (**Table.3.1**) for RN^{*v*}_{*n*} scheme and $v_1 = v_R = 20$ kHz for R³. For SFAM₁ recoupling, the v_1^{max} and Δv_{ref}^{max} values were fixed to 42 and 60 kHz. The ²⁷Al-{³¹P} HMQC-I, ³¹P-{²⁷Al} HMQC-D and HUQC 1D and 2D spectra result from averaging 8/16 transients with a recycle delay of 1/20 s and 200/90 t_1 increments for the 2D ones. The intensities have been normalized with respect to that of either the ³¹P signal after a $\pi/2$ hard-pulse (**Fig.3.18(b**)), or the ²⁷Al signal after a soft CT-selective $\pi/2$ pulse (**Fig.3.18(a**)).



Fig.3.4. Crystal structure of (a) α -Glycine, (b) γ -Glycine, (c) Na₇(AlP₂O₇)₄PO₄ and (d) VPI-5 (Al₃(PO₄)₃(H₂O)₅). These figures are adopted from CIF files with Diamond software.

3.4. Results and discussion

3.4.1. Numerical simulations

3.4.1.1. Build up curves.

Fig.3.5 shows the simulated build-up curves of ¹³C-{¹⁵N} HMQC-I experiments for an isolated ¹³C-¹⁵N spin pair in the absence of any CSA. As expected, the reduced orientation dependence of γ -independent sequences, HMQC-I-R N_n^{γ} and -R³, leads to a stronger oscillation of signal intensity versus τ than for HMQC-I-SFAM₁, the signal of which depends on $\gamma_{PR}^{D,IS}$ angle. Furthermore, the maximal transfer efficiency of γ -independent sequences is about 25% higher than that of HMQC-I-SFAM₁. These results are consistent with Eqs.(3.8) and (3.10). Furthermore, the optimal recoupling times agree with the τ^{opt} expressions and κ values given in the section II. Owing to its large scaling factor, R³ scheme produces the fastest transfer and hence must be advantageous in the case of fast signal decay. We checked [not shown] that the build-up curves of HMQC-D and HUQC sequences are identical to their HMQC-I counterpart using the same recoupling schemes.



Fig.3.5. Simulated build-up curves of ¹³C-{¹⁵N} HMQC-I experiments of an isolated ¹³C-¹⁵N spin pair without any CSA, using SFAM₁, RN_n^{ν} and R^3 recoupling (see the labels of the curves on the right of the figure).

3.4.1.2. Robustness to rf inhomogeneity.

There exists an inherent distribution of rf field amplitudes in the sample coil of MAS probes, mostly along the axis of solenoid coil. Typically the rf field amplitude is maximal at the center of the coil and drops by about 50% near the edges. [41] The simulated signal intensity of ¹³C-{¹⁵N} HMQC-I, HMQC-D-SFAM₁ and HUQC experiments on an isolated ¹³C-¹⁵N spin pair is shown as function of v₁₁ or v₁^{max} shown either in absolute (**Fig.3.6**) or in relative (**Fig.3.7**) value. SFAM₁ exhibits the highest robustness to rf inhomogeneity owing to the modulation of the rffield, whereas the R³ scheme is the least robust. The RNⁿ schemes, which are γ -encoded as R³, are nevertheless more robust to rf-field variation. In the absence of CSA₁ (compare **Fig.3.6**(a) and (c) or **3.7**(a) and (c)), the robustness of RNⁿ recoupling to rf-field is higher when the recoupling is applied to the indirectly detected spin. For both R³ and RNⁿ recoupling, the robustness to rf maladjustment or inhomogeneity increases when the irradiated spin is subject to CSA₁. Such effect has already been reported for R³ irradiation.[23,26]

Similar simulations for HMQC-D-R³ and $-RN_n^{\nu}$ experiments show that their efficiencies strongly decrease for CSA_I = 10 kHz (**Fig.3.8**), and hence that the HUQC method should be preferred for direct recoupling. This limited efficiency of HMQC-D-R³ and $-RN_n^{\nu}$ has been confirmed experimentally (not shown), and hence these sequences will not be analyzed anymore.



Fig.3.6. Simulated ¹³C signal versus the applied rf field of the recoupling scheme, $v_1(RN_n^{\nu} \text{ or } R^3)$ or v_1^{max} for SFAM₁, for ¹³C-{¹⁵N} experiments: (a,b) HMQC-I and (c,d) HMQC-D-SFAM₁ and HUQC using RN_n^{ν} and R^3 recoupling. CSA_I = 0 (a,c) and 10 kHz (b,d). Recoupling times were fixed to their optimal values (**Figs.3.5**).



Fig.3.7. Simulated ¹³C signal versus the ratio between the difference of the applied and nominal rf-fields and the nominal rf-field of the recoupling scheme for ¹³C-{¹⁵N} HMQC-I, HMQC-D-SFAM₁ and HUQC experiments for CSA_I of (a,c) 0 and (b,d) 10 kHz. The recoupling times were fixed to their optimal values (**Figs.3.5**).



Fig.3.8. Simulated ¹³C signal versus the applied rf field, $v_1(RN_n^{\nu} \text{ or } R^3)$ or v_1^{max} for SFAM₁, of the recoupling scheme for ¹³C-{¹⁵N} HMQC-D experiments for CSA_{15N} = 0 (a) and 10 kHz (b). The recoupling times were fixed to their optimal values (**Figs.3.5**).
3.4.1.3. Robustness to offsets.

Fig.3.9 compares the robustness to offset of ¹³C-{¹⁵N} HMQC-I, HMQC-D-SFAM₁ and HUQC sequences. SFAM₁ recoupling is always the most robust sequence to resonance offset owing to the modulation of the carrier frequency position. Among the γ -encoded schemes, R14⁵₂ and R³ benefit respectively from the highest and lowest robustness to offset owing to their largest (**Table.3.1**) and smallest nominal rf-fields. The robustness to offset is globally similar when the recoupling is applied to the indirectly detected or detected isotope. As these recoupling schemes are rotor-synchronized, the offset bandwidth increases for increasing MAS frequency (**Fig.3.11**).



Fig.3.9. Simulated ¹³C signal versus the resonance offset on the recoupled I channel for ¹³C- $\{^{15}N\}$ (a) HMQC-I experiments and (b) HMQC-D-SFAM₁ and HUQC with RN_n^{ν} and R^3 recoupling and CSA_I = 10 kHz. Recoupling times were fixed to their optimal values (**Figs.3.5**).

3.4.1.4. Robustness to CSA_I.

Fig.3.10 shows the variation of the signal intensity of ${}^{13}C-{}^{15}N$ HMQC-I, HMQC-D-SFAM₁ and HUQC sequences versus CSA_I. SFAM₁ scheme is the least robust since its modulation during the rotor period interferes with the modulation of the rf carrier frequency. R^3 scheme benefits from the highest robustness to CSA_I (see also **Fig.3.6** and **3.7**).

The robustness to CSA of RN_n^{ν} schemes is lower than that of R^3 since the CSA_I results in imperfect π -pulses. Nevertheless, the deviation from the π -pulse is inverse proportional to v_{1I} , and hence the robustness increases with the nominal rf-field. For the same reason, the robustness to CSA_I increases with v_R since the recoupling schemes are rotor-synchronized (**Fig.3.11(c)** and (**d**)).



Fig.3.10. Simulated ¹³C signal intensity versus CSA_I for ¹³C-{¹⁵N} experiments: (a) HMQC-I and (b) HMQC-D-SFAM₁ and HUQC with RN_n^{ν} and R^3 recoupling. Recoupling times were fixed to their optimal values (**Figs.3.5**).



Fig.3.11. Simulated ¹³C signal intensity at $v_R = 60$ kHz versus (a,b) the resonance offset and (c,d) the CSA_I of the irradiated isotope for ¹³C-{¹⁵N}: (a,c) HMQC-I experiments and (b,d) HMQC-D-SFAM₁ and HUQC using RN_n^{ν} and R^3 recoupling. In (a,b) CSA_I = 10 kHz, whereas in (c,d), the recoupling is applied on resonance.

3.4.1.5. MAS frequency variations.

Fig.3.12 displays the variations of signal intensities of ¹³C-{¹⁵N} HMQC-I, HMQC-D-SFAM₁ and HUQC sequences versus v_R. SFAM₁ scheme is most sensitive to variation in v_R since it is non- γ -encoded. The sensitivity to MAS variations is especially high when the SFAM₁ recoupling is applied to the detected nucleus (**Fig.3.12(b**)) since in that case, the CSA_I is imperfectly refocused when v_R \neq 20 kHz, which decreases the signal intensity. As expected the γ -encoded schemes exhibit better robustness to MAS fluctuations. Furthermore, for those recoupling methods, the robustness to v_R is similar when the recoupling is applied to the detected or indirectly detected isotope (compare **Fig.3.12(a)** and (**b**)). As seen by comparing **Fig.3.12** and **3.13**, the tolerance to v_R deviations does not depend on its value in Hz, and hence, the relative variations in MAS frequency must be smaller at high MAS frequency. In the case of larger CSA (29 kHz), R³, R14⁵₂ and R16⁵₃ schemes are more robust to the v_R fluctuations than the other sequences (**Fig.3.14**).



Fig.3.12. Simulated ¹³C signal intensity versus v_R for ¹³C-{¹⁵N} experiments: (a) HMQC-I and (b) HMQC-D-SFAM₁ and HUQC using RN_n^{ν} and R^3 recoupling with CSA_I = 10 kHz. Recoupling times were fixed to their optimal values (**Figs.3.5**).



Fig.3.13. Simulated ¹³C signal intensity around $v_R = 60$ kHz for ¹³C-{¹⁵N} experiments: (a) HMQC-I and (b) HMQC-D-SFAM₁ and HUQC experiments using RN_n^{ν} and R^3 recoupling with CSA_I = 10 kHz. The recoupling times were fixed to their optimal values (**Figs.3.5**).



Fig.3.14. Simulated ¹³C signal intensity around $v_R = 20$ kHz for ¹³C-{¹⁵N} HMQC-D-SFAM₁ and HUQC experiments when CSA_{13C} = 27.5 kHz, which is the shielding value of P₁ in sample (1) at 18.8 T.

3.4.2. Experimental verifications

3.4.2.1. ¹³C-{¹⁵N} D-HETCOR

Fig.3.15(a) displays the experimental build-up curves of the ¹³C^{α} signal of [2-¹³C,¹⁵N] glycine in 1D ¹³C-{¹⁵N} HMQC-I spectra. The CSA_{15N} of the NH₃⁺ group is equal to 9.7 ppm, i.e. 400 Hz at $B_0 = 9.4$ T.[42] The experimental build-up curves agree well with the simulated ones shown in **Fig.3.5** with null CSA_{15N}. The major difference is the lower transfer efficiency for HMQC-I-R³ sequence, which stems from its poor robustness to rf field inhomogeneity. For HMQC-I experiments, the highest signal intensity is achieved using R N_n^{ν} recoupling since these methods combine γ -encoding and higher robustness to rf-field than R³ scheme.

Nevertheless, when the recoupling is applied to the detected ¹³C nucleus, subject to CSA_{13C} = 19.43 ppm, i.e. 1.95 kHz at $B_0 = 9.4$ T,[43] SFAM₁, R18⁵₄, R10³₂ and R16⁵₃ schemes produce similar intensities (**Fig.3.15(b)**) since the RN^{ν}_n recoupling techniques are less robust to rf inhomogeneity when applied to the detected spin (**Table.3.3**). **Fig.3.16(a)**,(**b**) and (**c**),(**d**) show respectively the ¹³C-{¹⁵N} HMQC-I and HMQC-D/HUQC 2D spectra of glycine, which exhibit two cross-peaks, one correlating the de-shielded ¹³C signal to the shielded ¹⁵N one, assigned to α -glycine and the other one to γ -glycine.[44] As seen in ¹³C slices of these 2D spectra, RN^{ν}_n recoupling schemes always produce higher signal intensity than SFAM₁ and R³ schemes.

We measured experimentally the robustness to rf-field inhomogeneity and offset of the various recouplings and the results are given in **Table.3.3**. As already observed in numerical simulations, SFAM₁ recoupling exhibits the highest robustness to rf-field inhomogeneity and offset and RN_n^{ν} schemes are more robust to offset and rf inhomogeneity than R³. Furthermore, the RN_n^{ν} recoupling schemes are more sensitive to the offset and rf field when they are applied to the detected isotope. Experiments also confirm that the non- γ -encoded SFAM₁ sequence is the least robust to variation in MAS frequency (**Fig.3.17**).

Table.3.3. Experimental robustness to rf-inhomogeneity, R_{rf} , and offsets, Δv_{ref} , for the ${}^{13}C^{\alpha}$ signal of [2- ${}^{13}C$, ${}^{15}N$] glycine in ${}^{13}C$ -{ ${}^{15}N$ } HMQC-I, HMQC-D-SFAM₁ and HUQC 1D experiments.

Scheme	HMQC-I		HMQC-D/HUQC	
	^a R _{rf}	$^{\rm b}$ $\Delta u_{ m ref}/ m kHz$	^a R _{rf}	$^{\rm b}$ $\Delta u_{ m ref}/ m kHz$
R18 ⁵ 4	0.29	9.8	0.20	7.5
R10 ³ 2	0.30	9.8	0.21	7.3
R16 ⁵ 3	0.28	9.8	0.23	7.0
R14 ⁵ 2	0.31	9.0	0.25	7.5
R ³	0.14	7.0	0.09	7.0
SFAM ₁	1.01	35	1.46	20

^a R_{rf}, is defined as the ratio between the total rf-range where the signal is larger than half its maximum and the nominal nutation frequency. ^b Δv_{ref} is defined as the frequency offset range on the recoupled channel, for which the signal intensity is larger than the half maximum of the signal.



Fig.3.15. Experimental build-up curves of ${}^{13}C^{\alpha}$ signal of $[2 \cdot {}^{13}C, {}^{15}N] \alpha$ -glycine for ${}^{13}C \cdot \{{}^{15}N\}$ 1D experiments: (a) HMQC-I, (b) HMQC-D-SFAM₁ and HUQC using RN_n^{ν} and R^3 recoupling.



Fig.3.16. Experimental ¹³C-{¹⁵N} (a,b) HMQC-I and (c,d) HMQC-D-SFAM₁ and HUQC with RN_n^{ν} and R^3 recoupling 2D spectra of [2-¹³C,¹⁵N] glycine containing a mixture of α and γ polymorphs. The recoupling times were fixed to their optimal values determined from **Fig.3.15**.



Fig.3.17. Experimental ¹³C^{α} signal versus v_R for ¹³C-{¹⁵N} experiments: (a) HMQC-I and (b) HMQC-D-SFAM₁ and HUQC experiments using RN_n^{ν} and R^3 recoupling. The recoupling times were fixed to their optimal values determined from **Fig.3.15**.

3.4.2.2. ²⁷Al-³¹P *D*-HETCOR on VPI-5 at 9.4 T.

Hydrated VPI-5 contains three equally populated sites for Al and P, which are coordinated with each other through one bridging oxygen. Under MAS at 9.4 T, the ³¹P resonances are well resolved, but only two ²⁷Al peaks are observable (Al₁ and Al_{2,3}). The resonance labeled Al₁ at \approx -20 ppm represents a site between the fused four-membered rings. Two water molecules complete an octahedral coordination sphere for Al₁ and render inequivalent the tetrahedrally coordinated Al₂ and Al₃ sites at \approx 40 ppm, as well as the phosphorus sites P₂ and P₃ in the sixmembered rings. The CSA_{31P} are equal to 26.3, 33.7 and 34.6 ppm, i.e. 4.26, 5.46 and 5.60 kHz for P₁, P₂ and P₃ sites, respectively at $B_0 = 9.4$ T. ²⁷Al quadrupolar parameters are equal to (C_Q (MHz), η_Q) = (3.5,0.91), (1.1,0.3) and (2.2,0.8) for Al₁, Al₂ and Al₃, respectively [46]. The specific connectivities between various nuclei are as follows: Al₁ (2P₁, P₂, P₃), Al₂ (P₁, 2P₂, P₃).

Fig.3.18 shows the build-up curves of ²⁷Al_{2,3} signal in ²⁷Al-{³¹P} HMQC-I and ³¹P₂ signal in ³¹P-{²⁷Al} HMQC-D-SFAM₁ and HUQC spectra of VPI-5, and **Fig.3.19** the corresponding 2D spectra and 1D slices. SFAM₁ recoupling always results in the fastest build-up (**Fig.3.18**). For HMQC-I experiments, the highest intensity is achieved using SFAM₁ (**Figs.3.18(a)** and **3.19(a)-(c)**). Conversely HMQC-D-SFAM₁ and HUQC-RN^{ν}_n sequences produce similar crosspeak intensities (Fig.3.18(b) and 3.19(d)).

Table.3.4 compares the robustness to rf inhomogeneity and offset of the various recouplings in VPI-5. As already observed for ¹³C-{¹⁵N} D-HETCORs, SFAM₁ recoupling exhibits the highest robustness to offset and rf inhomogeneity. The RN_n^{ν} schemes are more robust to rf field variation than R³. For RN_n^{ν} and R³ methods, the robustness to rf inhomogeneity and offset is higher when the recoupling is applied to the indirectly detected spin.

Fig.3.20 compares the robustness to MAS frequency of all HMQC and HUQC sequences. For HMQC-I experiment, RN_n^{ν} and R^3 techniques benefit from the highest robustness to variations in MAS frequency (**Fig.3.20(a**)). In the case of recoupling schemes applied to the detected spin (**Fig.3.20(b**)), the highest robustness is achieved by R^3 scheme but RN_n^{ν} ones are also much more robust to MAS frequency fluctuations than SFAM₁.

Table. 3.4. Experimental robustness to rf-inhomogeneity, R_{rf} , and offsets, Δv_{ref} , observed in 1D experiments of VPI-5 for the ²⁷Al_{2,3} signal in ²⁷Al-{³¹P} HMQC-I and for the ³¹P₂ signal of ³¹P-{²⁷Al} HMQC-D-SFAM₁ and HUQC.

Scheme	HMQC-I		HMQC-D/HUQC	
	R _{rf}	$\Delta v_{ref}/kHz$	R _{rf}	$\Delta \nu_{ref}/kHz$
R18 ⁵ ₄	0.41	22.3	0.33	16.7
R10 ³ 2	0.42	24.2	0.26	16.2
R16 ⁵ 3	0.45	22.6	0.27	16.2
R14 ⁵ 2	0.39	22.9	0.30	16.2
R ³	0.28	23.7	0.18	16.0
SFAM ₁	1.15	27.5	1.61	25.0



Fig.3.18. Experimental build-up curves observed with 1D experiments for VPI-5. (a) ${}^{27}Al_{2,3}$ signal with ${}^{27}Al_{1}{}^{31}P$ HMQC-I and (b) ${}^{31}P_{2}$ signal with ${}^{31}P_{1}{}^{27}Al$ HMQC-D-SFAM₁ and HUQC with RN_{n}^{ν} and R^{3} recoupling.





Fig.3.19. Experimental (a-c) ²⁷Al-{³¹P} *D*-HMQC-I and (d) ³¹P-{²⁷Al} HMQC-D-SFAM₁ and HUQC (R³ and R10³₂) 2D spectra and 1D slices of VPI-5 at $B_0 = 9.4$ T with $v_R = 20$ kHz. The recoupling times were fixed to their optimal values (**Fig.3.18**).



Fig.3.20. Experimental signal observed with 1D experiments of VPI-5 versus v_R of (a) ${}^{27}Al_{2,3}$ for ${}^{27}Al_{31}P$ HMQC-I and (b) ${}^{31}P_2$ for HMQC-D-SFAM₁ and HUQC with RN_n^{ν} and R^3 recoupling.

3.4.2.3. ³¹P-{²⁷Al} HMQC-D-SFAM₁ and HUQC on Na₇(AlP₂O₇)₄PO₄ at 18.8 T.

Numerical simulations have shown that RN_n^{ν} schemes are more robust to CSA_I than SFAM₁ recoupling. Therefore, the ³¹P-{²⁷Al} sequences were tested with direct recoupling on Na₇(AlP₂O₇)₄PO₄ sample, called (**1**) hereafter, which contains three P sites with two of them subject to large CSA (**Fig.3.21**). Their CSA parameters are (δ_{aniso} (ppm), η_{CSA}) = (85, 0.6), (10.5, 0.85) and (75.7, 0.3) for P₁, P₂ and P₃ sites, respectively,[25] which is equivalent to CSA_{31P} = 27.5, 3.4 and 24.5 kHz at 18.8 T. This sample also contains one ²⁷Al site with C_Q = 5.3 MHz and η_Q = 0.46.

Fig.3.22 compares the F1 slices of P₁ in sample (1), which presents the largest CSA_{31P}, for 2D spectra recorded with ³¹P-{²⁷A1} HMQC-D-SFAM₁ and HUQC with RN_n^{ν} and R^3 recoupling. R³ and $R10_2^3$ schemes produce the smallest and largest signal intensities, respectively. However, one notices the very large differences in the *t*₁-noise, lower for R³, R16₃⁵ and R14₂⁵ schemes than for R10₂³ and SFAM₁ since the former recouplings are more robust to v_R than the latter ones. As a result, the S/N ratios are in the order: $R16_3^5 > R14_2^5 > R10_2^3 >> R18_4^5$. It must be noted that the order of the S/N is fully correlated to the robustness to spinning speed fluctuations (**Fig.3.13**), except for R³ which is very sensitive to rf-inhomogeneity.

It has recently been shown that the t_1 -noise is mainly related to the 2nd-order dipolar-CSA crossterms, and that one way to decrease this noise is to slightly de-synchronize the sequence [47]. We have used this trick with the HUQC-R10³₂ experiment by slightly increasing the spinning speed to $v_R = 20.1$ kHz, without changing the pulse timing based on $v_R = 20$ kHz. The corresponding F1 slices are shown in **Fig.3.23**. This de-synchronization slightly decreases the efficiency, but as expected largely improves the S/N ratio of the P₁ cross-peak. However, it introduces one additional parameter, the spinning speed which must be slightly optimized with respect to its theoretical value.



Fig.3.21. ³¹P and ²⁷Al single hard-pulse spectra of Na₇(AlP₂O₇)₄PO₄ at $B_0 = 9.4$ T and $v_R = 20$



Fig.3.22. Na₇(AlP₂O₇)₄PO₄: experimental F1 slices observed for P₁, which presents the largest CSA_{31P} = 27.5 kHz, at $B_0 = 18.8$ T and $v_R = 20$ kHz with HMQC-D-SFAM₁ and HUQC with R10³₂, R16⁵₃, R14⁵₂ and R³ recoupling. One observes very large differences in sensitivity, with HUQC-R10³₂ and -R16⁵₃ providing the largest and the smallest S/N, respectively.



Fig.3.23. Experimental F1 slices of ³¹P-{²⁷A1} HUQC-R10³₂ of Na₇(AlP₂O₇)₄PO₄ at $B_0 = 18.8$ T, either synchronized or unsynchronized with $v_R = 20$ or 20.1 kHz, respectively, both with the same τ values based on $v_R = 20$ kHz

3.5. Conclusion

We have introduced symmetry-based heteronuclear dipolar recoupling schemes, which are γ -encoded and result in rapid dipolar dephasing by reintroducing the space component |m| = 1for the heteronuclear dipolar coupling. These recoupling schemes have been incorporated into novel sequences to correlate half-integer spin quadrupolar nuclei and spin-1/2 isotopes, other than ¹H and ¹⁹F. These heteronuclear correlation sequences are γ -independent and hence their signal is in principle 25% higher than that of their counterparts using non- γ -encoded recoupling schemes, such as SFAM₁. Furthermore, they are more robust to the CSA of the irradiated spin and the fluctuations of the MAS frequency. Such improved robustness reduces the t_1 -noise in the case of spin-1/2 nuclei subject to large CSA. In addition, the γ -encoded $|m| = 1 RN_n^{\gamma}$ recoupling techniques, such as $R18_4^5$, $R10_2^3$, $R16_3^5$ and $R14_2^5$, are more robust to rf inhomogeneity than their R³(q = 1) cousin. Nevertheless, the γ -encoded |m| = 1 recoupling techniques are less robust to rf inhomogeneity and offset than SFAM1 method. ³¹P-²⁷Al heteronuclear correlation experiments show that (i) SFAM₁ recoupling leads to higher transfer efficiency when the spin-1/2 nucleus is indirectly detected and subject to small CSA, whereas (ii) R16 $_3^5$ scheme produces the highest S/N ratio in the case of detection via spin-1/2 nuclei subject to large CSA.

3.6. References

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Chapter 4: General conclusion and perspectives

4.1. General conclusion

This thesis has focused on the development and application of novel through-bond and through-space correlation solid-state NMR experiments involving half-integer quadrupolar nuclei. We have notably improved the sensitivity of the correlation experiment and extended the application range of the correlation experiment involving half integer spin quadrupolar nuclei. In main two part, main achievement and new insights are as follow:

(1) ⁷⁷Se{⁷¹Ga} *J*-RINEPT-CPMG, ⁷¹Ga{⁷⁷Se} *J*- and *D*-HMQC-QCPMG and ⁷¹Ga split- t_1 z-filter STMAS-QCPMG sequences were developed and applied to investigate the structure of gallium selenide materials. As a result, ⁷⁷Se-⁷¹Ga HETCOR and ⁷¹Ga STMAS experiments were acquired within reasonable experimental time using the developed sequences. The analytical expressions for heteronuclear *J* coupling estimation were extended to inorganic materials with 3D bond connectivity. ⁷⁷Se-⁷¹Ga HETCOR experiment indicates that the sample of β -Ga₂Se₃ crystal is composed of Annealed phase and Quenched phase. This Quenched phase only contains Se^{III} sites and ⁷¹Ga nuclei located in symmetrical environment but exhibiting a large distribution of isotropic chemical shifts. In the case of 20Ga₂Se₃-80GeSe₂ glass sample, 2D HETCOR ⁷⁷Se projection spectra was deconvoluted into 6 distinct Se sites bonded to Ga atom. These results have never been reported previously, notably because of the lack of sensitivity of HETCOR experiment. The combination with CPMG acquisition can open the door to the new application for HETCOR and STMAS experiments.

(2) Novel Dipolar-Heteronuclear Universal Quantum Correlation with γ encoded heteronuclear dipolar recoupling on direct channel (*D*-HUQC-DR) was developed in order to increase the sensitivity, compared to conventional *D*-HMQC with R³. MAS fluctuation cause t_1 noise for 2D experiment in solid and t_1 noise reduces the sensitivity of 2D experiment. *D*-HUQC experiment with γ encoded *R* symmetry-based recoupling reintroducing m = 1 spatial component of heteronuclear dipolar couplings has similar robustness to MAS fluctuation than the one using R³ recoupling. Hence, this method overcomes the t_1 noise problem for the aluminophosphate materials with large CSA. Furthermore, R symmetry recoupling with m = 1 spatial component has much better robustness to RF inhomogeneity than R³ recoupling which lead to 3 times higher efficiency. This new pulse sequence partially solves the t_1 noise issue and will be useful for the condition of ultra-high field (> 18.8 T), in which CSA could be very large, and unstable MAS frequency (such as very fast MAS and DNP experiment).

4.2. Perspectives

4.2.1. Correlation experiment for Gallium Selenide material

DFT calculation of β -Ga₂Se₃ crystal and Ga₂Se₃-GeSe₂ glass

It is revealed that the structure of β -Ga₂Se₃ crystal possesses complicated structure including Quenched phase. It may be possible to reveal the detailed structure by performing DFT calculation using the information of ⁷¹Ga and ⁷⁷Se chemical shifts, ⁷¹Ga-⁷⁷Se *J* coupling constants, ⁷¹Ga quadrupolar parameters (C_Q and η_Q) and ⁷⁷Se CSA. Similarly, DFT calculation will be useful to support the assignment of ⁷⁷Se signals for 2D HETCOR ⁷⁷Se projection spectrum in glass sample.

HETCOR experiment with population transfer at higher field

Further sensitivity improvement of ⁷¹Ga-⁷⁷Se HETCOR can be performed at higher magnetic field. The CT spectrum of half-integer quadrupolar nuclei will be narrowed and population transfer pulse could be applied at the beginning of HETCOR sequence. Population transfer pulse was not applied to the present experiment in the thesis because of too broad ⁷¹Ga line width at 9.4 T. If the combination population transfer and high field is possible, the sensitivity could be further increased, even if CSA and chemical shift distribution, which broaden the ⁷⁷Se spectrum, is also increased. The improved resolution and sensitivity at high magnetic field can provide additional details on the nature of molecular patterns in gallium selenide materials.

Application to Ga₂Se₃-GeSe₂ glass-ceramics

Ga₂Se₃-GeSe₂ glass-ceramics material benefits from higher mechanical strength than the glass sample, while keeping IR transparency. Moreover, the lens made of glass-ceramics can be molded as those made of glass material. For a glass-ceramics sample, narrow peak occurs in ⁷¹Ga 1D MAS spectra. This narrow peak is similar to that of β -Ga₂Se₃ crystal. The chemical structure and the mechanism of the nucleation could be clarified by using ⁷¹Ga-⁷⁷Se HETCOR experiment and DFT calculation.

Application to other system

Present proposed *J*-RINEPT-CPMG and *J/D*-HMQC-QCPMG sequence could be applied not only to gallium selenide materials but also other difficult system exhibiting broad NMR spectra. Here, CPMG acquisition enhances sensitivity when the observed nuclei possess the property of (i) low natural abundance, (ii) short FID, (iii) long T_2 '. Nevertheless, as mentioned in the introduction part, modified CPMG protocol proposed by R. Siegel et al may make the CPMG acquisition more efficient in non-dilute system. Similarly to *J*-RINEPT sequence, *D*-RINEPT sequence could be combined with CPMG acquisition as well as PRESTO-III-QCPMG sequence. *D*-RINEPT sequence is complementary to *J*-RINEPT for extracting both through space and through bond information in the material. In *D*-RINEPT sequence, appropriate heteronuclear dipolar recoupling sequence could be chosen depending on the application (e.g. $SR4_1^2$ and SFAM instead of R^3).

4.2.2. *γ* independent *D*-HMQC pulse sequence

Utilization of dipolar truncation effect

As mentioned in the introduction, the recoupling method used in *D*-HMQC was mostly non- γ encoded recoupling except for R³. Since these method enables long-range correlation, it is effective for observing the correlation between all spins. On the other hand, γ -encoded recoupling has a dipolar truncation effect. Therefore, in principle it is possible to obtain the correlation of only the nearest neighbor nucleus. By employing the two types of recoupling complementarily, it will be useful for editing the correlation spectrum and it will be possible to obtain more detailed material structure.

The correlation experiment at very high field and with DNP

NMR magnet with very high magnetic fields are being developed. They will notably improve the resolution of half-integer quadrupole nuclei. In the Lille, 1.2 GHz NMR spectrometer is planned to be installed in 2020. On the other hand, a high magnetic field increases the CSA. For non- γ -encoded recoupling, larger CSA decreases the robustness to MAS frequency fluctuations, thus generating larger t_1 noise. The γ -encoded recoupling proposed in this thesis should allow the suppression of t_1 noise even under high magnetic field conditions. In the experiment of DNP, usually carried out at 100 K, MAS fluctuation are also significantly larger than for conventional NMR experiments. DNP-enhanced *D*-HUQC spectra can be acquired, for instance by initially transferring the DNP-enhanced 1H polarization to the detected isotope using CP. The use of *D*-HUQC method under DNP conditions will reduce the t_1 noise and thus improve the sensitivity, allowing the observation of small correlation peaks.

HUQC *m* = 2 recoupling

D-HMQC-DR sequence has been used for the indirect detection of quadrupolar nuclei, such as ¹⁴N, or spin-1/2 isotope exhibiting wide NMR signal, such as ¹⁹⁵Pt, via ¹H nuclei. Heteronuclear dipolar recoupling used here must have the property of homonuclear dipolar decoupling, and SR4²₁ recoupling is often chosen. However, again, high t_1 noise occurs since this recoupling is non- γ -encoded. For these systems, it is expected that this t_1 noise could be suppressed by applying R symmetry recoupling with m = 2 component having the property of homonuclear dipolar decoupling.

Curriculum Vitae

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Research Topics

2018 -: Research scientist at IRC3, AIST, Japan

Development and application of DNP-NMR and advanced SS-NMR methodology for industrial materials

2017 – 2018: Postdoctoral researcher at University of Lille Sciences and Technologies, Supervisor: Prof Olivier Lafon

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2009 – 2014: Bridgestone. Co., Japan

Characterization of composite material in the tire using advanced SS-NMR methodology

2007 – 2009: The University of Tokyo, Supervisor: Prof Masashi Takigawa

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2006 – 2007: Toho University, Supervisor: Prof Yutaka Nishio

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Publications

- Hiroki Nagashima, Grégory Tricot, Julien Trébosc, Olivier Lafon, Jean-Paul Amoureux, Frédérique Pourpoint " 3D correlation NMR spectrum between three distinct heteronuclei for the characterization of inorganic samples: application on sodium alumino-phosphate materials" *Solid state Nuclear Magnetic Resonance* (2017) 84, 1664-170 (2017)
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- 6) <u>Hiroki Nagashima</u>, François Méar, Julien Trébosc, Frédérique Pourpoint, Hervé Vezin, Lionel Montagne, Olivier Lafon "Optimization of paramagnetic dopants to enhance the sensitivity of solid-state NMR" *in preparation*
- 7) <u>Hiroki Nagashima</u>, Aany S. Lilly Thankamony, François Méar, Lionel Montagne, Julien Trébosc, Frédérique Pourpoint, Jean-Paul Amoureux, Gwendal Kervern, Olivier Lafon, "Heteronuclear dipolar recoupling using adiabatic inversion pulses" *in preparation*
- 8) <u>**Hiroki Nagashima**</u>, Frédérique Pourpoint, Julien Trébosc, François Méar, Lionel Montagne, Olivier Lafon "NMR spectroscopy of glass thin-films enhanced by Dynamic Nuclear Polarization" *in preparation*
- 9) Zhehong Gan, Ivan Hung, Yusuke Nishiyama, Olivier Lafon, <u>Hiroki Nagashima</u>, Julien Trébosc, Jean-Paul Amoureux, Ilya Kuprov "Theory of ¹⁴N overtone nuclear magnetic resonance of rotating solids" *in preparation*
- 10) <u>Hiroki Nagashima</u>, Charlotte Martineau, Grégory Tricot, Julien Trébosc, Frédérique Pourpoint, Jean-Paul Amoureux, Olivier Lafon, "Recent developments in NMR studies of aluminophosphate" *in preparation*
- 11) <u>Hiroki Nagashima</u>, Shantanu Lanke, Julien Trébosc, Frédérique Pourpoint, Jean-Paul Amoureux, P. K. Madhu, Vivek Polshettiwar, O. Lafon "Dynamic Nuclear Polarization enhanced NMR spectroscopy of hybrid and inorganic materials" *in preparation*
- 12) <u>Hiroki Nagashima</u>, Frédérique Pourpoint, Julien Trébosc, François Méar, Lionel Montagne, Olivier Lafon, "The review of glass thin film NMR"

Presentations

- Hiroki Nagashima, Julien Trébosc, Frédérique Pourpoint, François Mear, Laurent Calvez, Olivier Lafon, Jean Paul Amoureux, ^{"71}Ga-⁷⁷Se connectivities and proximities in gallium selenide materials probed by solid state NMR" Société Chimique de France (SCF) 2017, Montpellier (France), November 8– 10 2017 Oral presentation
- Hiroki Nagashima, Aany S. Lilly Thankamony, Julien Trébosc, Frédérique Pourpoint, Jean-Paul Amoureux, Olivier Lafon, "Correlation between spin-1/2 and quadrupolar nuclei: high robustness to Magic-Angle Spinning fluctuations" Euromar 2017, Warsaw (Poland), July 2– 6 2017 Oral presentation
- 3) <u>Hiroki Nagashima</u>, Julien Trébosc, Frédérique Pourpoint, François Mear, Laurent Calvez, Olivier Lafon, <u>Jean Paul Amoureux</u>, "⁷¹Ga-⁷⁷Se connectivities and proximities in gallium selenide materials probed by solid state NMR" Euromar 2017, Warsaw (Poland), July 2– 6 2017 Poster presentation

- Hiroki Nagashima, Frédérique Pourpoint, Julien Trébosc, Jean-Paul Amoureux, <u>Olivier</u> <u>Lafon</u>, Solid-state ionics 21, "Insights into atomic-level structure of materials from Dynamic Nuclear Polarization-enhanced NMR spectroscopy", Padua (Italy), June 2017
- 5) <u>Hiroki Nagashima</u>,"⁷¹Ga-⁷⁷Se connectivities and proximities in gallium selenide materials probed by solid state NMR", NMR Grand Basin Parisien meeting, Paris (France), July 2017 *Oral presentation*
- 6) Hiroki Nagashima, Julien Trébosc, Frédérique Pourpoint, François Mear, Laurent Calvez, <u>Olivier Lafon</u>, Philippe Corcos, Jean Paul Amoureux, ^{"71}Ga-⁷⁷Se through-bond and throughspace connectivities analyzed by solid-state NMR", 58th ENC, California(USA), March 26-31,2017
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- 10) Hiroki. Nagashima, F. Pourpoint, J. Trébosc, J.-P. Amoureux, <u>O. Lafon</u>, "Ultra-high field NMR: shining light on the dark sites of heterogeneous catalysts and advanced materials" ICMRBS satellite workshops (Kyoto), August 2016
- 11)Hiroki Nagashima, Julien Trebosc, Frederique Pourpoint, Jean-Paul Amoureux, <u>Olivier</u>
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- 12) <u>Nagashima H</u>, Takigawa M, Nagao Y, Hiroi Z "Magnetic order and dynamics of Pyrochlore oxide Cd₂Os₂O₇ with metal-insulator transition", The Physical Society of Japan Spring meeting, Tokyo, Japan, 2009 *Oral presentation*
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Appendix: Bruker Pulse Program

A.1. D, J-HMQC (with indirect recoupling)-QCPMG pulse sequence

This sequence was used on AV-II Bruker console driven by topspin2.1.

```
;hmqcIR-CPMG.jt
; hmqc with indirect dipolar recoupling and CPMG detection
; Reference sequence : hmqcIR.jt
; CPMG works on Avance-II. It need to modify for Avance-III
; version 1.0 (published online XXX)
 _____
; DESCRIPTION :
; hmqc experiment using SFAM (simultaneous frequency and
; amplitude modulation) or SR4 to generate heteronuclear multiple
; quantum correlation spectra
; you need to run SFAM AU program to generate correct shape pulse
; AUTHOR
; Julien TREBOSC / Hiroki NAGASHIMA
;$COMMENT=HMQC with dipolar recoupling on indirect channel
;$CLASS=Solids
;$DIM=2D
;$TYPE=
;$SUBTYPE=
;$OWNER=Trebosc
;ns : 64*n min, 128*n max
;d1 : recycle delay
;pl1 : =119 dB, not used
;pl21 : RF power level p3/p4
;pl3 : RF power level p1
;pl23 : SFAM/SR4 power level
;p3 : 90 degree pulse @ pl21
;p4 : 180 degree pulse @ pl21
;p1 : 90 degree pulse @pl3
;p16 : SFAM/SR4 dipolar recoupling time
; cnst3 : shape pulse resolution in ns (300ns)
;cnst30 : SFAM offset amplitude
;cnst31 : =MAS spin rate
;cnst0 : factor for second pulse
;13 : SFAM mode (13=1 or 2 for homo dipol decoupl)
;122 : # of echos to be acquired
;d3 : time to allow pulse ringdown, 10 to 100 us
;d6 : enter duration of FID
;FnMODE : States or States-TPPI
;10 : set to 0 automatrically
;ZGOPTNS : -DPRESAT -DdecF3 -DdecF2t1 -DdecF2aq -D DFS -Dopt1D
; -DPRESAT : send presaturation pulses on F1 can be replaced with DS=1 or 2
; -DdecF3 : applyies decoupling during aq on F3
; -DdecF2aq : applyies decoupling during aq on F2 (1H)
; -DdecF2t1 : applyies decoupling during t1 on F2 (1H)
 -D SR4 : use SR4 recoupling
; -D SFAM : use SFAM recoupling (default)
; -D DFS : add DFS enhancement pre-pulse
; -Dopt1D : select only +1 pathway : 1D only, not to be used for 2D
#include <Avancesolids.incl>
#ifdef PRESAT
#include "presat.incl"
#else
#define PRESAT1(f1)
#define presatPH
```

#endif #ifdef decF3 #define dec #define decF3on cpds3:f3 #define decF3off do:f3 #else #define decF3on #define decF3off #endif #ifdef decF2t1 #define decF2 #define decF2t1on cpds2:f2 #else #define decF2t1on #endif #ifdef decF2aq #define decF2 #define decF2aqon cpds2:f2 #else #define decF2aqon #endif #ifdef decF2 #define dec #define tppm #define decF2off do:f2 #else #define decF2off #endif #ifdef dec #include "decouple.incl" #endif #ifdef DFS ;p2 DFS/HS pulse ;cnst1 : (kHz) Start DFS sweep freq. ;cnst2 : (kHz) End DFS sweep freq. ;cnst3 : (ns) time resolution of shape sp1 ;spoffs1 HS offset (spoffs1 < 1/cnst3) ;spnam1 DFS/HS shape : use HS.jt of DFS.jt to regenerate ;sp1 DFS/HS shape power define delay showInASED "showInASED=cnst1+cnst2+cnst3" #define DFSpulse (5u p2:sp1 ph0 5u):f1 #else #define DFSpulse #endif define delay del3 "del3=d3-2u" define loopcounter tmpD3 define delay d3best define delay cycle define loopcounter tmpTD define loopcounter TDtot define delay rest define delay Spik int define delay showInASED2 define delay ratioOK

```
; Calculate best d3 for rotor synchronisation
"tmpD3=(d6+p4/2)*cnst31"
"d3best=(1s*(tmpD3+1)/cnst31)-d6-(p4/2.0)"
;calculate minimum TD to set
"tmpTD=0.5*(((d6*2+d3*2+p4)*122)+d6+d3)/dw"
"TDtot=(tmpTD+1) *2"
"rest=abs(aq-(TDtot*dw))"
"Spik int=1s/(d6*2+d3*2+p4)"
"cycle=d6*2+d3*2+p4"
"ratioOK=cycle/(2*dw)"
; to make TDtot, etc. show up in ased
"showInASED2=TDtot+d3best+Spik_int+cycle+ratioOK"
define delay Dmin
define loopcounter lmin
define delay delA
define delay delAa
define delay delAb
define delay delB
"Dmin=(2*p1+d0+2u)+0.4u"
"lmin=(Dmin*cnst31)+1"
"delA=(((1s*lmin)/cnst31)-2u-p4)/2.0"
"delB=(((1s*lmin)/cnst31)-2u-d0-p1*2.0)/2.0"
"delAa=1s/cnst31+0.5s*(lmin%2)/cnst31-p3/2"
"delAb=1s/cnst31+0.5s*(lmin%2)/cnst31"
define loopcounter LCounter
define delay dummy
#ifndef SR4
#define _SFAM
#endif
#ifdef SFAM
"p6=1s/cnst31"
"LCounter=(p16*cnst31/1e6+0.5)"
"p17=LCounter*p6"
"dummy=cnst31+cnst30+cnst3+13+p17"
#endif
#ifdef _SR4
"p6=(0.25s/cnst31)"
"LCounter=(p16*cnst31/1e6+0.5)"
"p17=LCounter*p6*4"
"dummy=p17"
#endif
; counter for cycling SR4
"10=0"
;topspin 2.1 only
"in0=inf1"
;duty cycle
define delay pulsef1
define delay scandelay
"pulsef1=p2*2+p3+p4*(122+2)"
"scandelay=d1+p16+aq+100m"
"cnst60=pulsef1/scandelay"
1 ze
2 100m decF2off decF3off
```

```
"Dmin=(2*p1+d0+2u)+0.4u"
"lmin=(Dmin*cnst31)+1"
"delA=(((1s*lmin)/cnst31)-2u-p4)/2.0"
"delAa=1s/cnst31+0.5s*(lmin%2)/cnst31-p3/2"
"delAb=1s/cnst31+0.5s*(lmin%2)/cnst31"
"delB=(((1s*lmin)/cnst31)-2u-d0-p1*2.0)/2.0"
;SR4 manual cycling
10u iu0
#ifdef SR4
#ifndef opt1D
"cnst47=180*(((10-1)/4)%2)"
"cnst46=180*(((10-1)/16)%2)"
#else
"cnst47=180*(((10-1)/8)%2)"
"cnst46=180*(((10-1)/32)%2)"
#endif
10u ip16+cnst46
10u ip17+cnst47
#endif
  PRESAT1(f1)
  d1
  STARTADC
  RESETPHASE
  1u REC_BLK
  1u SGU3_pulse
  DFSpulse
  5u pl21:f1 pl23:f3
  (p3 ph1):f1
  delAa decF2t1on
;----- D, J-HMQC -----
#ifdef _SFAM
SFAM1, (p6:spf5 ph4):f3
lo to SFAMl1 times LCounter
#endif
#ifdef _SR4
sr4_1, (p6 ph16<sup>^</sup>):f3
       (p6 ph16^):f3
       (p6 ph16^):f3
       (p6 ph16^):f3
  lo to sr4 1 times LCounter
#endif
  111
  (delB pl3 pl ph11 d0 pl ph12 delB):f3 (delA p4 ph2 delA ):f1
  1u pl23:f3
#ifdef _SFAM
SFAM12, (p6:spf5 ph5):f3
lo to SFAM12 times LCounter
#endif
#ifdef SR4
sr4_2, (p6 ph17^):f3
       (p6 ph17^):f3
       (p6 ph17^):f3
       (p6 ph17^):f3
  lo to sr4 2 times LCounter
#endif
  delAb decF2off
;----- CPMG acq -----
  d6 decF2aqon decF3on
  2u
  del3
```

```
129
```

(p4 ph7):f1 del3 1u DWL CLK ON 1u SGU3 observe d6 REC UNBLK 3 d6 REC UNBLK 1u REC BLK 1u del3 SGU3 pulse (p4 pl21 ph8):f1 211 del3 SGU3 observe d6 REC_UNBLK lo to $\overline{3}$ times 122 d6 del3 REC BLK rest decF3off decF2off 1u DWL_CLK_OFF rcyc=2 ; go=2 ph31 decF2aqon decF3on 1u decF3off decF2off 100m mc #0 to 2 F1PH(ip11,id0) exit #ifndef opt1D ;phase cycling for 2D ph0=0 ;ph1={0 0 2 2}*2 ph1=0 ;ph2=1 ph2={0 0}^21^3 ph4={0}*16 {2}*16 ph5={0}*8 {2}*8 ph7=1 ph8=1 ;ph7={1}*16 {3}*16 ;ph8={1}*32 {3}*32 ph11=0 ph12=0 2 ;ph12=0 0 ph30=0 ;ph31={{{{0 2 2 0}*2}*2}^2; over 64 phases ph31={0 2}^0^2^2; over 64 phases ph31=ph12+2*ph2+0*ph4+0*ph5 ;ph31={0 0 2 2}*2 {3 1 1 3}*2 ph16=(360) 90 270 90 270 270 90 270 90 210 30 210 30 30 210 30 210 330 150 330 150 150 330 150 330 ph17=(360) 90 270 90 270 270 90 270 90 210 30 210 30 30 210 30 210 330 150 330 150 150 330 150 330 #else ; phase cycling for 1D optimization ph0=0 ph1={0 0 0 0 2 2 2 2}*2 ph2=1 ph4={0}*16 {2}*16 ph5={0}*8 {2}*8 ph7={1}*32 {3}*32 ph8={1}*64 {3}*64 ph11=0 ph12=0 2 1 3 ph30=0 ph31={{{{0 2 1 3 2 0 3 1}*2}*2}^2}^2 ph16=(360) 90 270 90 270 270 90 270 90 210 30 210 30 30 210 30 210 330 150 330 150 150 330 150 330

ph17=(360) 90 270 90 270 270 90 270 90 210 30 210 30 30 210 30 210 330 150 330 150
150 330 150 330
#endif
; set phases for presat : ph19 and ph20

A.2. J-RINEPT-CPMG pulse sequence

presatPH

This sequence was used on AV-II Bruker console driven by topspin2.1.

```
; ineptrd cpmg.jt
; J-RINEPT with cpmg detection
; CPMG works on Avance-II. It need to modify for Avance-III
; with decoupling during acquisition
; AUTHOR
; Julien TREBOSC / Hiroki NAGASHIMA
;pl1 : power level for p1,p2
;pl21 : power level for p3,p4
;pl22 : power level for p5 (CPMG)
;pl12: f2 channel - power level for CPD/BB decoupling
;pl13: f2 channel - power level for CPD/BB decoupling
;p1 : 90 degree @ pl1
;p2 : 180 degree @ pl1
;p3 : 90 degree @ pl21
;p4 : 180 degree @ pl22 for CPMG
;p5 : 180 degree @ pl21
;d1 : relaxation delay; 1-5 * T1
;d4 : J-inept mixing delay/2
;d44 : J-inept mixing delay
;
     1/(6J(XH)) XH, XH2, XH3 positive
      1/(4J(XH))
                 XH only
;
     1/(3J(XH)) XH, XH3 positive, XH2 negative
;d5 : J-inept refocusing delay/2
;d55: J-inept refocusing delay
     1/(4J(XH))
;
;d6 FID decay time for CPMG
;d3 dead time for CPMG
;122 number of CPMG echoes
;cnst31 : spinning speed (Hz)
;ZGOPTNS : -DPRESATf3 -DPRESATf1 -DdecF2aq -DdecF2mix -DdecF2t1 -D DFS -DnoDelSync
;NS: 32 * n, total number of scans: NS * TDO
;DS: 16
;cpdprg1: decoupling during mix
;cpdprg2: decoupling during t1/AQ
;cpdprg3: decoupling during AQ
;pcpd2: cpd pulse on channel f2
;duty cycle
define delay pulsef1
define delay pulsef3
define delay scandelay
"pulsef1=p2*2+p1+p4*(122+1)"
"pulsef3=(p3+p5)*2"
"scandelay=d1+d4+d5+aq+3m+30m"
"cnst63=pulsef1/scandelay"
#include <Avancesolids.incl>
#include "presat.incl"
#ifndef PRESATf3
#undef PRESAT2(f3)
```

```
#define PRESAT2(f3)
#endif
#ifndef PRESATf1
#undef PRESAT1(f1)
#define PRESAT1(f1)
#endif
#include "decouple.incl"
#ifdef decF3aq
#define decF3on cpds3:f3
#define decF3off do:f3
#else
#define decF3on
#define decF3off
#endif
#ifdef decF2all
#define decF2mix
#define decF2t1
#define decF2AQ
#endif
#ifdef decF2mix
#define decF2
#define decF2mixon cpds1:f2
#else
#define decF2mixon
#endif
#ifdef decF2t1
#define decF2
#define decF2t1on cpds2:f2
#else
#define decF2t1on
#endif
#ifdef decF2aq
#define decF2
#define decF2aqon cpds2:f2
#else
#define decF2aqon
#endif
#ifdef decF2
#define decF2off do:f2
#else
#define decF2off
#endif
#ifdef DFS
;p10 DFS/HS pulse
;spname0 DFS/HS shape pulse
;sp0 DFS/HS shape power
#define DFSpulse (5u p10:sp0 ph10 5u):f3
#else
#define DFSpulse
#endif
define delay del3
"del3=d3-2u"
define loopcounter tmpD3
define delay d3best
define delay cycle
```

```
define loopcounter tmpTD
define loopcounter TDtot
define delay rest
define delay Spik int
define delay showInASED2
define delay ratioOK
define delay tldelay
; Calculate best d3 for rotor synchronisation
"tmpD3=(d6+p4/2)*cnst31"
"d3best=(1s*(tmpD3+1)/cnst31)-d6-(p4/2.0)"
;calculate minimum TD to set
"tmpTD=0.5*(((d6*2+d3*2+p4)*122)+d6+d3)/dw"
"TDtot=(tmpTD+1) *2"
"rest=abs(aq-(TDtot*dw))"
"Spik int=1s/(d6*2+d3*2+p4)"
"cycle=d6*2+d3*2+p4"
"ratioOK=cycle/(2*dw)"
; to make TDtot, etc. show up in ased
"showInASED2=TDtot+d3best+Spik_int+cycle+ratioOK+cnst63"
"p5=p3*2"
"d0=0"
#ifdef _synct1
"tldelay=d0+(1s/cnst31)-p3/2"
#else
"tldelay=d0"
#endif
#ifndef noDelSync
"14=d4*cnst31"
"d14=(1s*14/cnst31)-p3/2.0-larger(p2,p5)/2.0-1u"
"d24=(1s*14/cnst31)-larger(p3,p1)/2.0-larger(p2,p5)/2.0"
#else
"d14=d4"
"d24=d4"
#endif
"d44=2.0s*14/cnst31"
#ifndef noDelSync
"15=d5*cnst31"
"d15=(1s*15/cnst31)-larger(p3,p1)/2.0-larger(p2,p5)/2.0"
"d25=(1s*15/cnst31)-larger(p2,p5)/2.0-1u"
"d55=2.0s*15/cnst31"
#else
"d15=d5"
"d25=d5"
#endif
"in0=inf1"
1 ze
2 30m decF3off decF2off
#ifdef synct1
"t1delay=d0+(1s/cnst31)-p3/2"
#else
"tldelay=d0"
#endif
 PRESAT2(f3)
 d1
  STARTADC
 RESETPHASE
  1u REC BLK
```

```
1u SGU1 pulse
  PRESAT1(f1)
  DFSpulse
; ----- INEPT part -----
 10u pl21:f3 pl1:f1
  0.1u decF2t1on
  (p3 ph1):f3
  tldelay
 lu decF2off
  d14 decF2mixon
  (center (p5 ph2):f3 (p2 ph4):f1 )
  d24
  (center (p3 ph3):f3 (p1 ph5):f1 )
 d15
 (center (p5 ph2):f3 (p2 ph6):f1 )
  d25
  1u decF2off
; ----- CPMG acq -----
 d6 decF2aqon
  2u
  del3
 (p4 pl22 ph7):f1
  del3
  1u DWL_CLK_ON
 lu SGUI observe
 d6 REC UNBLK
3 d6 REC_UNBLK
  1u REC_BLK
  1u
  del3 SGU1_pulse
  (p4 pl22 ph7):f1
  2u
 del3 SGU1 observe
  d6 REC_UNBLK
 lo to \overline{3} times 122
 d6
  del3 REC_BLK
 d6 decF2off
  rest decF2off
 1u DWL_CLK_OFF
  rcyc=2
  30m mc #0 to 2 F1PH(ip1,id0)
exit
; Phase cycling
ph1 = 0 2
ph2=0
ph3=1
ph4={{0}*2}^2
ph5={{0}*4}^2
ph6={{0}*8}^2^1^3
ph7=0
ph31= {{{0 2}^0}^2}^02^2
ph30=0
ph10=0
; set phases for presat : ph19 and ph20
presatPH
```

A.3. Split-t1 STMAS with z filter and QCPMG pulse sequence

This sequence was used on AV-III Bruker console

```
;stmas split t1 Zcpmg.jt
; pulse sequence for (satellite transition) STMAS spectroscopy
; on 3/2 nuclei only
; with coherence transfer pathway 0 -> +1/-1 -> +2/-2 -> 0 -> -1/+1
; uses split t1 technique and z-filter
;then a cpmg train is added
; see J. Trebosc, J.-P. Amoureux, and Zhehong Gan, SSNMR 31 (2007) 1-9
; see JP Amoureux et al JMR 175,285 (2005)
; written by julien trebosc
; CHANGES :
;ns : 16 * n
;p1 : excitation pulse
;p2 : mixing pulse
;p3 : selective 90 degree pulse
;p4 : selective 180 degree pulse
;p7 : set delay such that delB>0.3u and delA>0
;pl1 : =119 dB, not used
;pl11 : power for hard pules
;pl21 : power for selective pulse
;11 : first d0 span 11 Tr
;17 : run time test counter
;d1 : recycle delay
;d4 : z-filter delay, typ. 20 us
;d23 : offset for d10/d11 calculation not being negative
;d6 : cpmg half echo delay
;d3 : for dead time
;p60: storage of cpmg cycle time
;cnst31 : spinning frequency
; in 0 : =1/spinning frequency for rotor synchronisation,
      or half of it for half rotor synchronisation
;
;FnMode : States or States-TPPI
;$COMMENT=stmas for 3/2 spins with t1 split and cpmg acquisition
;$CLASS=Solids
;$DIM=2D
;$TYPE=half integer quadrupoles
;$SUBTYPE=STMAS
;$OWNER=Trebosc
#include <Avancesolids.inc>
#ifdef PRESAT
#include "presat.incl"
#else
#define PRESAT1(f1)
#define presatPH
#endif
#ifdef decF2
#define decF2on cpds2:f2
#define decF2off do:f2
#include "decouple.incl"
#else
#define decF2on
#define decF2off
#endif
"p4=2*p3"
define delay del1
```

```
define delay del3
"del3=d3-2u"
"del1=del3+2u-((p3)/2)"
define loopcounter tmpD3
define delay d3best
;d3best set d3 to this value for rotr synchronized echoes
define loopcounter tmpTD
define loopcounter TDtot
;TDtot set TD to this value + dig filter to record all echoes
define delay rest
define delay Spik int
define delay showInASED
define delay cycle
define delay PTSperCycle
; Calculate best d3 for rotor synchronisation
"tmpD3=(d6+p4/2)*cnst31"
"d3best=(1s*(tmpD3+1)/cnst31)-d6-(p4/2.0)"
;"d3=d3best"
;calculate minimum TD to set
"tmpTD=0.5*(((d6*2+d3*2+p4)*122)+2*d6+2*d3+p4+4u)/dw"
"TDtot=(tmpTD+1) *2"
"cycle=(d6*2+d3*2+p4)"
"p60=cycle"
"PTSperCycle=cycle/(2*dw)"
"rest=aq-(TDtot*dw)"
"Spik int=1s/(d6*2+d3*2+p4)"
 to make TDtot, etc. show up in ased
"showInASED=TDtot+d3best+Spik int+p60+PTSperCycle"
#ifdef Sync
#define SyncP1
                0.3u trigpe4 \n\
                delA
                 if "dll-halfTr <= 0" goto 72419 \n
#define SyncP2
                  0.3u trigpe4
#else
#define SyncP1
#define SyncP2
#endif
define delay halfTr
define delay delA
define delay delB
"halfTr=0.5s/cnst31"
"delB=p7"
"delA=delB+(p2-p1)/2.0"
"d0=1s*(l1*1/cnst31)"
"d10=d0/9.0 -p1/2 -p4/2 +d23"
"d11=8*d0/9.0 - p2/2 - p4/2 -d23 -delB"
"in0=inf1"
"in11=8.0*in0/9.0"
"in10=in0/9.0"
dwellmode auto
1 ze
"showInASED=1us"
2 100m
"d10=d0/9.0 -p1/2 -p4/2 +d23"
"d11=8*d0/9.0 - p2/2 - p4/2 -d23 -delB"
#ifdef Sync
if "dll-halfTr <= 0" goto skipSync
```

```
;/* redefine dll for allowing rotor syncing when dll is longer than half rotor
period. Else syncing is skipped */
"d11=8*d0/9.0 - p2/2 - p4/2 -d23 -delB -halfTr"
skipSync, 1u
#endif
;presaturation only if -DPRESAT in ZGOPTNS
 PRESAT1(f1)
  d1
  (1u pl11 ph1):f1
  STARTADC
  RESETPHASE
  SyncP1
                      ; first pulse
  (p1 ph1):f1
  d10 decF2on
                      ; ST1Q evol
  (p4 pl21 ph2):f1
                      ; DQ filter
  d11
                      ; ST2Q evol
  SyncP2
72419 (delB pl11 ph3):f1
  (p2 pl11 ph3):f1
                   ; reconversion pulse
  50u ; Z filter delay
  (p3 pl21 ph4):f1 ; SPAM pulse
                     ; +1/-1 evolution for echo creation
  d6
  del1
  (p4 pl21 ph5):f1
  del3 START_NEXT_SCAN
  1u
  1u
  d6 RG ON
3 d6 RG_ON
  2u
  del3 RG OFF
  (p4 pl21 ph6):f1
  del3
  2u
  d6 RG ON
  lo to 3 times 122
  d6
  del3 RG OFF
  rest decF2off
  1u
  rcyc=2
 100m mc #0 to 2 F1PH(ip1,id0)
exit
ph30=0
ph1= 0 2
ph2= {{0}*2}^2
ph3= {{0}*4}^1^2^3
ph4={{0}*16}^2
ph5= 1
ph6= 1
ph31={{{0 2}^2}^20^2}^2 ; cycling of 32
;ph31=-ph1-ph2+2*ph3+ph4 for +1 +2 +1 -1 pathway
; phase of presat
presatPH
```
A.4. D-HUQC (with RN_n^{ν} recoupling) pulse sequence

```
;huqcDR-m1.jt
; for topspin 1 and 2
; for topspin 3 and more check for trunc function in lmin calculation
; hugc with direct dipolar recoupling
; version 1.0 (published online XXX)
; -----
; DESCRIPTION :
; hugc experiment using m = 1 gamma-encoded pulse sequences
; AUTHOR
; Olivier Lafon, Julien Trebosc, Hiroki Nagashima
; MODIFICATIONS :
;$COMMENT=HMQC with dipolar recoupling on direct channel
;$CLASS=Solids
;$DIM=2D
;$TYPE=
;$SUBTYPE=
;$OWNER=Trebosc
; -----
; PARAMETERS:
;ns... see below in phase cycling section
;d1 : recycle delay
;d4 : z-filter delay
;pl1 : RF power level p4/p5
;pl3 : RF power level p7
;pl23 : recoupling power level
;p4 : 90 degree pulse @ pl1
;p5 : 180 degree pulse @ pl1
;p6 : 180 degree pulse @ pl23
;p7 : 90 degree pulse @ pl3
;p16 : dipolar recoupling time [in us]
;cnst31 : =MAS spin rate
;FnMODE : States or States-TPPI
;ZGOPTNS : PRESATF1 PRESATF3 decF3 decF2t1 decF2aq
; PRESAT : send presaturation pulses on F1 can be replaced with DS=1 or 2 \,
; decF3 : applyies decoupling during aq on F3
; decF2aq : applyies decoupling during aq on F2 (1H)
; decF2t1 : applyies decoupling during t1 on F2 (1H)
#include "presat.incl"
#ifndef PRESAT
#undef PRESAT1(f2)
#define PRESAT1(f2)
#endif
#ifndef PRESATf1
#undef PRESAT2(f1)
#define PRESAT2(f1)
#endif
#ifdef decF3
#define dec
#define decF3on cpds3:f3
#define decF3off do:f3
#else
#define decF3on
#define decF3off
#endif
#ifdef decF2t1
#define decF2
#define decF2t1on cpds2:f2
```

#else #define decF2t1on #endif #ifdef decF2aq #define decF2 #define decF2aqon cpds3:f2 #else #define decF2aqon #endif #ifdef decF2 #define dec #define tppm #define decF2off do:f2 #else #define decF2off #endif #ifdef dec #include "decouple.incl" #endif define delay dummy #define ZGOPNTS ERROR #ifndef _R1425
#ifndef _R1635
#ifndef _R1845 #iIndef _R1043
#ifndef _R1023
#ifndef _R3 #undef ZGOPTNS ERROR #define ZGOPTNS_ERROR you must use ZGOPTNS -D_R1425 or -D_R1635 or -D_R1845 or -D R1023 or -D R3 #endif #endif #endif #endif #endif ZGOPNTS_ERROR #ifdef _R1023 ;this is R1023 symmetry "p6=(2.0/10)*1s/cnst31" "123=trunc(p16/((2.0e6/cnst31)/5)+0.5)" #define RNphase1 23400 #define RNphase2 12600 #define RNphase3 5400 #define RNphase4 30600 #endif #ifdef R1425 ;this is R1425 symmetry "p6=(2.0/14)*1s/cnst31" "123=trunc(p16/((2.0e6/cnst31)/7)+0.5)" #define RNphase1 24429 #define RNphase2 11571 #define RNphase3 6429 #define RNphase4 29571 #endif #ifdef R1635 ;this is R1635 symmetry "p6=(3.0/16)*1s/cnst31"

"123=trunc(p16/((3.0e6/cnst31)/8)+0.5)" #define RNphase1 23625 #define RNphase2 12375 #define RNphase3 5625 #define RNphase4 30375 #endif #ifdef _R1845 ;this is R1845 symmetry "p6=(4.0/18)*1s/cnst31" "123=trunc(p16/((4.0e6/cnst31)/9)+0.5)" #define RNphase1 23000 #define RNphase2 13000 #define RNphase3 5000 #define RNphase4 31000 #endif #ifdef R3 ;this is R3 symmetry "p6=(1.0/4.0) *1s/cnst31" "123=trunc(p16/((1e6/cnst31)/2)+0.5)" #define RNphasel 18000 #define RNphase2 18000 #define RNphase3 0 #define RNphase4 0 #endif "p5=2*p4" "p17=(123)*p6*2" "dummy=p17" define delay Dmin define loopcounter lmin #ifdef d0sync "d0=1.0s/cnst31-p7" #endif "Dmin=(2.0*p7+d0+0.1u)/2.0" "lmin=trunc(Dmin*cnst31)+1" "d62=((1s/cnst31)*lmin-p7-d0/2.0)" "d63=((1s/cnst31)*lmin-p4-p5/2.0)" ;topspin 2.1 and more only "in0=inf1" "dummy=p17+123" 1 ze #ifdef optMAS ; just for VCLIST to appear in ASED and saved with status acq params 12435 lu lo to 12435 times c #endif 2 100m decF2off decF3off "Dmin=(2.0*p7+d0+0.1u)/2.0" "lmin=trunc(Dmin*cnst31)+1" "d62=((1s/cnst31)*lmin-p7-d0/2.0)" "d63=((ls/cnst31)*lmin-p4-p5/2.0)" PRESAT2(f1) d1

```
10u pl23:f1 pl3:f3
  0.5u fq=cnst29:f1
  0.5u decF2t1on
RN 1, (p6 pl23 ph21):f1
         (p6 pl23 ph22):f1
  lo to RN 1 times 123
  (d62 p7 pl3 ph6 d0 p7 pl3 ph7 d62):f3 (p4 pl1 ph14 d63 p5 pl1 ph4 d63 p4 pl1
ph15):f1
RN_2, (p6 pl23 ph23):f1
         (p6 pl23 ph24):f1
  lo to RN 2 times 123
(p4 pl1 ph8):f1
   0.5u decF2off
  go=2 ph31 decF3on decF2aqon
  6.35u decF3off decF2off
  100m mc #0 to 2 F1PH(ip6, id0)
exit
#ifdef opt1D
;phase cycling for 1D
;ns : 8 * n
ph4 = \{\{1\} * 4\}^2
ph6=0 2 1 3; use to select p=-1 between the two p7 pulses
ph7=0
ph8=1
ph14=3
ph15=3
ph21=(36000) RNphase1
ph22=(36000) RNphase2
ph23=(36000) RNphase3
ph24=(36000) RNphase4
ph31=0 2 1 3
#else
;phase cycling for 2D
;ns : 4 * n
ph4={{1}*2}^2
ph6=0 2 ; use to select p=1 or -1 between the two p7 pulses
ph7=0
ph8=1
ph14=3
ph15=3
ph21=(36000) RNphase1
ph22=(36000) RNphase2
ph23=(36000) RNphase3
ph24=(36000) RNphase4
ph31={0 2}
#endif
ph0=0
; set phases for presat : ph19 and ph20
presatPH
```

A.5. D-HUQC (with R³ recoupling) pulse sequence

```
;huqcDR-R3.jt
; version 1.0 (published online XXX)
; ------
; DESCRIPTION :
; huqc experiment using R3
;
```

```
; AUTHOR
; Julien TREBOSC, Olivier Lafon, Hiroki Nagashima
; MODIFICATIONS :
;$COMMENT=HUQC with R3
;$CLASS=Solids
;$DIM=2D
;$TYPE=
;$SUBTYPE=
;$OWNER=Trebosc
; -----
; PARAMETERS:
;ns : 4 * n
;d1 : recycle delay
;pl1 : RF power level p1/p2
;pl3 : RF power level p3
;pl23 : SFAM power level
;p1 90 degree pulse @ pl1
;p2 180 degree pulse @ pl1
;p3 90 degree pulse @pl3
;p16 : R3 dipolar recoupling time
;cnst31 : =MAS spin rate
;cnst0 : factor for second pulse
;FnMODE : States or States-TPPI
;ZGOPTNS : PRESATF1 PRESATF3 decF3 decF2t1 decF2aq
; PRESAT : send presaturation pulses on F1 can be replaced with DS=1 or 2
; decF3 : applyies decoupling during aq on F3
; decF2aq : applyies decoupling during aq on F2 (1H)
; decF2t1 : applyies decoupling during t1 on F2 (1H)
#include "presat.incl"
#ifndef PRESAT
#undef PRESAT1(f2)
#define PRESAT1(f2)
#endif
#ifndef PRESATf1
#undef PRESAT2(f1)
#define PRESAT2(f1)
#endif
#ifdef decF3
#define dec
#define decF3on cpds3:f3
#define decF3off do:f3
#else
#define decF3on
#define decF3off
#endif
#ifdef decF2t1
#define decF2
#define decF2t1on cpds2:f2
#else
#define decF2t1on
#endif
#ifdef decF2ag
#define decF2
#define decF2aqon cpds2:f2
#else
#define decF2aqon
#endif
#ifdef decF2
#define dec
```

```
#define decF2off do:f2
#else
#define decF2off
#endif
#ifdef dec
#include "decouple.incl"
#endif
#ifdef d0sync
"d0=1s*11/cnst31-p3"
#endif
define delay Dmin
define loopcounter lmin
define delay delA
define delay delB
"Dmin=(2*p3+d0+2u)"
"lmin=(Dmin*cnst31/2.0)+1"
"delA=((1s*lmin)/cnst31)-1u - p2/2.0"
"delB=(((2s*lmin)/cnst31)-2u-d0-p3*2.0)/2.0"
define delay RF
define loopcounter LCounter
define delay dummy
"cnst0=2.0"
"p2=p1*cnst0"
#ifdef R3
"p6=1s/cnst31"
"l11=p16/(p6)"
"p17=p6*l11"
"RF=13*500000/p6"
"dummy=RF+p17"
#endif
"in0=inf1"
1 ze
#ifdef optMAS
; just for VCLIST to appear in ASED and saved with status acq params
12435 lu
lo to 12435 times c
#endif
2 100m decF2off decF3off
"Dmin=(2*p3+d0+2u)"
"lmin=(Dmin*cnst31/2.0)+1"
"delA=((1s*lmin)/cnst31)-1u - p2/2.0"
"delB=(((2s*lmin)/cnst31)-2u-d0-p3*2.0)/2.0"
 PRESAT2(f1)
 d1
 1u rpp3 rpp6
 10u pl1:f1 pl3:f3
 (p1 ph1):f1
 0.5u fq=cnst29:f1
 1u pl23:f1 decF2t1on
#ifdef _R3
```

```
R3 1, (p6 ph4):f1
  lo to R3 1 times 111
#endif
  111
  (delB pl3 p3 ph11 d0 p3 ph12):f3 (delA pl1 p2 ph2 delA ):f1
  1u pl23:f1
#ifdef _R3
R3_2, (p6 ph5):f1
  lo to R3_2 times 111
#endif
  1u decF2off
  go=2 ph31 decF2aqon decF3on
  1u decF3off decF2off
  100m mc #0 to 2 F1PH(ip11,id0)
exit
;phase cycling
ph0=0
ph1=3
ph4=2
ph5=0
ph12=0
#ifdef opt1D
ph2 = \{\{1\} * 4\}^2
ph11=0 2 1 3
ph31={0 2 1 3}
#else
ph2={{1}*2}^2
ph11=0 2
ph31=0 2
#endif
ph30=0
ph3=0
ph6=0
; set phases for presat : ph19 and ph20
presatPH
```

A.6. Including file (preset.incl) and AU program (for DFS and SFAM)

Include file presat.incl

```
;$COMMENT=presaturation loops
;$CLASS=Solids INCL
;$DIM=
;$TYPE=presaturation
;$SUBTYPE=
; $OWNER=Trebosc
;d20 : delai between Presat pulses (p20)
;pl20 : power of Presat pulses (p20)
;120 : number of Presat pulses (p20)
;p20 : Presat pulses
;ph20 : phase of Presat pulses (p20)
; second presat parameters
;d19 : delai between Presat2 pulses (p21)
;pl19 : power of Presat2 pulses (p19)
;119 : number of Presat2 pulses (p19)
;p19 : Presat2 pulses
;ph19 : phase of Presat2 pulses (p19)
#define PRESAT1(ch) 983547 d20 pl20:ch \n\
(p20 ph20^):ch \n\
lo to 983547 times 120
```

```
#define PRESAT2(ch) 9835472 d19 pl19:ch \n\
(p19 ph19^):ch \n\
lo to 9835472 times l19
#define PRESAT11(ch) 9835479 d20 pl20:ch \n\
(p20 ph20^):ch \n\
lo to 9835479 times l20
#define PRESAT22(ch) 98354729 d19 pl19:ch \n\
(p19 ph19^):ch \n\
lo to 98354729 times l19
#define presatPH ph19= 0 \n ph20= 0
```

DFS generator AU program

```
/* dfs.jt 16.11.2011
/*
   Short Description :
                                        */
/*
    Program to calculate shape file for double frequency */
/*
    sweep and subsequent data-acquisition
                                             */
/* Keywords :
                                      */
/*
    adiabatic sweep, shaped pulse, MQMAS
                                              */
Description/Usage:
/*
                                      */
/*
    This program runs with xaua from within poptau or
                                              * /
/*
    paropt etc.
/*
     This means it can be used to optimise the parameters */
/*
                                              * /
     for the sweep in an automatic way.
/*
    Do ased first to make sure that the parameters listed */
/*
    below are set appropriately:
                                              */
/*
                                         */
/*
    p2 : duration of the sweep
                                         * /
,
/*
                                              */
     sp1 : power level of the sweep
/*
                                              */
    spnam1 : DFSjt is always used as default name
/*
    cnst1 : (in kHz) Startfrequency of the sweep
                                              * /
/*
    cnst2 : (in kHz) Endfrequency of the sweep
                                              * /
/*
    cnst3 : (in ns) currently used to define the timing
                                              * /
/*
                                              */
         resolution of the sweep
/*
/*
                                              * /
    Make sure that a customer-made pulse program uses
                                              */
    these parameters for the same purpose!
/*
    The file which is created contains a comment line like:
                                                   */
/*
    ##USAGE= Frequency sweep of 100 kHz in 100 usec
                                                   */
/*
     to be able to remember what sweep had been used
                                                   */
/*
     This AU program is suitable to be used with the
                                              */
/*
                                        * /
    following library pulse programs:
/*
    dfs90sel : sweep followed by 90 degree sel. pulse */
/*
    Author(s) :
                                         */
/*
                                              */
     Name
          : Stefan Steuernagel
/*
    Organisation : Bruker Analytik
                                         * /
/*
    Email : stefan.steuernagel@bruker.de
                                              */
/*
    Name Date Modification:
                                        */
/*
              000817 created
                                              */
    ste
/*
              031128 changed to allow sweep of */
     ste
/*
                    fractions of rotor periods */
/*
                    by setting 10 = 1, 2, or 4 * /
/*
                    blank character included for
                                              * /
/*
                    npoints in parameter part */
     jt
/*
               111116 modification to match JT syntax */
/***
        /*
$Id: zg dfs,v 1.4 2003/12/03 10:05:07 es Exp $
*/
FILE *fwave;
char outfile[256],outputfile[256],filename[256];
```

```
double PI=3.14159265359;
double amplitude, t, Startfreq, Endfreq;
float Anfang, Ende;
float phase=0;
int npoints;
GETCURDATA
/* read parameters for sweep calculation from acqu-file
                                                               */
/* and store filename for shaped pulse
(void) strcpy(outfile, "DFSjt");
STOREPAR("SPNAM1", outfile);
// pulse length in us
FETCHPAR("P 2",&f1);
//printf("p2=%f",f1);
/* used for timing resolution of sweep in ns*/
/* must not be less than 50 ns */
FETCHPAR("CNST 3",&f2);
/* get start- and end-frequencies in kHz*/
FETCHPAR("CNST 1", &Anfang);
FETCHPAR("CNST 2",&Ende);
Startfreq=(double)Anfang;
Endfreq=(double)Ende;
/* calculate number points in the file */
npoints=round(f1/(f2*1e-3));
f2=f1/npoints*1000;
/* open outputfile for shaped pulse
                                                        */
(void) sprintf(outputfile, "%s%s", getstan(0, "lists/wave/user/"), outfile);
if ((fwave=fopen(outputfile, "w+")) == NULL ) {
       Perror(DEF ERR OPT,outfile);
       ABORT;
       }
/* store amplitude values in shaped pulse file
                                                      */
fprintf(fwave,"##TITLE= %s\n",outputfile);
fprintf(fwave,"##USAGE= Frequency sweep from %4.1f kHz to %4.1f kHz in %4.1f usec
with resolution %4.1f ns\n", Startfreq, Endfreq, f1, f2);
fprintf(fwave,"##JCAMP-DX= 5.00 $$ Bruker JCAMP library\n");
fprintf(fwave,"##DATA TYPE= Shape Data\n");
fprintf(fwave,"##ORIGIN= Bruker BioSpin GmbH\n");
fprintf(fwave, "##DATE= 00/01/20\n");
fprintf(fwave, "##TIME= 08:15:00\n");
fprintf(fwave, "##MINX= -1.000000e+02\n");
fprintf(fwave,"##MAXX= 1.000000e+02\n");
fprintf(fwave,"##MINY= 0.000000e+00\n");
fprintf(fwave,"##MAXY= 0.000000e+00\n");
fprintf(fwave,"##$SHAPE EXMODE= None\n");
fprintf(fwave,"##$SHAPE_TOTROT= 0.000000e+00\n");
fprintf(fwave,"##$SHAPE BWFAC= 0.000000e+00\n");
fprintf(fwave,"##$SHAPE_INTEGFAC= 7.460936e-01\n");
fprintf(fwave, "##$SHAPE_MODE= 1\n");
fprintf(fwave, "##NPOINTS= %d\n", npoints);
fprintf(fwave,"##XYPOINTS= (XY...YX)\n");
TIMES (npoints)
       t=(loopcount1*f1*1e-6)/npoints;
       d1=2*PI*Startfreq*1000*t;
       d2=(2*PI*((Startfreq*1000)-(Endfreq*1000))*t*t)/(2*f1*1e-6*(npoints-
1)/npoints);
       amplitude=cos( d1 - d2 );
       if (amplitude<0) {
              amplitude*=-1;
```

```
phase=180.0;
} else { phase=0.0; }
fprintf(fwave,"%3.6f, %3.6f\n",amplitude*100,phase);
END
fprintf(fwave,"##END\n");
fclose(fwave);
(void) sprintf(text,"parameters and waveform file stored!");
Show_status(text);
QUIT
```

SFAM generator AU program

```
parameters:
cnst0: max offset
cnst31: approximate spinning speed (rounded to match shape requirements)
cnst3:
            resolution
13: n=1 or 2
*****
FILE *fwave;
char outfile[256],outputfile[256],filename[256];
double PI=3.14159265359;
int points=0;
int ph=0;
int n=1;
float off, spin, step;
float plength;
int n50, n350, max;
/*******
CNST: float
L
     int.1
_
*******/
GETCURDATA
FETCHPAR("CNST 30",&off);
FETCHPAR("CNST 31", &spin);
FETCHPAR("L 3", &n);
FETCHPAR("CNST 3",&step);
// interval must be at least 350ns
// interval must be a multiple of 50ns
// pulse length must be a multiple of interval
// thus pulse length must be a multiple of 50ns
//calculate plength depending on spinning speed
plength=1e9/spin;
// we want to split plength in at least 20 steps
max=(int) (plength/20/50+0.5);
n50=(int) (plength/50.0+0.5);
11
printf("plengthini=%f,n50i=%f,rn50=%d,plength=%f\n",plength,plength/50.,n50,n50*50.
);
// find closed n50 that is multiple of at least 7 (so that step=n350*50>=350)
n50=findclosest(n50,max);
// plength is now a multiple of 50ns
plength=n50*50;
// step is a multiple of 50ns and is greater or equal than 350ns
n350=mult(n50,max);
step=n350*50;
// number of points is plength/step=n50/350
points=n50/n350;
//recalculate the spinning speed after rounded plength :
spin=le9/plength;
```

```
// printf("\npulse de %fns decoupe en %d intervales de
%fns\n",plength,points,step);
//store back possibly modified spinning speed and step
STOREPAR("CNST 31", spin);
STOREPAR("CNST 3", step);
/\star read parameters for sweep calculation from acqu-file
                                                               */
/* and store filename for shaped pulse
                                                        * /
(void) strcpy(outfile, "sfam2");
STOREPAR("SPNAM5", outfile);
/* open outputfile for shaped pulse
                                                        * /
(void) sprintf(outputfile, "%s%s", getstan(0, "lists/wave/"), outfile);
if ((fwave=fopen(outputfile, "w+")) == NULL ) {
       Perror(DEF ERR OPT,outfile);
       ABORT;
       }
/* store amplitude values in shaped pulse file
                                                        */
fprintf(fwave,"##TITLE= %s\n",outputfile);
fprintf(fwave,"##USAGE=SFAM\n");
fprintf(fwave, "##CNST31=%f\n", spin);
fprintf(fwave, "##CNST30=%f\n", off);
fprintf(fwave,"##CNST3=%f\n",step);
fprintf(fwave,"##L3=%d\n",n);
fprintf(fwave,"##JCAMP-DX= 5.00 $$ Bruker JCAMP library\n");
fprintf(fwave,"##DATA TYPE= Shape Data\n");
fprintf(fwave,"##ORIGIN= Bruker BioSpin GmbH\n");
fprintf(fwave,"##DATE= 00/01/20\n");
fprintf(fwave, "##TIME= 08:15:00\n");
fprintf(fwave, "##MINX= -1.000000e+02\n");
fprintf(fwave,"##MAXX= 1.000000e+02\n");
fprintf(fwave,"##MINY= 0.000000e+00\n");
fprintf(fwave, "##MAXY= 0.000000e+00\n");
fprintf(fwave,"##$SHAPE EXMODE= None\n");
fprintf(fwave, "##$SHAPE TOTROT= 0.000000e+00\n");
fprintf(fwave,"##$SHAPE_BWFAC= 0.000000e+00\n");
fprintf(fwave,"##$SHAPE_INTEGFAC= 7.460936e-01\n");
fprintf(fwave,"##$SHAPE MODE= 1\n");
fprintf(fwave, "##NPOINTS= %d\n", points);
fprintf(fwave, "##XYPOINTS= (XY...YX) \n");
int i:
double amp1, ph1, z;
for (i=0;i<points;i++) {</pre>
       amp1=sin(n*(i*1.0)/((points)*1.0)*2*PI)*100;
       ph1=sin(n*(i*1.0)/((points)*1.0)*2*PI)*off/(n*spin)*360/2/PI;
       if (amp1<0) { amp1=-amp1;ph1=ph1+180;}</pre>
       fprintf(fwave,"%12.6f, %12.6f\n", amp1, ph1);
fprintf(fwave,"##END\n");
fclose(fwave);
(void) sprintf(text,"%s file stored!offset=%3.6f spin=%3.6f points=%i
step=%f",outfile,off,spin,points,step);
Show status(text);
sleep(1);
/* start acquisition */
OUIT
// function that returns the first multiple of n50 greater or equal than 7
// but lower than max
```

```
int mult(int n50, int max) {
    int i=7;
    while ((n50%i)!=0) { i++; if (i>max) {i=0; break; }}
    // printf("pour n50=%d n350=%d", n50, i);
    return i;
    }
    int findclosest(int n50, int max) {
    int i, j;
        for (i=0; i<n50 ; i++) {
            for (j=-1; j<=1; j+=2) {
            // printf("fc : n50=%d j=%d, i=%d\n", n50+j*i, j, i);
            if (mult(n50+j*i, max)!=0) {return n50+j*i; }
        }
    }
}</pre>
```

Abstract

My PhD thesis focuses on the development of the through-bond and through-space correlation solid state NMR experiments involving half-integer quadrupolar nuclei in order to characterize chemical structure of inorganic material at atomic level. This thesis consists of two part.

First, we introduce two-dimensional (2D) ⁷¹Ga-⁷⁷Se through-bond and through-space heteronuclear correlation (HETCOR) experiments. Such correlations are achieved using (i) the *J*-mediated Refocused Insensitive Nuclei Enhanced by Polarization Transfer (*J*-RINEPT) method with ⁷¹Ga excitation and ⁷⁷Se Carr-Purcell-Meiboon-Gill (CPMG) detection, as well as (ii) the *J*- or dipolar-mediated Heteronuclear Multiple-Quantum Correlation (*J*- or *D*-HMQC) schemes with ⁷¹Ga excitation and quadrupolar CPMG (QCPMG) detection. These methods are applied to the crystalline β -Ga₂Se₃ and the 0.2Ga₂Se₃-0.8GeSe₂ glass. We also report 2D ⁷¹Ga Satellite Transition Magic-Angle Spinning (STMAS) spectrum of β -Ga₂Se₃ using QCPMG detection at high magnetic field, high Magic-Angle Spinning frequency, and high rf-field.

Second, we introduce novel sequences using indirect detection to correlate quadrupolar nuclei and spin-1/2 isotopes, other than ¹H and ¹⁹F. These sequences use γ -encoded symmetry-based RN_n^{ν} schemes that reintroduce the space component |m| = 1 of the heteronuclear dipolar coupling. These schemes can be applied to the indirectly detected spin in Dipolar-mediated Heteronuclear Multiple-Quantum Correlation (*D*-HMQC) sequence or to the detected isotope in a novel sequence, named Dipolar-mediated Heteronuclear Universal-Quantum Correlation (*D*-HUQC). The performance of the sequences have been compared to conventional *D*-HMQC with R³ and SFAM recoupling via SIMPSON simulations and NMR experiments, including ¹³C-{¹⁵N} heteronuclear correlation on glycine and ³¹P-²⁷Al ones on VPI-5 and Na7(AlP₂O₇)₄PO₄.